

A Quantum Monte Carlo Study of the Structural, Energetic, and Magnetic Properties of Two-Dimensional H and T Phase VSe₂

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ABSTRACT: Previous works have controversially claimed near-room- temperature ferromagnetism in two-dimensional (2D) VSe ₂ , with conflicting results throughout the literature. These discrepancies in magnetic properties between both phases (T and H) of 2D VSe ₂ are most likely due to the structural parameters being coupled to the magnetic properties. Specifically, both phases have a close lattice match and similar total energies, which makes it difficult to determine which phase is being observed experimentally. In this study, we used a combination of density functional theory, highly accurate diffusion Monte Carlo (DMC), and a surrogate Hessian line-search optimization technique to resolve the previously reported discrepancy in structural parameters and relative phase stability. With DMC accuracy, we		2.55 X Fit eqm. (H) 9 2.55 .50 9 2.50 .50 2.45 .50 2.45 .50 9 .50 1 .5 eqm. (H) 2.45 .50 9 .50 2.45 .50 9 .50 1 .5 eqm. (H) 2.45 .50 9 .50 9 .50 1 .5 eqm. (H) 2.45 .50 9 .50 1 .5 eqm. (H) 2.45 .5 9 .50 9 .50 10 .5 11 .5 12 .5 13 .5 14 .5 15 .5 16 .5 17 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5 .5

determined the free-standing geometry of both phases and constructed a phase diagram. Our findings demonstrate the successes of the DMC method coupled with the surrogate Hessian structural optimization technique when applied to a 2D magnetic system.

ne of the most promising two-dimensional (2D) magnetic materials that has been extensively studied experimentally and theoretically is 2D VSe₂. Similar to other 2D transition metal dichalcogenides (such as MoS_2),¹ VSe₂ exists in two phases, the T [octahedral phase (1T)-centered honeycombs phase that is metallic and the H [the trigonal prismatic phase (2H)-hexagonal honeycombs (see Figure 1)] phase that is semiconducting. Several experimental and theoretical studies have controversially claimed near-roomtemperature ferromagnetism in VSe2, with conflicting results throughout the literature. Density functional theory (DFT) along with classical Monte Carlo simulations have been used to obtain an estimate of the Curie temperature of H-VSe₂ (291 K),² but the model Ising Hamiltonian used did not take into account the magnetic anisotropy energies, which are essential for an accurate estimation of the Curie temperature of a 2D lattice. The Curie temperature of multilayered 2D H-VSe₂ has been experimentally measured to be 425 K, with the ferromagnetism softening as the thickness of the sample increases.³ Additionally, the experimental Curie temperature for monolayer T-VSe₂ has ranged from 300 to 470 $K^{4,5}$ depending on which substrate is used (MoS₂, graphite, or SiO₂-coated silicon). The experimental magnetization of T-VSe₂ has also been met with controversy, with values of 15 and 5 $\mu_{\rm B}$ [per formula unit (f.u.)] being reported from two separate studies.^{4,6} Insight has also been reported with regard to how the ferromagnetism is enhanced with defects, molecular adsorption, and the choice of substrate for VSe₂.^{4,5,7} Although recent reports have suggested that T-VSe₂ could be

experimentally paramagnetic,³ it is possible that this paramagnetism can be induced by magnetic anisotropy. In addition, a wide range of values have also been reported for the charge density wave (CDW) transition temperature for T-VSe₂, ranging from 120 to 350 K.^{3,6,8–10}

These discrepancies in the electronic and magnetic properties of either phase of 2D VSe₂ arise from the structural parameters of each phase being coupled closely to the magnetic and electronic properties and the external factors (substrates and defects) of the individual samples. One example of this has been a reported discrepancy in which phase (T or H) is energetically more favorable. The T and H phases have a close lattice match and similar total energies, which makes it difficult to determine which phase is being observed experimentally. Recently, it has been reported experimentally that the T phase is favored for bulk VSe₂, but with a decrease in dimensionality, the H phase transition can be realized by thermal annealing.¹¹ This same structural phase transition has even been reported by applying a biaxial strain of $\approx 3\%$ (from the calculated results).^{7,11,12} Researchers have

