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Letter

Improved interspecies optical clock comparisons through differential spectroscopy

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Comparisons of high-accuracy optical atomic clocks¹ are essential for precision tests of fundamental physics², relativistic geodesy³⁻⁵ and the anticipated redefinition of the second by the International System of Units⁶. The scientific reach of these applications is restricted by the statistical precision of comparison measurements between clocks realized with different atomic species. The instability of individual clocks is limited by the finite coherence time of the optical local oscillator, which bounds the maximum atomic interrogation time. Here we experimentally demonstrate differential spectroscopy⁷, a comparison protocol that enables interrogating times beyond the optical local oscillator coherence time. By phase coherently linking a zero-dead-time⁸ Yb optical lattice clock with an Al⁺ single-ion clock via an optical frequency comb and performing synchronized Ramsey spectroscopy, we show an improvement in comparison instability relative to previous results⁹ of nearly an order of magnitude. This result represents one of the most stable interspecies clock comparisons to date.

Atomic clocks based on optical transitions in single trapped ions or ensembles of neutral atoms in optical lattices have achieved remarkable fractional systematic uncertainties at the 10⁻¹⁸ level or below^{3,10-13}, establishing them as the most accurate measurement devices of any kind. Beyond their application in timekeeping, this unrivalled accuracy makes optical atomic clocks ideal sensors for a variety of scientific and technological applications. For example, the most stringent constraints on models of ultralight dark matter^{9,14} are set by the frequency ratio measurements of clocks based on different atomic species, with correspondingly different sensitivities to proposed physics beyond the Standard Model¹⁵. In addition to high accuracy, these constraints and other sensing applications are enhanced by the high comparison bandwidth and stability of interspecies clocks. The fractional frequency instability of a clock based on Ramsey spectroscopy of *N* uncorrelated atoms is fundamentally limited by the quantum projection noise (QPN) at

$$\sigma_{\rm QPN}(\tau) = \frac{e^{\Gamma_{\rm c} T/2}}{2\pi v_{\rm c} \sqrt{NT\tau}},\tag{1}$$

where Γ_c is the excited-state decay rate of the clock transition, v_c is the unperturbed atomic transition frequency, τ is the averaging time and T is the Ramsey free-evolution (interrogation) time. The QPN limit is particularly restrictive for single-ion clocks (N=1), as opposed to lattice clocks that routinely operate with $N \approx 10^4$ atoms. However, singly and multiply ionized¹⁶ atoms and molecules¹⁷ offer a wider variety of transitions that are suitable for clock operation, some of which are highly





Fig. 1 | **Experimental overview.** a, An ultrastable laser, prestabilized to an optical cavity, is used to interrogate the Yb optical lattice clock. For ZDT measurements, two ensembles (Yb-1 and Yb-2) are interrogated in an interleaved fashion, and frequency feedback to the OLO and phase feedforward to the Al⁺ clock are alternately provided by the two ensembles. A frequency comb multiplies the Yb OLO frequency up to near the Al⁺ transition frequency, and the Al⁺ OLO is phase locked to the comb. This OLO interrogates an Al⁺ ion nearly synchronously with the Yb interrogation, completing the interrogation soon after the Yb phase feedforward is applied via an AOM to correct for common-mode laser noise. The grey dashed lines represent frequency feedback and the green dashed lines represent phase feedforward. **b**, c, Pulse sequence and a possible evolution of the integrated atom–laser phase during an interrogation are shown for single Yb ensemble measurements (**b**) and ZDT measurements (**c**). The $\pi/2$ pulses in

Ramsey spectroscopy are depicted by the orange (blue) square pulses for the Yb (AI⁺) clock. The grey-shaded regions represent the Ramsey free-evolution periods. The two clocks start their interrogation at the same time, after which the relative phase between the OLO and atoms evolves for the two clocks. After the Yb clock makes a measurement of the atom–laser phase, the phase information is fed forward to the AI⁺ clock so that it can complete the interrogation on the ion with the phase corrected by the Yb clock. For ZDT measurements, the Yb clock interrogates two Yb optical lattice systems in an interleaved fashion; after each interrogation, the OLO phase is adjusted for the AI⁺ clock. The AI⁺ clock completes its interrogation after *m* cycles on the Yb clock. At the point in time indicated by the arrow with the dashed green line, the total phase correction accumulated is the sum of the *m* phase corrections measured by interrogating the Yb clock.

sensitive to the proposed effects beyond the Standard Model, including dark-matter couplings¹⁸ and fundamental symmetry violations¹⁴. Instability due to QPN can be reduced by extending the interrogation time, but for Ramsey spectroscopy, the optical local oscillator (OLO) noise restricts *T* to less than the coherence time of the laser¹⁹. For large *T*, the evolved relative phase between the atoms and laser can wander outside the range $[-\pi/2, \pi/2]$, beyond which the phase measurements become ambiguous, and it is no longer possible to lock the frequency of the OLO to the atomic transition.

This limit to the stability of independent clocks has motivated the development of several novel clock comparison techniques in which the two clocks use phase-synchronized OLOs to enable interrogation durations beyond the laser coherence time. As first proposed and demonstrated²⁰ in fountain clocks, by synchronizing the interrogations of the two clocks and using the same OLO, it is possible to suppress common-mode OLO noise, though the total interrogation time remains limited by OLO decoherence^{8,21}. Using a protocol called correlation spectroscopy²², it is possible to interrogate beyond the OLO coherence limit for differential measurements, as demonstrated in a recent lifetime-limited comparison of two Al⁺ clocks²³. Correlation spectroscopy is effective only for clocks similar in frequency, but other protocols are usable for more general comparisons. Such protocols can be realized by using one or multiple systems to prestabilize the OLO^{8,24}, by making non-destructive measurements to realize a phase lock^{25,26} or by employing dynamical decoupling²⁷. Another work⁷ proposed a protocol called differential spectroscopy in which the phase measurements from one clock are fed forward to a second clock and used to disambiguate the phase measurements of the second clock, which is operated beyond the laser coherence limit.

