

Compact Stereo Waveguide Display Based on a Unidirectional Polarization-Multiplexed Metagrating In-Coupler

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Abstract: Three-dimensional (3D) vision in augmented reality (AR) displays can enable highly immersive and realistic viewer experience, hence attracts much attention. Most current approaches create 3D visions by projecting stereoscopic images to different eyes using two separate projection systems, which are inevitably bulky for wearable devices. Here, we propose a compact stereo waveguide AR display system using a single piece of thin flat glass integrated with a polarization-multiplexed metagrating in-coupler and two diffractive grating out-couplers. Incident light of opposite circular polarization states carrying stereoscopic images are first steered by the metagrating coupler to opposite propagation directions in a flat glass waveguide, subsequently extracted by the diffractive

grating couplers and finally received by different eyes, forming 3D stereo vision. Experimentally we fabricated a display prototype and demonstrated independent projection of two polarization-multiplexed stereoscopic images. This work paves a novel path towards the implementation of high-performance stereo displays with compact size, light weight, and multi-color compatibility.

Keywords:

waveguide display, stereo display, augmented reality display, metasurface, unidirectional coupling

Augmented reality (AR) display can superimpose virtual images over a real-world scene and enables the user to observe both simultaneously. As it may lead to a new paradigm in many areas including navigation, education, surgery and entertainment, the research of AR display devices, namely near-to-eye see-through displays, is booming and has attracted considerable attention over the last decade. Various approaches such as freeform optical prisms,^{1,2} projection systems,^{3,4} retina scanning,⁵ reflective systems,⁶ hybrid reflective-refractive systems,⁷ and optical waveguides⁸⁻¹² have been proposed.

Among these various approaches, optical waveguide technology is considered as the most promising means toward realizing light weight and compact devices of high performance; thus, it enjoys rapid development. A transparent optical waveguide acts as an off-axis imaging system that projects images to human eye(s) without blocking the ambient scene. For AR display, three-dimensional (3D) vision is highly desirable because it can provide an immersive and realistic experience for the viewer. Although various

approaches have been proposed to realize 3D AR display,¹³⁻¹⁷ this functionality has been a challenge for optical waveguide-based approach. One common method to address the aforementioned limitation utilize holographic gratings as couplers to reconstruct 3D objects, but it suffers from low image quality and small field of view (FOV)^{18,19}. Stereoscopy provides another approach to create 3D depth perception, which arises from the given two-dimensional images representing two perspectives of the same object that both eyes naturally receive in binocular vision. Stereo waveguide display is usually realized by using two waveguides as subsystems to respectively project stereoscopic images from two images sources to different eyes, which inevitably results in bulky volume and increased difficulty for integration. In recent years, metasurfaces, which are composed of two-dimensional metallic or dielectric nanostructures of subwavelength scale have received tremendous attention. Various planar optical devices such as filters,^{20,21} lenses,²²⁻²⁵ polarizers^{26,27} and absorbers^{28,29} have been implemented by diverse reflective or transmissive metasurfaces, featuring high optical performance as well as ultracompact footprint. Apart from engineering light in free space, metasurfaces have also demonstrated the ability to manipulate guided light, primarily focusing on the near-infrared spectral range for communication applications³⁰⁻³³. Compared to conventional couplers such as prisms and gratings, metasurface couplers offer a unique feature of unidirectional in-coupling that can be controlled by the polarization state of incident light.

Here, targeting at visible light, we design a geometric-phase-based metagrating paired with two diffractive gratings on a thin fused-silica substrate as a compact platform to realize polarization-multiplexed in-coupling for stereo waveguide display. Incident circularly polarized light (CPL) illuminating the metagrating is deflected into the

underlying substrate, and satisfies the total internal reflection (TIR) condition to propagate inside this flat waveguide. The deflection angle is determined by the phase gradient imposed by the metagrating, which is opposite for CPL of opposite handedness. Therefore, incident light with opposite handedness bearing two stereoscopic images can be in-coupled along opposite directions inside the waveguide and finally out-coupled to different eyes, generating 3D vision for the viewer. As a prototype demonstration, unidirectional in-coupling with a high contrast ratio for opposite CPL incidence is achieved by the metagrating and independent projection of two stereoscopic images multiplexed by polarization is demonstrated.

Design of the Metagrating In-coupler

A schematic layout of the proposed stereo waveguide display based on unidirectional polarization-multiplexed in-coupling is shown in Figure 1. The system comprises of a micro-display, a collimator, and a glass waveguide that is integrated with a metagrating in-coupler and two surface-relief grating out-couplers. The metagrating is designed based on geometric phase, which can lead to opposite deflection directions for CPL with opposite handedness. Image bearing light in circular polarization states from the micro-display is first collimated and then deflected by the metagrating following the phase gradient direction. Deflected light towards the bottom surface of the waveguide has an angle greater than the critical angle of TIR, ensuring that the light stays confined as it propagates within the waveguide. At the end of the waveguide, the out-coupling grating diffracts the guided light, extracting it from the waveguide and projecting it onto the human eye. The periods of the in- and out-couplers are designed to be the same to guarantee no distortion of the projected images after propagation along the folded light paths inside the waveguide. When

the circular polarization of incident light is switched to the opposite state, so does the deflection as well as the in-coupling direction. Using this approach, incident light in opposite circular polarizations carrying two stereoscopic images can be received separately by the two eyes to create 3D vision.