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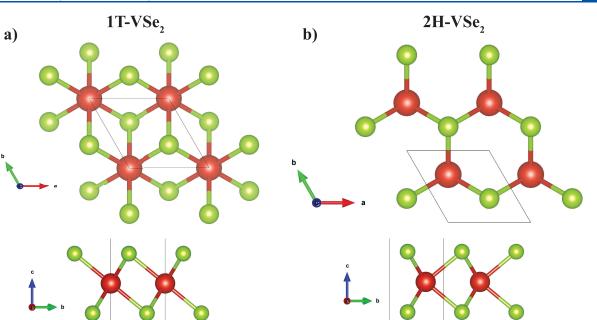


Figure 1. Top and side views of the atomic structure of monolayer VSe2 in the (a) 1T and (b) 2H phases.

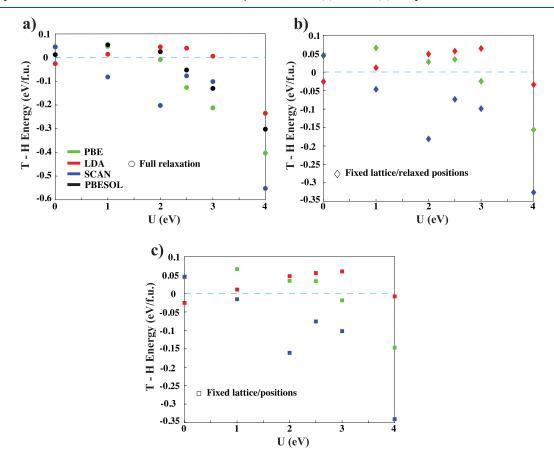


Figure 2. Relative (T - H) energy between T and H phase 2D VSe₂ as a function of the *U* parameter for several density functionals and methods of atomic relaxation: (a) fully relaxing the structure, (b) fixing the lattice and atomic positions to the U = 0 eV relaxed geometry of that particular functional and calculating the static energy, and (c) fixing the lattice to the U = 0 eV relaxed geometry of that particular functional and relaxing just the atomic positions. The dotted line indicates 0 eV.

proposed that this lattice strain can be induced by the mismatch that occurs from placing 2D VSe₂ on a substrate.^{7,12}

From a computational perspective, the results for \mbox{VSe}_2 depend strongly on which methodology is employed. In

most cases, DFT with an empirical Hubbard correction (+U) for correlated electrons is used.¹³ For example, if the *U* correction is applied for T- and H-VSe₂, the T phase is more energetically favorable, while if no *U* correction is applied, the

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method	T-VSe ₂		H-VSe ₂		
	a (Å)	$d^{\rm V-Se}$ (Å)	a (Å)	$d^{\rm V-Se}$ (Å)	$E^{\mathrm{T-H}}$ (eV/f.u.
PBE	3.336	2.489	3.333	2.502	0.045
PBE+U=2	3.435	2.526	3.364	2.520	-0.008
LDA	3.228	2.438	3.229	2.445	-0.026
LDA+U=2	3.277	2.455	3.266	2.464	0.045
SCAN	3.387	2.486	3.329	2.486	0.045
SCAN+U=2	3.462	2.524	3.353	2.502	-0.202
PBEsol	3.262	2.458	3.272	2.471	0.013
PBEsol+U=2	3.323	2.483	3.301	2.487	0.025
PBE-D2	3.323	2.484	3.318	2.496	0.010
PBE-D3	3.315	2.485	3.319	2.497	0.042
SCAN+rvv10	3.379	2.481	3.319	2.482	0.051
DMC	3.414(12)	2.505(7)	3.335(8)	2.503(5)	0.06(2)

Table 1. Lattice Constants, V–Se Distances, and Relative Energies (T - H) for T and H Phase 2D VSe₂ for Several Computational Methods^{*a*}