In this work, we demonstrate a comparison between an ytterbium (171 Yb) optical lattice clock and a single-ion aluminium (27 Al⁺) quantum-logic clock using differential spectroscopy. Figure 1a shows the experimental setup. The 267 nm Al⁺ OLO is phase locked to the 578 nm Yb OLO using an Er/Yb-doped glass femtosecond optical frequency comb. Maintaining phase coherence between the two systems via the frequency comb and active fibre noise cancellation



Fig. 2|Differential spectroscopy clock comparison results for various T_{AI} values for the single Yb ensemble case and varying the number of Yb clock interrogation cycles for the ZDT case. The data corresponding to the single Yb ensemble case (orange circles) and the ZDT case (blue squares) were obtained by driving the stretch states on the AI⁺ clock. The data for the the ZDT case (blue diamonds) were obtained by driving the Zeeman transitions in the inner manifold that are less sensitive to the magnetic field fluctuation (Methods). Also shown are the results of spectroscopy without phase feedforward corrections (grey triangles). Numerical simulations are shown for the single Yb ensemble with corrections (orange line), single Yb ensemble without corrections (grey line) and ZDT (blue line) cases for $m \in \{2, 3, 4, 5, 6, 8, 10, 12\}$ with $l\sigma$ standard deviation

at each experiment are critical for differential spectroscopy to be effective. The two clocks initiate Ramsey interrogation with synchronized $\pi/2$ pulses of 10 ms duration (Fig. 1b). Synchronizing the initial $\pi/2$ pulses ensures that the two clocks accumulate the same phase such that the information of the accumulated phase from one clock can be passed on to the other one. The evolved phase of the Al⁺ clock during the Ramsey free-evolution time is given by $\Delta \phi_{AI} = \beta \Delta \phi_{Yh}$, where $\beta = v_{Yb}/v_{Al} \approx 2.16$ is the frequency ratio and $\Delta \phi_{Yb}$ is the evolved phase of the Yb clock. The measured Yb phase is used to estimate $\Delta \phi_{Al}$, which is fed forward to correct the Al⁺ OLO phase before its final Ramsey $\pi/2$ pulse. Because $\beta > 1$, the Yb OLO coherence time is a factor of β longer than that of the Al⁺ coherence time. Assuming that Yb has enough atoms to measure the phase with a high signal-to-noise ratio and that the OLO instability is characterized by flicker frequency noise, the Al⁺ interrogation time may be extended by up to a factor of β longer than is possible without feedforward corrections from the Yb clock.

We extend the original differential spectroscopy proposal by operating the Yb clock in the zero-dead-time (ZDT) mode⁸ in which two independent atomic ensembles are interrogated using Ramsey spectroscopy in an interleaved fashion. Multiple interrogations with times $T_{\rm Yb}$ are completed on the Yb clock, with phase feedforward corrections applied to the Al⁺ clock after each one, during a single Al⁺ interrogation (Fig. 1c). Further details about the experimental setup and protocol can be found in the Methods. Using ZDT differential spectroscopy, the Al⁺ clock interrogation time $T_{\rm Al}$ may be extended yet further, potentially approaching the 20.6 s Al⁺ excited-state lifetime. error given by the shaded regions. The green dashed line represents the QPN limit of the ratio measurement instability. The panels on the right show the Ramsey fringe (atomic transition probability as a function of the relative phase between the two Ramsey pulses) of the Al⁺ spectroscopy with (orange curve for the single Yb ensemble and blue curve for the ZDT) and without (grey curve for both top and bottom) phase feedforward from the Yb clock for two different values of $T_{\rm Al}$. The grey curve (bottom right) is not a fit to the experimental data, but rather assumes that there is no contrast left by this interrogation time, as it is well beyond the coherence time of the OLO. The maximum slope points are used for feedback to the AOM, whereas the other points are interrogated once every ten cycles to gather information on the contrast of the Ramsey fringe.

The results of both single Yb ensemble and ZDT experiments are shown in Fig. 2. The single Yb ensemble experiments are carried out for various values of T_{yb} . We use $T_{Al} = T_{yb} + 50$ ms to allow time for the Yb clock to perform the second $\pi/2$ pulse, population measurement and phase feedforward. The ZDT experiments have a fixed $T_{yb} = 0.404$ s, which was chosen for safely interrogating the Yb ensembles without a fringe hop, and the number of Yb clock interrogations is incremented. For comparison, the results of conventional Ramsey spectroscopy without phase feedforward are also shown. Figure 2 (inset) shows the Ramsey phase scans of the Al⁺ clock at a specific T_{Al} value, one with feedforward corrections from the Yb clock (orange and blue curves) and one without (grey curve), which are fit to determine the contrast. The power spectral density of the measured frequency ratio noise is fit to determine the long-averaging-time asymptotic Allan deviation (Methods) (Fig. 2, bottom left). The improvement in the atom-laser phase coherence with corrections is shown by the increase in Ramsey contrast in both plots. As T_{Al} increases, the interrogation time comes to exceed the coherence limit of Al⁺OLO, and the Ramsey fringe without phase feedforward drops to zero contrast indicating that phase feedforward is required to run the Al⁺ clock at these interrogation times.