The metagrating in-coupler consists of anisotropic Au nanobars that have the same size but different rotational orientations to produce the geometric phase gradient. They can convert the incident CPL to its cross polarization and simultaneously induce a phase shift that is twice the orientation angle of the nanobars^{34,35}. By arranging nanobars with linearly changing orientation angles, transmitted light in cross polarization can be deflected, which is commonly interpreted as anomalous refraction³⁶. For the CPL incidence with opposite polarizations, the induced geometric phase acquires opposite signs, and therefore transmitted light is deflected to opposite directions. When the phase gradient is steep enough, the deflection angle satisfies the TIR condition, thereby realizing polarization-multiplexed in-coupling. Using a cartesian coordinate system, the in-coupling condition can be expressed by equations 1 and 2:

$$n_1 \sin \theta_d \sin \varphi_d = n_0 \sin \theta_i \sin \varphi_i \quad (1)$$

$$n_1 > n_1 \sin \theta_d \cos \varphi_d = n_0 \sin \theta_i \cos \varphi_i + \frac{\lambda}{2\pi} \frac{d\phi}{dx} = n_0 \sin \theta_i \cos \varphi_i + \frac{\lambda}{T} > 1, \quad (2)$$

where λ is the wavelength of the incoming light; T is the period of the metagrating; $d\phi/dx$ denotes the phase gradient, which equals $2\pi/T$ for the designed metagrating. n_0 and n_1 are the refractive indices of air and the waveguide material, respectively; θ_i and θ_d are the incident and deflection polar angles respectively, defined in the plane of incidence, and φ_i and φ_d are the incident and deflection azimuthal angles respectively, defined along the plane of the metasurface (Figure 2). The right-hand inequality of eq. 2 decides the upper

limit of the period in order to satisfy the TIR condition, while the left-hand relation gives the lower limit to ensure the existence of deflection (anomalous refraction). According to the in-coupling condition of eq. 2, the phase gradient of the metagrating determines the deflection angle, therefore, it also determines the angular range of the incident light that can be coupled into the waveguide, namely the FOV, which is related to the size of the projected image. The horizontal and vertical FOVs are the components of the incident angle θ_i on the X-Z and Y-Z plane, respectively. They are denoted by θ_H and θ_V in the inset of Figure 2 and can be described by equations 3 and 4. Targeting operation with red light ($\lambda = 635$ nm), the period of the metagrating is optimized to be 555 nm such that a maximum diagonal FOV of $\approx 20^\circ$ ($16^\circ \theta_H \times 12^\circ \theta_V$) can be realized.

$$\theta_H = \arctan(\tan(\theta_i) \cos(\varphi_i)) \quad (3)$$

$$\theta_V = \arctan(\tan(\theta_i) \sin(\varphi_i)) \quad (4)$$

The structure of the metagrating is shown in Figure 3a. Each period contains three equally spaced Au elliptical nanobars, with orientation angles of -60° , 0° and 60° , respectively, to cover a phase shift range of 2π . The long axis of each nanobar is 160 nm and the short axis is 70 nm. The simulated wavefronts of the transmitted light for normal incidence are shown in Figures 3b-3d. Light in co-polarization state remains in the same propagation direction, but cross-polarized light is deflected with an angle of $\approx 51^\circ$ inside the substrate and undergoes TIRs at the fused-silica/air interface. The deflection direction becomes opposite when the handedness of the incident CPL light flips. For the metagrating, every three elliptic nanobars constitute one period. From the perspective of periodic diffraction, one can treat the anomalous refraction and normal refraction as the $+1st$ order and the $0th$ order diffraction, respectively, while the $-1st$ order is strongly suppressed. The in-coupling

unidirectionality γ is defined as the intensity contrast ratio between the +1st order and -1st order (T_1/T_{-1}), which ranges from ≈ 6.2 to ≈ 14.1 across the horizontal FOV, as shown by Figure 3e. Figures 3f and 3g present the light propagation path by TIRs inside a fused-silica waveguide for left circularly polarized (LCP) and right circularly polarized (RCP) incidence, respectively, clearly showing opposite deflection and unidirectional in-coupling. The thickness of the waveguide is set to 10 μm for ease of simulation.

Ray-tracing Simulation of the Waveguide System

To further verify the unidirectional coupling and the FOV achievable in a waveguide system, ray-tracing simulation is implemented. In simulation, the period of the diffractive grating out-coupler is set to 555 nm as well, with an out-coupling efficiency of 10 %. The size of the waveguide system is shown in Figure 4, which is set after taking into account the actual size that is needed for a wearable AR device. The two eye boxes are 10 mm \times 5 mm at an eye relief of 20 mm and their distance is 60 mm. The incident angle varies from -8° to 8° horizontally and from -6° to 6° vertically, in accordance with the maximum achievable FOV. Taking LCP incidence as an example, we present the normalized luminance distributions over the two eye boxes in Figure 4. The horizontally gradual decrease of normalized luminance intensity is due to the repeated out-coupling diffraction of the guided light. As shown, most of the in-coupled light propagates to the right side of the waveguide. Compared to the right eye box, the luminance on the left eye box is significantly lower with a maximum value of ≈ 0.13 , corresponding to a contrast ratio greater than 7, which agrees well with the in-coupling unidirectionality of the metagratings. The results indicate that the impact of LCP incident light on the left exit pupil is negligible, which enables independent projection of two polarization-multiplexed images to different

eyes. As the geometric phase has broadband property and light in the $0th$ order transmitting through the waveguide can preserve handedness upon transmission, this design can be expanded to use a stack of multiple layers of waveguides to display multiple colors. We demonstrate unidirectional in-coupling of light in three colors using two layers of waveguides by simulation, as shown in the Supporting Information.