H phase is more favorable.¹⁴ In addition to the discrepancies in results calculated with DFT+*U*, results between van der Waals (vdW)-corrected functionals and hybrid functionals are also inconclusive¹⁴ in terms of predicting the relative phase stability. To alleviate the uncertainty in DFT methods, more sophisticated methods can be used such as diffusion Monte Carlo (DMC).¹⁵ DMC is a correlated, many-body electronic structure method that has been demonstrated to have success for the electronic and magnetic properties of a variety of bulk and 2D systems.^{16–24} This method has a weaker dependence on the starting density functional and *U* parameter and can successfully achieve results with an accuracy beyond the DFT +*U*.¹⁵

Due to the fact that T- and H-VSe₂ have structural parameters that are coupled to their electronic and magnetic properties, it makes it difficult to produce conclusive results that rely solely on DFT or DFT+U. For this reason, we employed our recently developed energy-based surrogate Hessian method for structural optimization with stochastic electronic structure theories (such as DMC)²² to obtain the geometric structure of T- and H-VSe₂ with DMC accuracy, resulting in high-accuracy bond lengths that resolve previous functional-dependent structural discrepancies. After obtaining an accurate geometry for both structures, we constructed a phase diagram between T- and H-VSe₂ using DMC-calculated energies and obtained accurate magnetic properties of each structure. The accurate estimates of the lattice geometry, relative phase energy, and DMC phase diagram assist in clarifying previously inconclusive theoretical and experimental results with regard to T and H phase VSe₂. It is important to note that the modeling of paramagnetism with computational methods imposes a great challenge, requiring the simulation of large supercells with different magnetizations, which is why we focus on the free-standing ferromagnetic ground states of both phases. A more robust treatment of the magnetic structure can be explored in the future but is beyond the scope of this work, which primarily focuses on determining the geometric structure and phase stability of 2D T- and H-VSe₂. For full details of the computational methods used, see the Supporting Information.

As an initial starting point for our study, we performed benchmarking DFT and DFT+*U* calculations using a variety of density functionals [local density approximation (LDA),²⁵ Perdew–Burke–Ernzerhof (PBE),²⁶ and strongly constrained and appropriately normed $(SCAN)^{27}$ meta-GGA functionals (see the Supporting Information for more details)] and the Vienna Ab initio Simulation Package (VASP) code for monolayer T-VSe₂ and H-VSe₂. The goal of these simulations was to assess how sensitive the relative energy between the T and H phase is with respect to functional and material geometry. Another goal of these simulations was to benchmark the structural parameters of each material with respect to several density functionals. It is advantageous to perform these reference calculations with VASP and projector-augmented wave (PAW) pseudopotentials^{28,29} as a precursor to the more expensive DMC calculations due to the fact that they require a much smaller cutoff energy and are more cost-effective for a large number of simulations. It is important to note that for all DFT and DMC simulations, we assumed a ferromagnetic ground state for both T- and H-VSe₂.

In Figure 2, we present a comprehensive look at the difference in total energy between T-VSe₂ and H-VSe₂, using several DFT functionals under different geometric constraints. We performed these calculations for a variety of U values in three different ways: fully relaxing the structure at each value of U (Figure 2a), fixing the lattice and atomic positions to the U= 0 eV relaxed geometry of that particular functional and calculating the static energy at each value of U (Figure 2b), and fixing the lattice to the U = 0 eV relaxed geometry of that particular functional and relaxing just the atomic positions at each value of U (Figure 2c). The results in Figure 2 indicate that there is a significant disagreement between DFT functionals, U value used, and material geometries, with all three factors playing a significant role in the energy difference between the T and H phases. Specifically, regardless of the relaxation method, all bare (no U correction) SCAN, PBE, and PBEsol functionals predict H favorable while bare LDA predicts T favorable. For all functionals, there is a critical value of U that reverses the relative phase stability, which is dependent on the functional and relaxation method. The SCAN functional with a U correction predicts T phase favorable, with larger energy differences. As shown in Figure 2, the trends in the relative phase stability between panels b and c of Figure 2 are nearly identical but significantly vary from those in panel a of Figure 2. This implies that the density functional is strongly coupled to material geometry, but the lattice constant change has a stronger effect on phase stability than atomic positions and bond distances. This is most prevalent for

higher U values (>2 eV), where the relaxed geometry changes more drastically with U. The interrelated nature of the material's geometry, density functional, and value of U are reasons to seek out higher levels of theory beyond DFT/DFT +U such as DMC to accurately determine the optimal geometry and relative energy between the phases of 2D VSe₂.