The results of numerical simulations—which model comparisons between the two clocks with realistic noise generated to match the laboratory conditions—are also plotted for the single Yb ensemble and ZDT cases (Fig. 2, solid lines). With no sources of noise, we expect the instability to follow the QPN limit (green curve, Fig. 2 (bottom)), which continues to improve until T_{AI} reaches the lifetime of the AI⁺ clock's excited state. Instead, the one-second instability reaches a



Fig. 3 | **Fractional instability measured for a 36-h-long ZDT differential spectroscopy.** Stability of a 36-h-long ZDT differential spectroscopy clock comparison taken from 5 to 6 November 2020, with m = 4 Yb clock interrogations corresponding to a single Al⁺ clock interrogation cycle for the full run (yellow circles) and an 8 h selection of the total run (blue triangles). Our previous result compared Yb and Al⁺ (orange squares) using a conventional optical clock comparison technique. The solid lines are error-weighted least-squares fits to the asymptotic region of the instability curves. The green-shaded region represents a bound on the frequency transfer instability introduced by the frequency comb.

minimum value when the interrogation time is at 1-2 s, after which it begins to rise again. Further simulation results indicate (Methods) that technical noise sources in the system, such as fibre links and local fluctuations in the magnetic field, compromise instability as T_{AI} increases. The reasonable level of agreement between simulation results and empirical data suggests that with further suppression of such sources of technical noise, it will be possible to obtain a comparison instability that approaches the lifetime limit of the AI⁺ clock.

Figure 3 (yellow circles) shows the Allan deviation of a 36-h-long continuous ZDT differential spectroscopy comparison, with a duty cycle of 68.0% and total uptime of 88.8%, using four Yb interrogations $(T_{\rm Yb} = 0.404 \, \text{s})$ for each Al⁺ interrogation $(T_{\rm Al} = 1.720 \, \text{s})$. A drifting systematic frequency shift leads to an apparent 3×10^{-18} flicker-noise floor at averaging times greater than 30,000 s for differential spectroscopy. The source of this long-term noise has not yet been identified. For these measurements, we note that neither clock was operated in a configuration with low systematic uncertainty (Methods). However, an eight-hour subset (Fig. 3, blue triangles) shows that the data average as white frequency noise over this timescale, approaching the 1×10^{-18} level. Furthermore, we anticipate that the apparent noise floor can be suppressed in future work by operating the clocks in the low-uncertainty mode. In Fig. 3, the asymptotic instability of ZDT differential spectroscopy is $(1.97 \pm 0.11) \times 10^{-16} / \sqrt{\tau}$ (blue line), which is improved by nearly an order of magnitude over our previous result of $1.3 \times 10^{-15} / \sqrt{\tau}$ using conventional techniques⁹ (red line).

For context, we plot the asymptotic instability of various interspecies comparisons (Fig. 4) versus the date on which the comparison was performed. Due to the large number of atoms participating in each interrogation, optical lattice clocks generally have lower instability; as shown in Fig. 4, the most stable lattice–lattice comparisons (yellow squares) perform with lower instability than the most stable lattice–ion (orange circles) and ion–ion (blue triangles) comparisons. Nevertheless, due to our ability to push the duration of the Ramsey interrogation of the ion clock beyond the laser coherence time, our asymptotic instability is lower than even some of the best previous interspecies lattice–lattice clock comparisons.

Differential spectroscopy improves the instability of clock comparison measurements by using a low-QPN clock to measure the laser phase noise and perform feedforward corrections to the second clock's laser. This allows the second clock to operate with a longer interrogation time, beyond the coherence time of its laser, when the frequency



Fig. 4 | **One-second instability of various interspecies optical clock comparisons plotted by their measurement date.** Comparisons between an optical lattice clock with another optical lattice clock (yellow squares), an ion clock with another ion clock (blue triangles) and an optical lattice clock with an ion clock (orange circles). Note that this is not an exhaustive list of all the previous interspecies comparisons but does include the most competitive results. Each measurement is marked with the laboratories involved in the measurement, as well as the species of participating optical clocks^{9,21,28-30}; the data point labeled 'PTB E3/E2' is from personal communication with N. Huntemann.

ratio between the two clocks is greater than unity. Furthermore, by running the first clock in the ZDT mode, the duration of interrogation of the second clock can be extended yet further, potentially approaching the excited-state lifetime limit. Though we demonstrate the technique for an interspecies comparison with a large frequency ratio, we note that ZDT differential spectroscopy can be utilized to improve other clock comparisons, even if the two clocks have the same transition frequency. This scheme can be understood as fusing the two clocks into a single, compound optical clock, capable of realizing an instability that could be below that of either system taken independently. Last, the differential spectroscopy algorithm is also applicable for a second clock based on multiple entangled atoms or ions, which would allow clock comparison measurements at the Heisenberg instability limit.

Online content

Any methods, additional references, Nature Research reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at https://doi.org/10.1038/s41567-022-01794-7.

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Letter

Methods

Experimental setup

The two ytterbium optical lattice systems make use of one-dimensional optical lattices, operated near the magic wavelength, to confine the atoms in the Lamb–Dicke regime and perform spectroscopy of the ultranarrow clock transition, namely, ${}^{1}S_{0} \rightarrow {}^{3}P_{0}$. An amplified external-cavity diode laser at 1,156 nm is frequency doubled to reach the 578 nm clock transition. Both systems operate with approximately 10,000 atoms. The systems have been described in detail elsewhere³. A previous analysis of the instability for a ZDT clock found that a one-second instability well below 1×10^{-16} was accessible for these systems⁸.

The Al⁺ optical atomic clock used in this experiment has been described previously²³. Spectroscopy is performed on the ${}^{1}S_{0} \rightarrow {}^{3}P_{0}$ clock transition of a single Al⁺ ion. Sympathetic cooling and readout are achieved by co-trapping a single ${}^{40}Ca^{+}$ ion and using the motional coupling between the two ions³¹. A fibre laser at 1,068 nm is frequency doubled twice to deliver 267 nm light to the Al⁺ ion. The acousto-optic modulator (AOM) in the path of this light is utilized for the feedback corrections from the Al⁺ ion and another for the feedforward operation in differential spectroscopy, which is discussed at length in the 'Differential spectroscopy feedforward corrections' section.