Experiments and Results

For a proof-of-principle experiment, we fabricated the designed metagrating with a size of 0.7 mm (X) \times 1.4 mm (Y) on a nominally 2 mm thick fused-silica waveguide. A representative scanning electron microscope (SEM) image of the metagrating is shown in Figure 5a. To characterize the unidirectional in-coupling of the metagrating, in-coupling efficiency and unidirectional coupling ratio are measured. Circularly polarized light is incident on the metagrating and a portion of it is in-coupled into the fused-silica waveguide. The in-coupled light is extracted by using a prism and its intensity is measured, as shown in Figure 5b. When the incident angle changes across the FOV, the in-coupling efficiency is $\approx 8\%$. To measure the in-coupling unidirectionality, we flipped the handedness of incident light and observed high intensity contrast of the out-coupled light, with a ratio of ≈ 7.5 . The experimental results agree well with the simulation in Figure 3e. It is worth noting that the relatively low coupling efficiency as well as the in-coupling unidirectionality can be significantly improved by using high refractive index dielectric material for the metagrating, such as Si, to enhance the interaction between the nanostructures and incident light^{37,38}. In order to visualize the impact of handedness of incident light on the projected image, we fabricated a surface-relief diffractive grating on the waveguide, using nanoimprint lithography^{39,40}, as the out-coupler to extract the in-

coupled light. Corresponding SEM image of the imprinted grating is shown in Figure 5c. The out-coupling grating has a size of 2 cm (X) \times 1 cm (Y) and it is made of transparent UV-curable polyurethane acrylate (PUA) resin. We made an M-shaped pattern (nominal width = 400 μ m) on a photomask and illuminate red light on it as the image source. The experimental setup is shown in Figure 5d. For LCP incidence, a bright projected image “M” can be clearly seen overlaying on an ambient scene; when the incident light polarization is changed to RCP, the pattern became considerably dim and neglectable, as shown in Figures 5e and 5f. To further demonstrate the stereo display enabled by the metagrating design, we made two photomasks with two stereoscopic patterns (nominal width = 200 μ m) representing two perspective views of an octahedron, as depicted in Figure 6a. Out-coupling gratings are imprinted on both ends of the waveguide. Two beams in orthogonal linear polarization states are illuminated on the two masks to bear the image information. After collimation, the two beams are converted to LCP and RCP, respectively, by a quarter wave plate and finally imaged onto different cameras, which mimic the left and right eyes. The experimental setup is shown in Figure 6b and the experimental results are presented in Figures 6c and 6d. As can be seen, the two stereoscopic patterns can be received independently with high fidelity and negligible crosstalk, which verifies the feasibility of this design. In actual display devices, stereoscopic images in different polarizations can be provided by a micro-display combined with an electronic polarization modulator to change the polarization of emitted light along with the switching of stereoscopic images in real time, such that 3D video images can be displayed by this device.

Summary

In this paper, we propose and experimentally demonstrate a stereo waveguide display that employs a metagrating in-coupler paired with two diffractive grating out-couplers. The metagrating is designed based on geometric phase and can impose handedness-dependent phase gradient that is steep enough to satisfy the in-coupling condition. Stereoscopic images carried by incident light with opposite handedness can be coupled into the waveguide along opposite directions and delivered to different eyes, generating 3D vision for the viewer. Although the prototype only demonstrates monochromatic images, the underlying design is compatible with stacking multiple layers of waveguides for multi-color display. This metagrating for polarization-multiplexed unidirectional in-coupling can simplify the configuration of stereo waveguide displays by involving less optical elements, making the system more compact, lighter weight and easier for integration. This design could find promising applications in various mixed reality display devices as well as in integrated optics.

Methods:

The metagrating was fabricated on a nominally 500 μm thick fused-silica substrate using electron beam (e-beam) lithography followed by metal lift-off. Two ≈ 100 nm thick layers of poly-methyl methacrylate (PMMA) electron beam resist of different molecular weight (PMMA 495 kg/mol and 950 kg/mol) were consecutively spin-coated onto the fused-silica substrate, followed by thermal evaporation of a ≈ 20 nm thick Al charge-dissipation layer. A 100 keV electron beam system was used to expose the metagrating pattern, followed by Al removal with tetramethylammonium hydroxide, and PMMA development with methyl isobutyl ketone. The developed pattern in the PMMA bilayer was used to lift off an electron-beam-evaporated ≈ 52 nm thick Au layer (with ≈ 5 nm thick Ti adhesion layer).

The fused-silica substrate with metagrating was then adhered onto a nominally 1.5 mm thick flat fused-silica to constitute a ≈ 2 mm thick waveguide. The out-coupling diffractive gratings were imprinted using a Si mold. The mold's surface was treated by gas phase deposition of tridecafluorooctyltrichlorosilane for anti-sticking in advance. 5 μL polyurethane acrylate (PUA) resin was drop-cast on the fused-silica substrate and then covered by the mold. After aligning the mold to the metagrating, UV light from a spot UV curing system (365 nm, 200 W) was illuminated on the PUA resin for 3 min to fully cure it, during which slight pressure was applied on the mold for conformal contact. Thereafter, the mold was manually separated from the substrate, leaving the imprinted grating structures on it.

Supporting Information

The Supporting Information is available free of charge at <http://pubs.acs.org>.

Stacking two layers of waveguides for multi-color stereo display.

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Conflict of Interest

The authors declare no conflicts of interest.