The relaxed lattice constants, V–Se distances, and T - H energies from Figure 2a are listed in Table 1 and Figure 3,

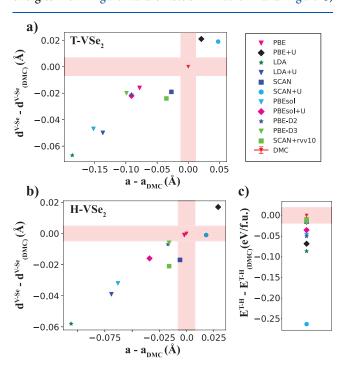


Figure 3. Summary of the deviation of the geometric properties relative to the DMC-calculated geometric properties for (a) T-VSe₂ and (b) H-VSe₂ and (c) deviation of the T – H energy relative to the DMC-calculated T – H energy for a variety of DFT functionals (U = 2 eV), where the DMC error bar (standard error of the mean) is represented by the red bars.

along with additional VASP reference calculations performed with the vdW-corrected functionals (PBE-D2,³⁰ PBE-D3,³¹ and SCAN+rvv10³²). The DMC-computed parameters are also given for comparison in Table 1 and Figure 3 (more discussion to follow). We observe an $\approx 7\%$ variability in the lattice constant across the different methods for T-VSe₂ and an \approx 4% variability in the lattice constant across the different methods for H-VSe₂. Between both phases, we observe an \approx 3% variability in the V–Se distance (d^{V-Se}) . To contextualize our results with recent theoretical calculations of 2D T-VSe₂ (which used a widely adapted effective U value of 3 $eV^{14,33,34}$), we note that our lattice constant results for PBEsol+U=2 are in excellent agreement with recently reported PBEsol U = 3results (within 1%).33 Most strikingly, the energy difference between the T and H phases (E^{T-H}) drastically varies depending on the material geometry and computational methodology, ranging from -0.2 to 0.06 eV/f.u. Due to the fact that a strain-induced phase transition has been reported between T- and H-VSe₂, 7,11,12 we decided to perform additional VASP benchmarking calculations that involved the application of tensile and compressive strain for each monolayer. We performed these calculations for PBE, SCAN, and LDA (with U = 0 eV and U = 2 eV), starting from the U =

0 eV geometry for each functional. The resulting equations of state are depicted in Figure S3. As shown in the figure, the equation of state and resulting strain-induced phase transition are entirely dependent on the functional and U value, with no consistent trend.

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The strong sensitivity of each monolayer with respect to geometry and functional is grounds for using a higher-order method such as DMC to obtain a statistically accurate estimate of the lattice parameters and relative energy between phases. Prior to performing the DMC/line-search calculations, we optimized our nodal surface (orbitals selected for DFT wave function generation). Because DMC has a zero-variance property, this means that as the trial wave function approaches the exact ground state, the statistical fluctuations in the energy decrease to zero.¹⁵ Although there have been instances in which various sophisticated methods have been used to optimize the nodal surface, $^{35-38}$ we employed the PBE+U approach, where the Hubbard (U) value was used as a variational parameter to optimize the nodal surface using DMC (similar to other successful DMC studies of magnetic materials^{16,20,21,24,39–41}). We performed these calculations for both T- and H-VSe₂ (24-atom supercells), where we tuned the U value from 1 to 4 eV while creating the trial wave function and computed the DMC energy. The results of these calculations are depicted in Figure 4, where we observe that

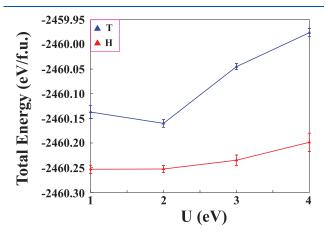


Figure 4. DMC-calculated total energies of a 24-atom supercell [normalized per formula unit (f.u.)] of 2D T (blue) and H (red) phase VSe_2 calculated as a function of the *U* parameter used to variationally determine the optimal trial wave function. The DMC error bars represent the standard error of the mean.