Extended Data Fig. 1 shows the optical paths surrounding the optical frequency comb in transferring the phase between the Yb and the Al⁺ clocks. Pulse outputs from the laser cavity are amplified by an Er-doped fibre amplifier from about 70 to 300 mW and subsequently sent through a highly nonlinear fibre for access to the carrier-envelope offset frequency, which requires spectral power on the two ends of an octave. We use a hybrid nonlinear fibre, comprising two stages: the first section (10 cm with dispersion of 5.6 ps km⁻¹ nm⁻¹) creates a dispersive wave around 1,000 nm and the second section (50 cm with dispersion of 2.0 ps km⁻¹ nm⁻¹) extends the spectrum to around 2,100 nm. Careful dispersion management before the highly nonlinear fibre and tuning of the input optical pulse power allows us to put enough spectral power at 1,068 and 1,156 nm for the detection of optical beats with Al⁺ and Yb OLOs, respectively. A periodically poled lithium niobate waveguide doubles light at 2,070 nm and the resultant 1,035 nm light is beat against the 1,035 nm part of the spectrum for the detection of the carrier-envelope offset frequency. The single-branch optical frequency comb design³² ensures that no out-of-loop fibre paths add instability to the comb.

The optical frequency comb is locked to the Yb clock OLO by comparing the beat between the OLO and comb light to a 10 MHz H-maser reference and feeding back to the mode-locked laser cavity length via a fast piezo-electric transducer. The actuator is glued between the semiconductor saturable absorber mirror, which is very light, and a heavy lead-filled copper mount specifically designed to suppress resonances below several hundred kilohertz³³. This affords comb noise suppression with a bandwidth of almost 200 kHz. A beatnote between the comb mode and light from the Al⁺ clock OLO is fed back to the Al⁺ clock lab to lock the OLO to the comb. To minimize instability due to the out-of-loop optical free-space paths, the light from both OLOs was combined on a dichroic mirror and then interfered with the comb light on a single beamsplitter and detected on a single photodiode. In this setup, there is only 20 cm of uncompensated optical free-space paths.

The Al⁺ clock OLO is stabilized to a high-finesse optical cavity with high-bandwidth (around 300 kHz) feedback. When running differential spectroscopy, we use the phase of the beatnote between the comb mode and Al⁺ clock OLO as the error signal for low-bandwidth (around 100 Hz) feedback to lock the cavity-stabilized OLO to the comb.

Differential spectroscopy feedforward corrections

For differential spectroscopy, the 10 ms duration of the first Ramsey $\pi/2$ pulse are synchronized in the clocks at the level of several microseconds. The synchronization is achieved by triggering the Ramsey pulse

sequence on the Al $^+$ clock with a transistor-transistor logic signal sent from the Yb clock experimental control system.

The second Ramsey $\pi/2$ pulse is applied on the Yb clock before the Al⁺ clock to allow time for the Yb clock to measure the phase wander of the shared OLO and feed it forward to the Al⁺ clock. The total interrogation time of the atoms, T_{Yb} , is set to be a fraction η of the coherence time of the OLO at the Yb transition frequency. To optimize σ_{QPN} (equation (1)), the duration of interrogation is maximized and ensuring that the relative phase between the OLO and the atoms, which is given by⁷

$$\Delta \phi_{\rm Yb} = 2\pi \int_0^{T_{\rm Yb}} [v_{\rm Yb} - f_{\rm Yb}(t)] dt = 2\pi (v_{\rm Yb} - \bar{f}_{\rm Yb}) T_{\rm Yb}, \qquad (2)$$

does not exceed the range $[-\pi/2, \pi/2]$ (the so-called invertible region) for Ramsey spectroscopy, where v_{Yb} is the Yb atomic transition frequency, f_{Yb} is the time-dependent Yb OLO frequency and \bar{f}_{Yb} is the mean frequency of the Yb OLO during clock interrogation.

After the second Ramsey $\pi/2$ pulse on the Yb clock, the ground-state and excited-state atom numbers are read out by destructive fluorescence detection using the strong ${}^{1}S_{0} \rightarrow {}^{1}P_{1}$ transition at 399 nm. The frequency of the Yb clock is locked to the centre of the resonance, but it is dithered between the half-maximum points on either side of the resonance centre, leading to an ~50% chance of excitation. Following this, the excitation ratio *r* is determined, and the estimated optical phase of the OLO is calculated as

$$\Delta \phi_{\rm Yb}^{\rm est} = \sin^{-1}(2(r - r_0)/A), \tag{3}$$

where $r_0 \approx 0.5$ and $A \approx 1$ are the empirically determined half-maximum ratio and contrast of the Ramsey fringe, respectively. The Yb OLO is frequency locked to the Yb atoms using the estimated deviation of the laser frequency $\Delta \phi_{\rm Yh}^{\rm est}/(2\pi T_{\rm Yb})$ as the error signal.

The Al⁺ OLO, which is phase locked to the Yb OLO, interrogates the Al⁺ ion for a duration of $T_{Al} = T_{Yb} + \tau_{delay}$ for a single Yb ensemble experiment and $T_{Al} \approx mT_{Yb} + \tau_{delay}$ for the ZDT experiment, where τ_{delay} is the time required for the Yb clock to make a measurement of its atom-laser phase and send the feedforward signal to the Al⁺ clock; *m* is a positive integer. The final $\pi/2$ pulse of the Yb clock, atom detection, phase calculation and phase correction are accomplished in several tens of milliseconds, but we choose to extend the free-evolution time of the Al⁺ clock by $\tau_{delay} = 50$ ms to ensure that the phase correction has been applied before the second $\pi/2$ pulse of the Al⁺ clock. For the ZDT mode, phase corrections are sent after each Yb clock interrogation. The second $\pi/2$ pulse of the Al⁺ clock is supplied 50 ms after the second $\pi/2$ pulse of the final ZDT cycle of the Yb clock.