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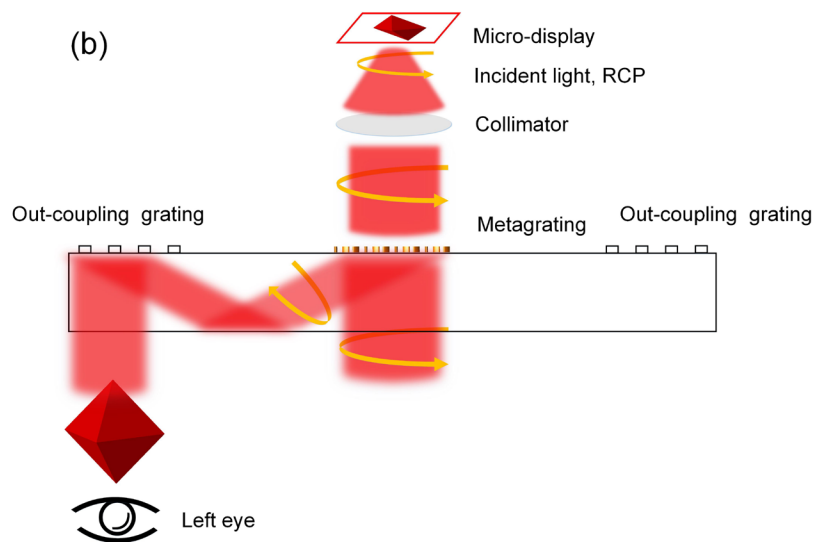
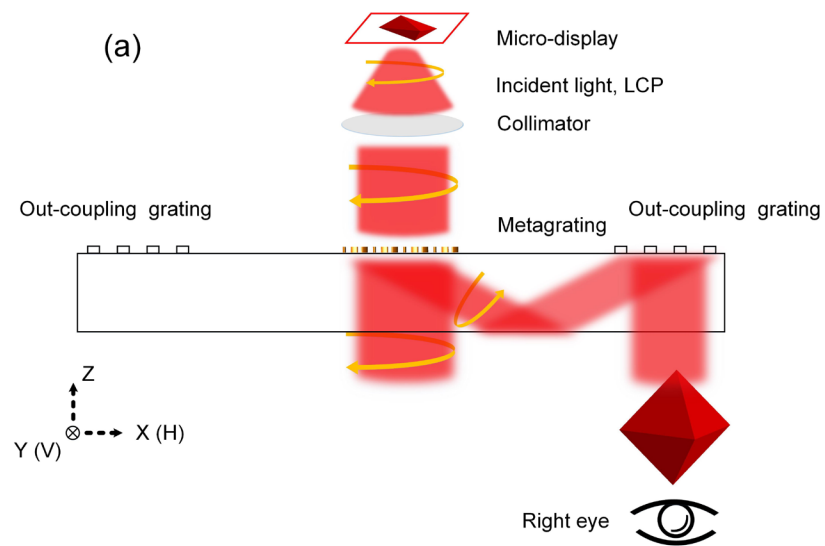


Figure 1 Schematics illustrating the stereo waveguide display based on unidirectional polarization-multiplexed in-coupling. When the handedness of incident CPL is flipped, as shown by (a) and (b), in-coupling direction becomes opposite and the stereoscopic images can be delivered to different eyes. H: horizontal direction; V: vertical direction.