a U of 2 eV yields the lowest energy for both phases. It is important to note that for the H phase, the DMC energies for U values of 1 and 2 eV are statistically identical. On this basis, we created the trial wave function using PBE+U (U = 2 eV) for all subsequent DMC calculations within the surrogate Hessian line search for both phases (all 52 DMC energy evaluations). Because we obtained an optimal U value of 2 eV for both materials, we focused our DFT+U benchmarking efforts more on a U value of 2 eV (Figures 2, 3, and 6, Table 1, and Figure S3).

On the basis of the DMC line-search results, we determined accurate bounds on the lattice parameter (*a*) and off-plane displacement of Se (*z*), within an error tolerance of ≤ 0.018 Å for both parameters. This translates to within $\approx 0.5\%$ accuracy in a parameter set of *a* and d^{V-Se} with 95% statistical confidence. Convergence (absence of significant displacements)

outside of the error tolerance) was achieved after two parallel line-search iterations for both phases. This convergence is illustrated in Figure S4, where the convergence of the parameter offsets of *a* and *z* and the convergence of the total energy per formula unit are depicted for both T and H phase 2D VSe₂ for the initial DFT-relaxed structure (1) and both subsequent iterations of DMC (2 and 3). In addition, the final energies of both of the fitted structures (squares) are given.

The final geometric parameters and relative phase energies determined with DMC are listed in Table 1 and Figure 3. For T-VSe₂, we determined a lattice constant of 3.414(12) Å and a V-Se distance of 2.505(7) Å. For H-VSe₂, we determined a lattice constant of 3.335(8) Å and a V–Se distance of 2.503(5) Å. The DMC finite-size extrapolated energy difference (T - T)H) between the two phases was determined to be 0.06(2) eV/f.u., indicating that in free-standing form at the equilibrium geometry, H-VSe₂ is favored over T-VSe₂. Upon comparison of these DMC results to the other DFT functionals in Table 1 and Figure 3, it is clear that very few DFT functionals can reproduce the DMC results for the lattice constant, V-Se distance, and relative energy difference. The SCAN functional comes the closest to reproducing all three simultaneous DMC values but still falls slightly short for the V-Se distances of both phases and the lattice constant of T-VSe₂. The fact that SCAN+U successfully predicts the structural properties (for H-VSe₂) and the fact that SCAN+rvv10 produces an energy difference closest to the average DMC energy difference for both phases loosely imply that a simultaneous description of correlated magnetism and vdW interactions is needed to correctly represent the physics of VSe₂. Experimental measurements of the lattice constant and V-Se distance of freestanding monolayer VSe2 are scarce and often dependent on external factors such as the substrate (more discussion to follow) and sample preparation technique.^{4,5,42,43} However, Chen et al.⁴² have recently reported a lattice constant of 3.4 Å for thin films of T-VSe₂, and Liu et al.⁴³ have recently reported a lattice constant of 3.3 Å for epitaxially grown monolayer H-VSe₂. Both of these measured values are in excellent agreement with our DMC-computed lattice constants. Additionally, we determined the near-equilibrium PES of both T and H 2D VSe₂ with DMC accuracy, which are both depicted in Figure S5.

The phase diagram presented in Figure 5 is based on similar fits to data, where the z displacement has been remapped to d^{V-Se} . This DMC phase diagram can directly be compared to the energy versus strain DFT benchmarking calculations in Figure S3, which emphasizes the need for an accurate representation of the phase boundary between the two phases. The free-standing geometries of both T and H lie in the energetic H phase, but a slice of the phase diagram along a d^{V-Se} of 2.505 Å indicates that the T phase becomes favorable over H at biaxial strain of approximately $a \ge 3.5$ Å. This implies that in free-standing form, once T-VSe₂ is positively strained at least \approx 2.5%, the T phase is favored over H. Alternatively, if free-standing H-VSe₂ is positively strained at least \approx 5%, the T phase is also favored over H. This strain can easily be accomplished by placing monolayer VSe₂ on a substrate with a significant lattice mismatch. In fact, this type of mismatch has been reported to alter the material properties,^{4,5,44,45} significantly contributing to the controversies of Tand H-VSe₂ (for energetic favorability and magnetic properties). Whether the changes in energetic favorability or magnetic properties with respect to the substrate are due to