In another work⁸, we utilized a ZDT sequence in which the $\pi/2$ pulses of the two systems overlapped with each other. Here we use a slightly modified sequence: by adding a delay between the second $\pi/2$ pulse of one of the systems and the first $\pi/2$ pulse of the other, it is possible to further decrease the time dependence of the ZDT clock's sensitivity function and thus decrease the Dick effect, too³⁴. Extended Data Fig. 2b displays the sensitivity functions of a ZDT clock with simultaneous $\pi/2$ pulses and a ZDT clock with a delay of 27.73% of the $\pi/2$ pulse time. Extended Data Fig. 2c displays the calculated Dick effect as a function of delay time between the $\pi/2$ pulses. In this work, we elect to operate our ZDT system with a delay of 2.773 ms, at which the calculated Dick effect is minimized.

The Yb clock feeds forward the accumulated atom–laser phase after the termination of each of its interrogations weighted by the ratio of the two clock frequencies, β . The phase correction is sent via a serial connection to a 10 MHz direct digital synthesizer in the Yb lab, which can be programmed with a 14 bit phase-tuning word, implying a 0.4 mrad phase resolution for the corrections. This 10 MHz synthesizer serves as the external reference for a 160 MHz synthesizer in the Al⁺ lab driving an AOM that frequency and phase shifts the Al⁺ OLO just before

it is delivered to the ion. Due to the difference in transition frequency between the clocks, the phase estimate must be multiplied by the frequency ratio β such that $\Delta \phi_{Al}^{est} = \beta \Delta \phi_{Yb}^{est}$. Because the phase correction signal is multiplied by (160 MHz)/(10 MHz) = 16, the phase correction sent to the direct digital synthesizer must be further reduced by a factor of 16, that is, $\Delta \phi_{DDS}^{DDS} = \Delta \phi_{Al}^{est}/16$.

Feeding forward the accumulated atom–laser phase after every Yb interrogation is equivalent to feeding forward the estimated total atom–laser phase accumulated during the Al⁺ clock interrogation time, $\Delta \phi_{y \text{tot}}^{\text{est}}$ For the Al⁺ clock, the relative phase between the OLO and atoms is given by

$$\Delta \phi_{\rm Al} = 2\pi (\nu_{\rm Al} - \bar{f}_{\rm Al}) T_{\rm Al} - \beta \Delta \phi_{\rm Yb, tot}^{\rm est}, \tag{4}$$

where the second term is the feedforward correction from the Yb clock, v_{Al} is the Al⁺ atomic transition frequency and \bar{f}_{Al} is the mean frequency of the Al⁺ OLO during the clock interrogation. For traditional operation of the Al⁺ clock, the atom–laser phase is simply given by the first term, and T_{Al} must be restricted such that $|2\pi(v_{Al} - \bar{f}_{Al})T_{Al}| < \pi/2$. However, for differential spectroscopy, the factor β allows the interrogation time T_{Al} to be increased by the same factor; in the case of ZDT differential spectroscopy, the constraint on T_{Al} is lifted such that excursions of the atom–laser phase far beyond the invertible region can be tolerated. This leads to a reduction in instability by $\sqrt{\beta m}$, as shown in equation (1).

After the second Ramsey $\pi/2$ pulse on the Al⁺ clock, the state of the Al⁺ ion is read out using quantum-logic spectroscopy and the atomlaser phase estimate $\Delta \phi_{Al}^{est}$ is computed. The Al⁺ clock OLO is frequency locked to the Al⁺ ion by shifting the drive frequency of the same AOM used for feedforward phase corrections, f_{AOM} , using the frequency estimate $\Delta \phi_{Al}^{est}/(2\pi T_{Al})$ as the error signal, with a feedback update rate of $1/T_{Al}$. Therefore, the measured frequency ratio of the two clocks is

$$\beta^{\text{est}} = \beta_0 + \frac{f_{\text{AOM}}}{v_{\text{Yb}}},\tag{5}$$

where β_0 is a known constant set by the mode numbers and frequencies of the comb beatnotes and the frequencies of the other AOMs that shift the OLOs of both clocks between the comb and atomic ensembles.

The raw frequency shift data from the two clocks are separately collected on each of the control computers. The Meinberg network time protocol programs loaded on the computers enable the Al⁺ clock control computer's onboard clock to synchronize to that of the Yb computer, such that the timestamps on the clock data collected on the two computers agree to within a few milliseconds. This enables us to look for noise that is correlated in both systems.

Sources of noise in differential spectroscopy

Noise of the OLO. Because the Al⁺ clock laser is phase locked to the OLO of the Yb clock, the noise characteristics of the Yb clock OLO determine the durations of both clock interrogations. We measure its noise characteristics by measuring the performance of its optical cavity reference, as well as by referencing the atoms. The former determines the spectrum of the relatively high-frequency noise, whereas the latter allows low-frequency noise to be determined. Combining the results from these two spectra, we find that the Yb clock OLO has a flicker-noise-limited fractional frequency noise of approximately 1.5×10^{-16} from 0.6 to 1,000.0 s. Below 0.6 s, the spectrum is approximately white frequency noise, and above 1,000 s, the spectrum is approximately random walk/run. The performance of the OLO supports $T_{\rm Yb} \approx 0.500$ s; however, for ZDT-mode differential spectroscopy, we use a conservative value of $T_{\rm Yb} \approx 0.404$ s.