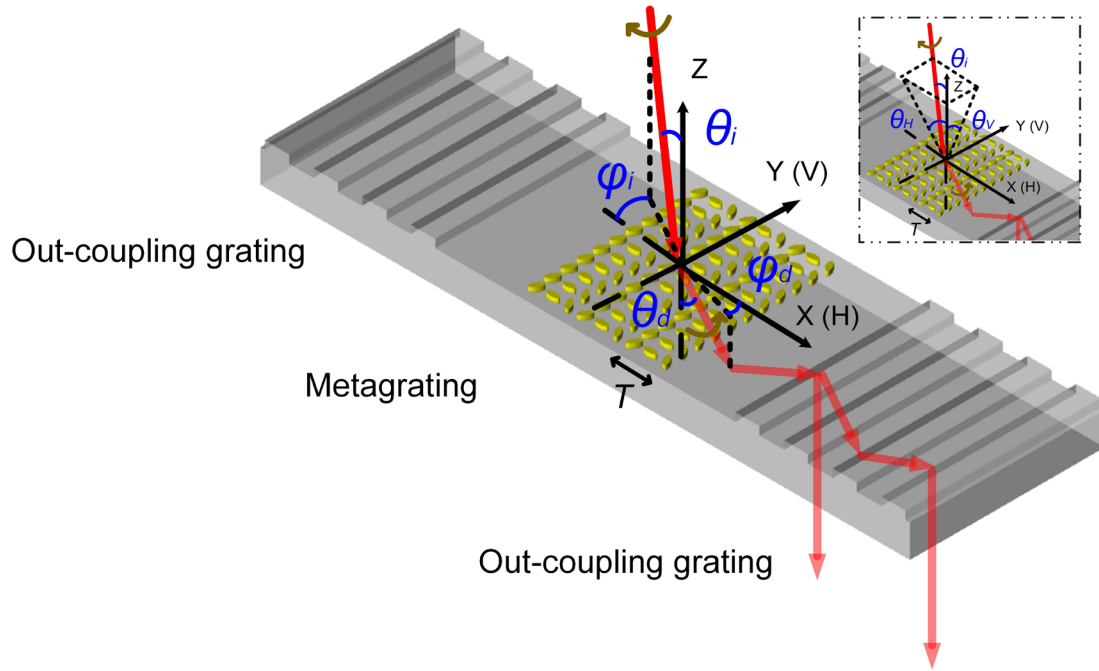
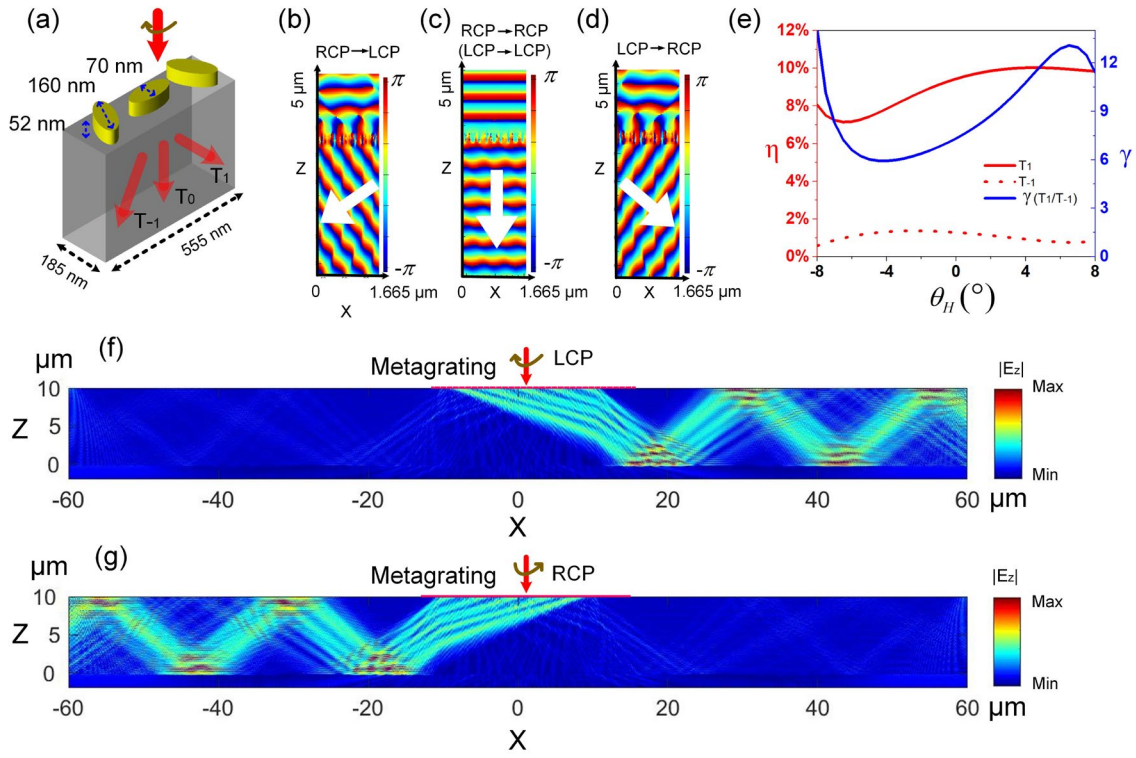


Figure 2. Schematic showing the in-coupling and out-coupling of the waveguide system. θ_H and θ_V shown in the inset are the components of the incident angle θ_i on the X-Z and Y-Z plane, respectively, representing the horizontal and vertical FOV, respectively.



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Figure 3. (a) Structure of the metagrating in a single period consisting of three Au nanobars of different orientations. (b)-(d) Simulated wavefronts of the transmitted light in cross-polarization and in co-polarization states. (b) and (d) indicate that flipping the handedness of incident light leads to opposite deflections. (e) Simulated diffraction efficiency η of the two first orders and their intensity contrast ratio (unidirectionality) γ across the horizontal FOV. (f) and (g) Distributions of $|E_z|$ inside a 10 μm thick fused-silica waveguide for LCP/RCP incidence. Coupled light propagates inside the waveguide by TIR along

negative/positive direction of the X axis, respectively. The red line indicates the metagrating.

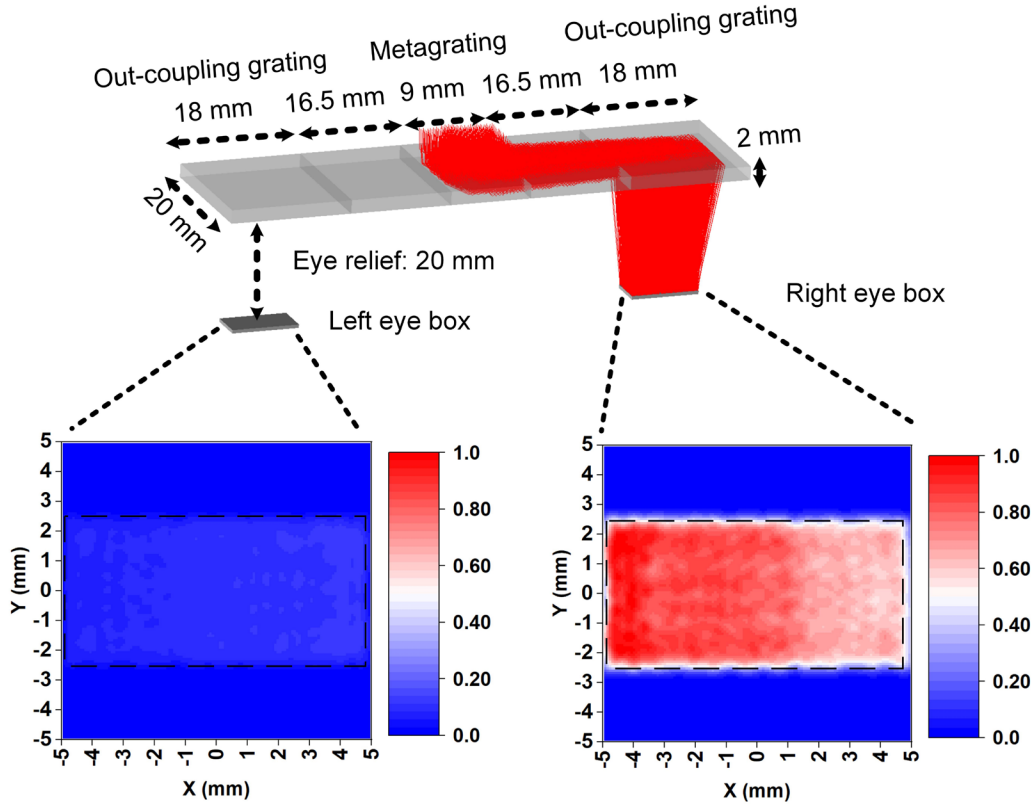


Figure 4. Ray-tracing simulation of the stereo waveguide display. The luminance distributions are normalized to the maximum value on the right eye box. The maximum of the normalized luminance on left eye box is 0.13.