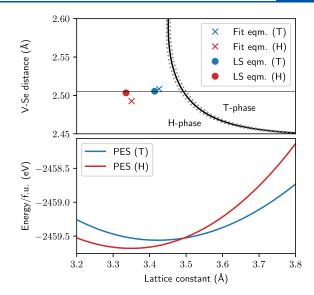


Figure 5. Phase diagram of 2D VSe₂ in terms of *a* and d^{V-Se} (top). The phase boundary (solid black line) is estimated from bicubic fits. To ensure the quality of the fits, the estimated ±0.01 eV error contours (dotted line) and the minima from the bicubic fits (times signs, Fit eqm.) and the line search (circles, LS eqm.) are all well separated. Slices of the PES at $d^{V-Se} = 2.505$ Å (bottom).

lattice mismatch or more complicated interactions between the substrate and the monolayer remains to be answered and is beyond the scope of this work, which has focused solely on the free-standing forms of T- and H-VSe₂. However, such calculations can be employed for future work using higher-order methods such as DMC. The proximity of the phase boundary between the T and H phases (Figure 5) is emphasized by the small energy difference between the two phases [0.06(2) eV/f.u., at the equilibrium geometry] between the two curves. Because this energy difference is so close to room temperature ($\approx 0.024 \text{ eV}$), this implies that a process such as thermal annealing can easily induce a phase transition. In fact, recently it was demonstrated that a structural phase transition of multilayer VSe₂ from T to H occurs through annealing at 650 K, along with a metal—insulator transition.¹¹

To gain a deeper understanding of the magnetic properties of 2D T- and H-VSe₂, we extracted the spin densities (using a trial wave function at U = 2 eV and a 24-atom supercell at the final equilibrium geometry predicted by DMC/line search). We went on to plot the radially averaged spin densities as a function of distance, separately for V and Se for T- and H-VSe₂ (depicted in Figure 6a-d). This allows us to view the spatial variations in spin density. Additionally, we benchmarked these V and Se radially averaged densities with PBE+U (U = 2 eV) using NC pseudopotentials at the equilibrium geometry (the calculation required to create the trial WF for the subsequent DMC runs). As shown in panels a and c of Figure 6, there is a substantial difference in the V spin density between DMC and PBE+U (U = 2 eV) for both T and H phases. This same substantial difference between DMC and PBE+U also occurs for the total charge density. This discrepancy is most prevalent near the radial density peak (peak of the d orbital) and can be attributed to the fact that DFT functionals (even with the added Hubbard correction) tend to delocalize and unsuccessfully capture 3d orbitals. This large discrepancy in the spin densities highlights the need for more accurate, many-body computational methodologies for correlated materials such as

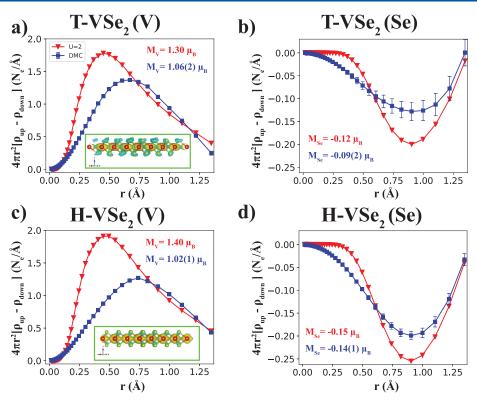


Figure 6. Radially averaged spin density ($\rho_{up} - \rho_{down}$) as a function of distance, calculated with DMC and PBE+U (U = 2 eV) of (a) V and (b) Se for 2D T-VSe₂ and (c) V and (d) Se for 2D H-VSe₂. The insets of panels a and c depict the spin isosurface density of T-VSe₂ and H-VSe₂, respectively, where the isosurface value was set to $6 \times 10^{-3} \text{ e/Å}^3$. The standard error of the mean for DMC is indicated by blue error bars.