Magnetic field noise. Along with phase noise fluctuations of the OLO, any environmental factors that can vary and induce uncertainty in the atomic transitions must be evaluated. One important source of

differential instability is uncorrelated fluctuations of the magnetic field sampled by the clocks. Each clock accounts for magnetic field fluctuations in its local environment by alternately probing the atoms on opposite Zeeman transitions: the Yb atoms are interrogated on the $m_F = 1/2 \rightarrow m_{F'} = 1/2$ or $m_F = -1/2 \rightarrow m_{F'} = -1/2$ transitions. As for Al⁺ ion, spectroscopy carried out in the single Yb ensemble cases and some of the ZDT cases employed the stretch states ($m_F = 5/2 \rightarrow m_{F'} = 5/2$ or $m_F = -5/2 \rightarrow m_{F'} = -5/2$). However, for longer ZDT cases, we opted to interrogate the Al⁺ ion on the $m_F = 3/2 \rightarrow m_{F'} = 1/2$ or $m_F = -3/2 \rightarrow m_{F'} = -1/2$ transitions. The latter is a departure from the traditional way of operating the Al⁺ clock using the stretch states that minimizes the sensitivity to magnetic field noise and extends the atomic dephasing time beyond the interrogation durations used in this work. The measured frequency difference between the opposite Zeeman transitions is used to determine the strength of the magnetic field for each system and is then fed back to the programmed difference between the interrogation frequencies used for opposite lines.

In the Yb clock, the atomic signal is used to serve the OLO laser frequency between the Zeeman sublevels. Due to the relatively $\log 1/e$ serve time constant of 44 s, we use a fluxgate magnetometer to measure the magnetic field fluctuations at shorter times. With the combination of these two datasets, we determine that the root mean square (r.m.s.) value of the noise in the Yb clock is 4×10^{-5} G.

In the Al⁺ clock, the magnetic field is actively stabilized by feeding forward fluxgate magnetometer measurements to the three orthogonal pairs of Helmholtz coils that surround the science chamber. The measurement details are discussed elsewhere²³. The r.m.s. value of the magnetic field noise in the Al⁺ clock is 5×10^{-6} G.

Fibre link noise. One source of noise that is important in differential spectroscopy is the frequency transfer uncertainty arising from imperfect phase noise cancellation of the clock light distribution among the participating laboratories. The determination of the atom–laser phase in the Yb clock is critical to the success of differential spectroscopy. However, if the frequency transfer system introduces dephasing by some $\Delta \phi_{PNC}$, then the estimated atom–laser phase $\Delta \phi_{AI}^{est} = \Delta \phi_{AI} - \Delta \phi_{PNC}$ will no longer be a good estimate of $\Delta \phi_{AI}$.

To mitigate this noise source, we use a path-length stabilization technique³⁵ for each fibre link between the Yb clock to the Al⁺ clock. At the receiving end of each fibre, a flat facet reflects a portion of the laser power back through a bidirectional AOM to the sending end. The beatnote between the reference arm and returned light is stabilized by feeding back to the drive radio-frequency of the AOM.

Additive uncertainty in the optical network is determined with a loop-back measurement. Light from the Yb and Al⁺ clock OLOs is sent over phase-stabilized links to the Er/Yb:glass frequency comb, which locks the Al⁺ clock OLO to the Yb clock OLO. Both OLOs also send light over stabilized fibre links to an independent Ti:sapphire³⁶ frequency comb to measure the instability (Extended Data Fig. 3). We measure a total network instability of 3.3×10^{-17} at 1 s, which is approximately twice the instability experienced by the path from the Yb clock to the Al⁺ clock. The optical frequency combs add negligible instability around 3×10^{-18} at 1 s, limited by uncompensated free-space optical paths³².

Other sources of noise. The Yb clock systems were operated in a similar mode to that described elsewhere³, with two main alterations. First, a relatively high Rabi frequency of $2\pi/(40 \text{ ms})$ was used, facilitating differential spectroscopy, but impacting the level of systematic effects from probe Stark shift, line pulling and AOM phase chirp. Second, some windows for the blackbody radiation shield of Yb-2 (ref. ³⁷) were not in place; we estimate that this could potentially result in drifts in the blackbody radiation shift at the 1×10^{-18} level. With these alterations, the systematic uncertainty reported earlier³ was not valid for these runs, and further investigation would be required to ensure long-term stability at that level. Our ZDT algorithm allows us to measure the fractional

frequency difference between the two atomic systems during a run, and we note that no drift was observed at the 2×10^{-18} level between Yb-1 and Yb-2 during the run reported in Fig. 3. In any case, these sources of systematic uncertainty can be reduced. Fundamentally, the differential spectroscopy scheme should be compatible with uncertainty budgets at the 10^{-18} level or below.

The systematic uncertainties of the Al⁺ clock have not been fully evaluated, but it has been built to mitigate the leading cause of uncertainty in trapped-ion clocks, which is Doppler shift due to excess micromotion¹⁰, among other improvements over the previous-generation Al⁺ clock. One of the possible sources of uncertainty in this clock is the first-order Doppler shift due to slow drift of the ion position. This can be caused by, for example, charging of the dielectric surfaces near the ion by photoelectrons generated by scattered laser light. The first-order Doppler shift was suppressed in the previous Al⁺ clock by operating with two counterpropagating clock beams: one interrogated the ion and the other was detuned by 100 kHz. The beam on resonance and the detuned beam were alternated every cycle. In this work, only one interrogation direction was used, and thus, there may be an uncompensated first-order Doppler shift. Another potential source of noise that has not yet been evaluated is a phase chirp of the AOM being used to supply the feedforward corrections to the Al⁺ clock.

Clock comparison instability limit

ZDT differential spectroscopy has the potential to extend the interrogation time of the second clock (Al⁺ in this work) to the fundamental limit set by the excited-clock-state lifetime of the atoms (20.6 s for the Al⁺ clock), providing a corresponding improvement in instability. This is due to the fact that the first clock's interrogation time is always within the coherence time of the laser, and the atom–laser phase is continuously measured and fed forward to the second clock. As the second clock's interrogation time increases, the number of ZDT interrogation cycles of the first clock for each interrogation of the second clock also increases. However, the results of our experiment in which we scan the number of Yb clock cycles do not show an improvement in instability after $T_{Al} \approx 2$ s (Fig. 2). Here we present numerical simulations of the comparisons in which we vary three different sources of noise–OLO noise, magnetic field noise and fibre link noise–revealing that all of them contribute to the comparison instability.