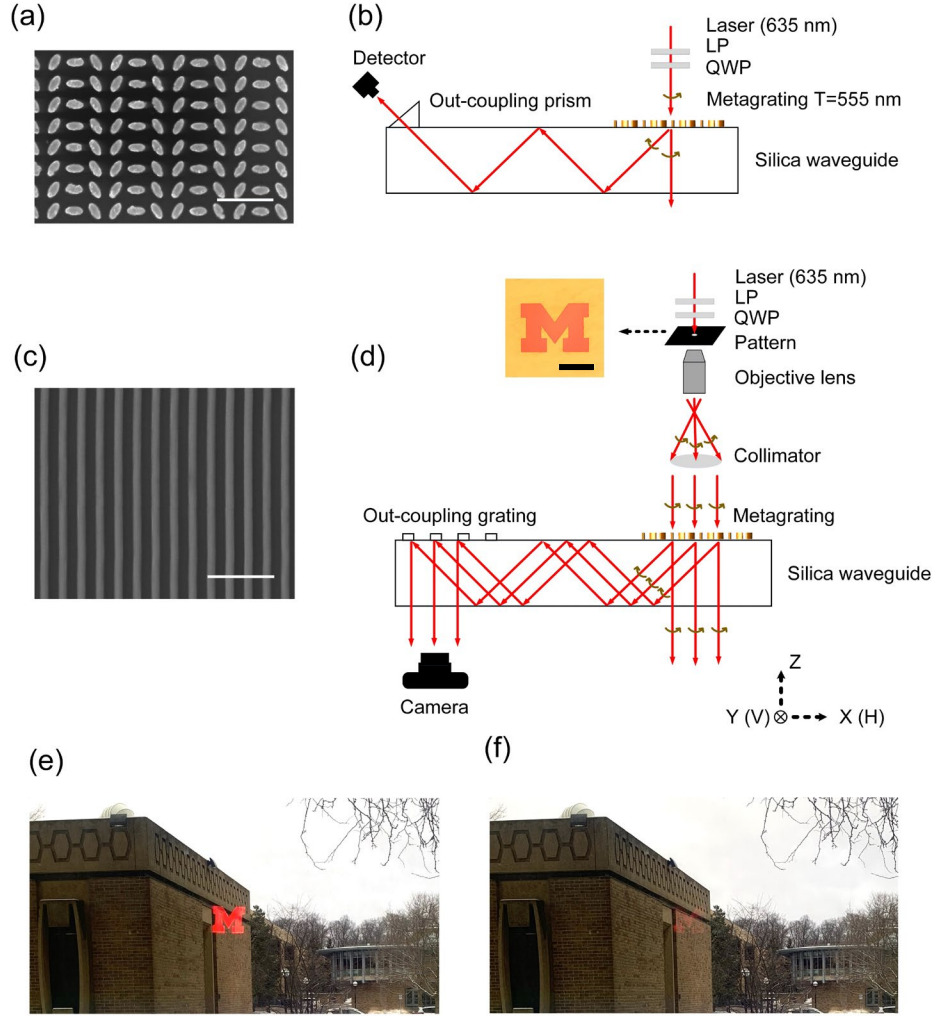


Figure 5. (a) SEM image of the metagrating (scale bar: 500 nm). (b) Experimental setup for the measurement of in-coupling efficiency and in-coupling unidirectionality. (c) SEM image of the imprinted out-coupling grating (scale bar: 2 μm). (d) Experimental setup to show the impact of handedness of incident light on the projected image. The objective lens (10 \times magnification, NA=0.25) is used to magnify the pattern. Inset is the optical micrograph of the M-shaped pattern on the photomask (scale bar: 200 μm). (e) and (f) The projected pattern overlapped on an ambient scene for RCP and LCP incidence, respectively. QWP: quarter wave plate; LP: linear polarizer.