VSe₂, where DFT fails. In contrast, there is closer agreement between the DMC and PBE+U spin densities for Se in T- and H-VSe₂ (see Figure 6b,d). The spin density isosurfaces of each phase ($\rho_{up} - \rho_{down}$) are depicted in the insets of panels a and c of Figure 6 for T-VSe₂ and H-VSe₂, respectively. For both phases, we observe the V atoms are highly spin-polarized, while the Se atoms are slightly antiparallel with respect to the V atoms. For more calculation details with regard to spin density, see the Supporting Information.

Finally, we estimated the site-averaged atomic magnetic moments per V and Se for both T and H phases by integrating the DMC and PBE+U spin densities depicted in Figure 6. At the DMC level, we estimated magnetic moments of 1.06(2) $\mu_{\rm B}$ for V and -0.09(2) $\mu_{\rm B}$ for Se in T-VSe₂ and magnetic moments of 1.02(1) μ_B for V and -0.14(1) μ_B for Se in H-VSe₂. At the PBE+U (U = 2 eV) level, we estimated magnetic moments of 1.30 $\mu_{\rm B}$ for V and $-0.12 \ \mu_{\rm B}$ for Se in T-VSe₂ and magnetic moments of 1.40 $\mu_{\rm B}$ for V and $-0.15 \,\mu_{\rm B}$ for Se in H-VSe₂. Consistent with the radial spin density results in Figure 6, we find that the DMC and PBE+U magnetic moments for Se are in much closer agreement than for V (for both T and H phases). By analyzing the spin densities and obtaining the onsite magnetic moments, we obtain a clear picture of how the magnetization of each ion depends on the computational method used, serving as a benchmark for the magnetic properties of 2D VSe₂.

In this work, we used a combination of DFT, DMC, and a recently developed surrogate Hessian line-search optimization technique to resolve the previously reported discrepancy in structural parameters and relative phase stability of monolayer $T-VSe_2$ and $H-VSe_2$. Using these methods, we determined the lattice constant and V–Se distance (with DMC accuracy) to

be 3.414(12) and 2.505(7) Å, respectively, for T-VSe₂ and 3.335(8) and 2.503(5) Å, respectively, for H-VSe₂. In addition, we find the relative energy between the phases (T - H) to be 0.06(2) eV/f.u. at the DMC level, indicating that in freestanding form, H-VSe₂ is more energetically favorable than T-VSe₂. We went on to obtain a phase diagram between T and H phases from the potential energy surface (PES) and determined that a phase transition can be induced by strain or mechanisms such as thermal annealing. Additionally, we benchmarked the magnetic properties such as spin density and on-site magnetic moment for both phases and find substantial differences between DMC and DFT. The results of this study demonstrate the successes of the DMC method coupled with the surrogate Hessian line-search structural optimization technique when applied to a 2D magnetic system. The estimates for the lattice constant, bond distance, relative phase energy, and extracted structurally dependent phase diagram assist in clarifying previously inconclusive theoretical and experimental results with regard to T and H phase VSe₂.

ASSOCIATED CONTENT

Data Availability Statement

The data from this work are available at https://figshare.com/ projects/2D_VSe2_Quantum_Monte_Carlo/162613.

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpclett.3c00497.

Computational details of DFT and QMC, plane wave cutoff converge, k-point convergence, time step convergence, details of spin density estimator, additional details of the surrogate Hessian accelerated optimization method, additional DFT benchmarking, and further details of the line-search convergence and potential energy surfaces (PDF)

Transparent Peer Review report available (PDF)

Accession Codes

Software packages mentioned in the article can be found at https://github.com/usnistgov/jarvis. Note that the use of commercial software (VASP) does not imply recommendation by the National Institute of Standards and Technology.

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Notes

The authors declare no competing financial interest.

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