For the numerical simulations, OLO noise, magnetic field noise and fibre link noise are numerically generated to match the experimentally measured noise spectra. White, flicker and random-walk noise models are used to generate the OLO noise with a fractional-frequency noise floor of 1.5×10^{-16} . The white noise is below 0.6 s and random walk and random run are beyond 1,000.0 s. The Yb and Al⁺ clocks are subject to the same OLO noise with the Al⁺ clock seeing noise amplitude increased by a factor of β . The simulations treat the two Yb clocks separately such that they experience different magnetic field noise levels. The magnetic field noise is mostly flicker, and the r.m.s. value of the Yb clock is 4×10^{-5} G (with a linear Zeeman shift of 199.516 Hz G⁻¹), and the r.m.s. value of the Al⁺ clock is 5×10^{-6} G (with a linear Zeeman shift of about 280.000 Hz G⁻¹). Besides the magnetic field noise and OLO noise, the Al⁺ clock is subject to fibre link noise, which imprints additional noise on the estimated atom-laser phase. The fibre link noise is mostly flicker in nature with both phase and frequency components and adds the maximum instability of 3×10^{-17} at 1 s.

Both clocks probe the points of maximum slope on the central Ramsey fringe for the highest sensitivity, on each side of the opposite Zeeman lines, such that a total of four interrogations are required for the full knowledge of the magnetic field and OLO phase. In addition to these four interrogation frequencies, for every tenth interrogation of the Al⁺ clock, we interrogate a randomly chosen extrema (the maximum or one of the two minima on either side) of the central Ramsey fringe. This allows us to determine the Ramsey contrast in real time to evaluate how well the feedforward is working. In simulations, we generate atom–laser phase estimates made by the Yb clock in the presence of noise after each interrogation. In the ZDT case, the Yb clocks make *m* measurements of the phase, and the total phase is fed forward to the Al⁺ clock. The Al⁺ clock, subject to its own set of noise sources, makes an estimate of the atom–laser phase, ideally within the invertible region with the assistance of the feedforward signal. The simulation results are compared with the experimental data (Fig. 2).

To explore the impact of different noise sources on the clock comparison instability, we study three cases: when only the OLO noise is present, when the OLO noise is present along with the magnetic field noise, and when these two sources are present as well as the noise from the fibre link. Extended Data Fig. 4 shows the contrast in the Al⁺ clock's phase scan (top) and the fractional frequency instability (bottom) in the clock comparison for each of these three cases. The simulations incorporate the noise profiles of the OLO, fibre link and magnetic field in each system. The one-second fractional measurement instability is extracted from each clock simulation run under various noise conditions. The statistical error associated with running 25 simulations for each Ramsey interrogation time is reflected in the shaded area; however, the error associated with extracting the one-second instability is not reflected in Extended Data Fig. 4. This is responsible for the fact that the simulations curve falls below the QPN limit in Fig. 2, which is not possible.

When the only source of noise present in the system is from the OLO, the instability continues to improve as T_{AI} is increased out to several seconds, following the QPN limit. This indicates that without additional sources of noise, it would be possible to continue improving the clock comparison instability beyond 10 s. In our case, the limit on the Ramsey interrogation time-and hence the lowest achievable instability-is the excited-state lifetime of the Al⁺ clock transition, which is 20.6 s. If the lifetime of the excited state were infinite for the ion clock, the instability would be limited by the QPN limit of the Yb clock. This would be reached when the number of clock cycles on the Yb clock is such that the phase noise accumulated reaches $\pi/2$ rad, such that it is no longer contained in the invertible region of the phase space. This maximum number of cycles, m_{max} , is fundamentally determined by the QPN of the Yb systems. The maximum Yb interrogation time, $T_{\rm Yb}$, is given by the coherence time of the Yb OLO. The maximum achievable Al⁺ interrogation time is, thus, given by $m_{\rm max}T_{\rm Yb}$, in the absence of other sources of noise. Beyond this extreme limit, a fringe hop would then be unavoidable, compromising clock performance. Due to the large number of atoms in the Yb clock, many Yb clock cycles will be necessary to lead to a fringe hop if no other noise source was an issue.

When the magnetic field noise is present along with OLO noise, the contrast in the Al⁺ clock is somewhat reduced, and the instability increases slightly. The magnetic field is servoed in the Al⁺ clock system and its r.m.s. noise level is about 5×10^{-6} G, and the least magnetically sensitive transitions are used for the Ramsey interrogation. This allows the magnetic field noise to be suppressed in the clock comparison, even at a Ramsey interrogation time above 10 s. A larger source of noise in the clock comparison arises from the fibre link between the various systems. When the fibre link noise is also present along with the OLO noise and magnetic field noise, the clock comparison instability does not improve beyond 1.4×10^{-16} in fractional frequency, which is reached for T_{Al} at about 2–4 s.

It is possible to improve the various sources of noise in our system to reach the QPN limit (Extended Data Fig. 4), which continues to improve beyond $T_{AI} > 8$ s. Research is already underway to build a cryogenic optical cavity as a reference for the OLO to reduce its noise; and the Al⁺ clock could be magnetically shielded to passively reduce the impact of magnetic field noise from the environment. Improving the fibre link noise will allow the Ramsey interrogation time to increase, allowing us to achieve lower instability.