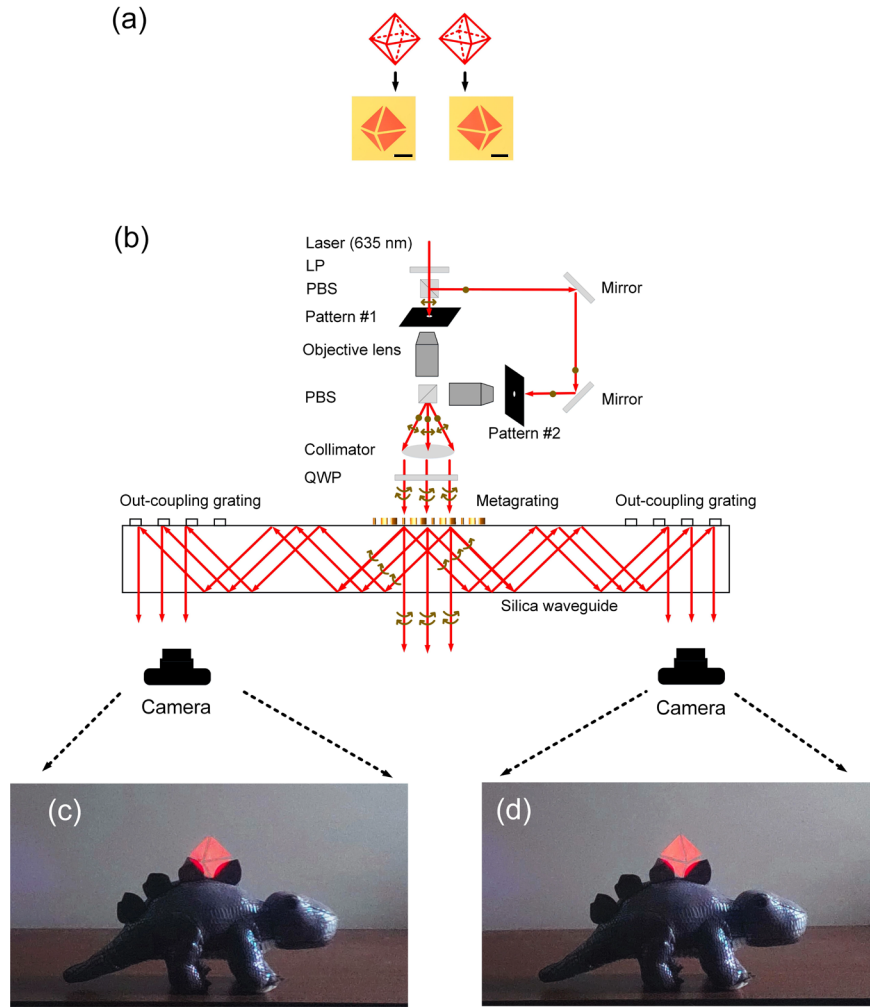


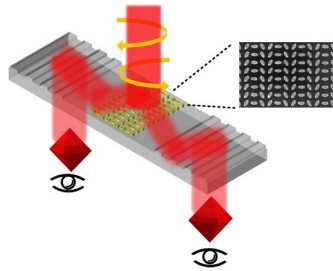
Figure 6. (a) Two stereoscopic patterns representing two perspectives of different eyes of an octahedron and the corresponding optical micrographs of the patterns on the photomasks. Scale bar: 100 μm . (b) Experimental setup to demonstrate the stereo waveguide display based on unidirectional polarization-multiplexed in-coupling enabled by the metagrating. (c) and (d) Two stereoscopic virtual images overlapped on an ambient scene are received by the two cameras on the left and the right sides, respectively. PBS: polarization beam splitter.

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Zeyang Liu, Cheng Zhang, Wenqi Zhu, Zhanhua Huang, Henri J. Lezec, Amit Agrawal, and L. Jay Guo

We demonstrated a compact stereo waveguide display consisting of a polarization-multiplexed metagrating in-coupler and two diffractive grating out-couplers on a piece of thin flat glass. Incident light of opposite handedness carrying stereoscopic images can be coupled into the flat glass by the metagrating along opposite directions and subsequently extracted by the diffractive gratings to be received by different eyes, forming 3D stereo vision.



Compact Stereo Waveguide Display Based on a Unidirectional Polarization-Multiplexed Metagrating In-Coupler

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1. Stacking two layers of waveguides for multi-color display

When circularly polarized light interacts with the metagrating, transmitted light in the 0 order can preserve the handedness of light. Because of this and also the broadband property of geometric phase, multiple waveguides can be stacked for multi-color stereo display. We design a two-layer waveguide system that is integrated with two metagratings for unidirectional in-coupling of light at three different colors. The two flat glass waveguides are nominally 2 mm thick and separated with a nominal air gap of 0.5 mm. The nominal period of the first metagrating on the top waveguide is 594 nm, designed for the in-coupling of red light ($\lambda = 680$ nm); the period of the second metagrating on the bottom waveguide

is 402 nm, designed for the in-coupling of green light ($\lambda = 510$ nm) and blue light ($\lambda = 460$ nm) that penetrate the first waveguide. Determined by the in-coupling conditions of eqs. (1) and (2) shown in the manuscript, a diagonal FOV of 20° ($16^\circ \text{ H} \times 12^\circ \text{ V}$) can be achieved for the three colors.

We choose Si as the material of the metagratings and carefully optimize the parameters of the nanopillars to reach a balance for the in-coupling efficiencies between different colors according to their in-coupling sequence. The parameters of the two metagratings and the simulated efficiencies of all useful orders are presented in Figure S1. The overall in-coupling efficiency of RGB colors is $\approx 6.9\%$, $\approx 4.2\%$ and $\approx 4.4\%$, respectively. The in-coupling unidirectionality of the two metagratings, namely the intensity contrast between ± 1 orders, is greater than 11.9 for all three red, green and blue colors across the FOV, which determines the contrast of the luminance on the two eyes. Figure S2 shows the ray-tracing simulation of the two-layer waveguide system for LCP incidence at these three colors. As designed, red light is coupled into the top waveguide; green and blue can be coupled into the bottom waveguide after transmitting through the first waveguide. The luminance distributions on the two eye boxes are normalized to the maximum value of each color, respectively, for ease of comparison. The luminance on the right eye box is one magnitude higher than that on the left eye box, which verifies the unidirectional in-coupling of light in three colors.

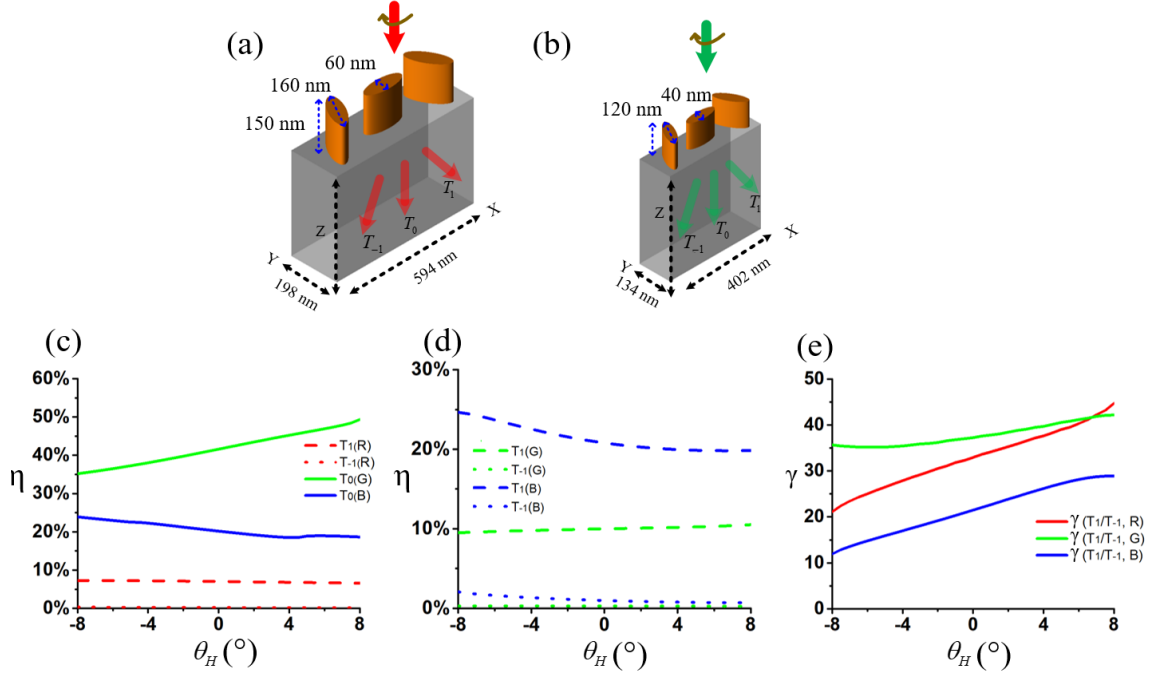


Figure S1. (a) and (b) Structures of the metagratings in one period on the first and the second waveguide, respectively. The first metagrating can couple red light into the first waveguide; the second metagrating can couple green and blue light into the second waveguide. (c) and (d) The corresponding simulated diffraction efficiencies η of useful orders of the first and the second metagrating versus horizontal FOV, respectively. (e) The intensity contrast ratio (unidirectionality) γ in the coupling of light in different colors by the two metagratings.

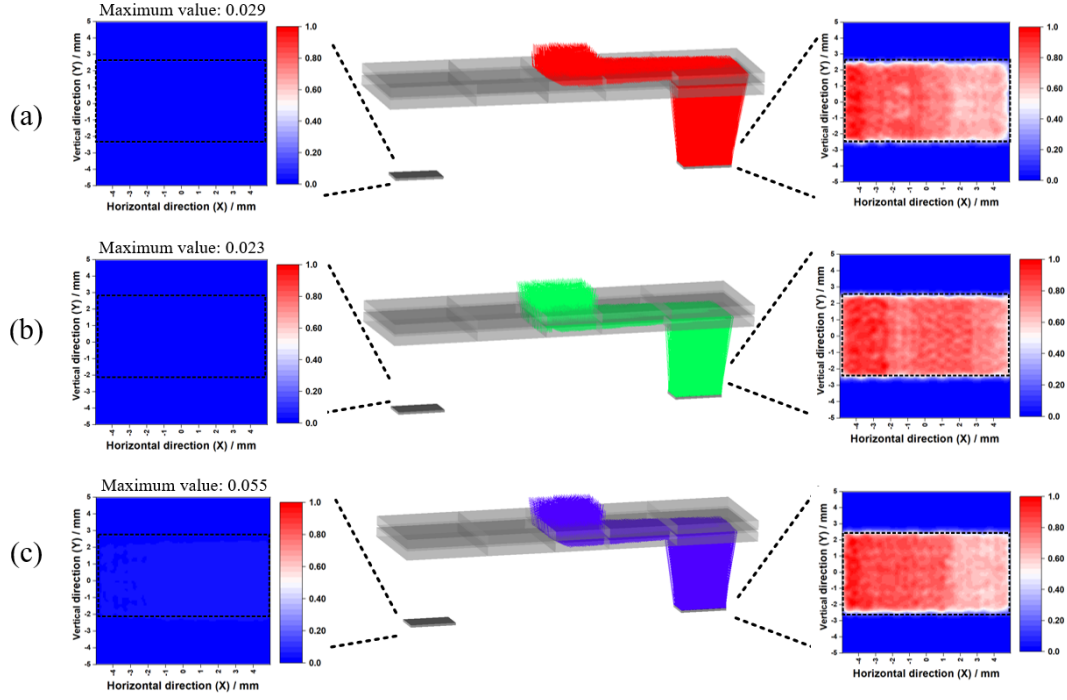


Figure S2 (a), (b) and (c) Ray-tracing results (200 rays in each case) and normalized luminance distributions on the right and the left eye box for LCP incident light in red, green and blue colors, respectively. The luminance distributions on the two eye boxes are normalized to the maximum value of each color, respectively.