Instability data analysis

For each dataset, the instability at long averaging times is determined by fitting the power spectral density of the measured frequency noise; an example is shown in Extended Data Fig. 5 (middle left). The fit function,

$$S_{\rm f}(f) = \frac{S_{\rm w}}{1 + (f/f_{\rm c})^2},$$
 (6)

corresponds to white frequency noise of magnitude S_w that has been low-pass filtered with a corner frequency of f_c . This is physically motivated because the OLO is stabilized to the QPN-limited Yb clock and the Al⁺ clock's frequency measurement is also limited by the QPN, resulting in a white frequency noise spectrum. However, the bandwidth of frequency measurement is limited by the frequency lock of the Al⁺ clock to the OLO. Because the Al⁺ frequency lock uses a single-frequency integrator, the power spectral density of the expected measurement frequency noise is low-passed white noise. The white frequency noise fit parameter S_w is converted into the long-averaging-time asymptotic Allan deviation $\sigma(\tau) = \sigma_{1s}/\sqrt{\tau}$ using $\sigma_{1s} = \sqrt{S_w/2}/\nu_{Al}$.

Notably, the two fit parameters S_w and f_c are correlated, as shown by the non-circular contour of χ^2 in Extended Data Fig. 5 (middle right). The reduced χ^2 of the fit in this example is $\chi^2_{\nu-1} = 1.45$. The upper and lower uncertainties of the fit parameter S_w are determined as

$$\sigma_{S_{w},upper} = \sqrt{\chi_{v-1}^{2}} \times \left(\max_{\chi^{2} = \min(\chi^{2}) + 1} (S_{w}) - S_{w} \right)$$
(7)

and

$$\sigma_{S_{w},\text{lower}} = \sqrt{\chi_{\nu-1}^{2}} \times \left(S_{w} - \min_{\chi^{2} = \min(\chi^{2}) + 1} (S_{w}) \right).$$
(8)

For long datasets, this data analysis procedure gives results that are consistent with direct fits of the Allan deviation at long averaging times, which are typically reported. However, for short datasets, it is often difficult to determine what range of averaging times should be included in such a fit, and the fit results depend strongly on this subjective choice. Furthermore, the Allan deviation values at different averaging times are correlated with each other, making it difficult to determine the uncertainty of direct fits of the Allan deviation. The procedure described here avoids these problems.

Data availability

All the supporting data are available from the corresponding authors upon reasonable request.

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Author contributions

All the authors contributed to the design of the experiment, collection of data and revision of the manuscript. During the measurements, Al^+ clock operation was conducted by E.R.C., D.B.H., M.E.K., D.R.L. and J.L.V. Yb clock operation was conducted by W.F.M., Y.S.H., X.Z. and A.D.L. Comb metrology laboratory operation was conducted by T.M.F., H.L. and N.V.N. Data analysis and preparation of the manuscript were performed by M.E.K., D.R.L., W.F.M. and N.V.N.

Competing interests

The authors declare no competing interests.

Additional information

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Extended Data Fig. 1|**Frequency comb optical path.** Optical paths surrounding the optical frequency comb portion of the experiment that enables coherent transfer of phase between the Yb and Al⁺ clocks.

Letter



Time (ms)

Fractional delay of Ramsey pulse time

Extended Data Fig. 2 | **An optimized zero-dead-time clock. (a)** The timing sequence for a ZDT clock with a variable delay between the π /2-pulses. Note that the length of each step is not to scale. **(b)** Displayed is the sensitivity function for a zero-dead-time sequence in which the Ramsey pulses of the two atomic systems are precisely overlapped (red) or offset from each other by 27.73% (green). The sensitivity functions have been vertically offset from each other for visual clarity. **(c)** The optimal delay is determined by calculating the one-second Dick instability for a variable delay between the two pulses. These calculations assume

the OLO noise is flicker-frequency and at the level of 1.5×10 -16. The blue line demonstrates that the Dick instability exhibits a sharply defined minimum. We emphasize that the Dick instability reported here would be added in quadrature with other sources of instability, such as atomic detection noise and quantumprojection noise, which under current conditions would limit the total clock instability at a level at least an order of magnitude higher than the calculated Dick instability. The red and green dots represent the conditions with overlapping Ramsey pulses and optimized timing, respectively.



The Al⁺ clock OLO, which is locked to the Yb clock OLO through the Er/Yb:glass frequency comb, and the Yb clock OLO are compared with a Ti:Sapphire

frequency comb. The top figure shows the histogram of the frequency noise, and the bottom shows the Allan deviation plot.





Extended Data Fig. 4 | **Results of the simulations that vary the noise sources in the operation of the ZDT di erential spectroscopy operation.** The top panel shows the contrast in the phase scan of the Al⁺ clock, and the bottom shows the Allan deviation plot for: when only the OLO noise is present (yellow line), when

OLO and the magnetic field noise sources are present (orange line), and when OLO, magnetic field, and the fibre link noises are present (blue line). The green dashed line in the bottom panel indicates the QPN limit.



Averaging time (s)

Extended Data Fig. 5 | Example of the data analysis used to determine the long-averaging-time asymptotic Allan deviation. This data set is Ramsey spectroscopy of the Al⁺ clock without any feedforward corrections from Yb, at a interrogation time of 454 ms. The top panel shows the time series of the measured Al⁺ transition frequency relative to the Yb stabilized OLO. The middle left panel shows the corresponding power spectral density of frequency noise, which is fit to the function $S_w/(1 + (f/f_c)^2)$. The tresiduals are shown at the

bottom of this panel. The middle right panel shows χ^2 as a function of the two t parameters. The red dotted line is a contour of constant $\chi^2 = \min(\chi^2) + 1$, and the black dashed lines are the 68% confidence interval bounds for the fit parameter S_w . The bottom panel shows the Allan deviation of the frequency data (blue circles) and the long-averaging-time asymptotic Allan deviation corresponding to the S_w fit parameter (red line and shaded confidence interval).