From single-particle-like to interaction-mediated plasmonic resonances in graphene nanoantennas

Marvin M. Müller, a,b Miriam Kosik, c Marta Pelc, 2,3,4 Garnett W. Bryant, 5,6 Andrés Ayuela, 3,4 Carsten Rockstuhl, 1,7 and Karolina Słowik 2

1) Institute of Theoretical Solid State Physics, Karlsruhe Institute of Technology (KIT), 76131 Karlsruhe, Germany
2) Institute of Physics, Nicolaus Copernicus University in Toruń, Grudziadzka 5, 87-100 Toruń, Poland
3) Donostia International Physics Center (DIPC), Paseo Manuel Lardizabal 4, 20018 Donostia-San Sebastián, Spain
4) Centro de Física de Materiales, CFM-MPC CSIC-UPV/EHU, Paseo Manuel Lardizabal 5, 20018 Donostia-San Sebastián, Spain
5) Joint Quantum Institute, University of Maryland and National Institute of Standards and Technology, College Park, Maryland 20742, USA
6) Nanoscale Device Characterization Division, National Institute of Standards and Technology, Gaithersburg, Maryland 20899, USA
7) Institute of Nanotechnology, Karlsruhe Institute of Technology (KIT), 76021 Karlsruhe, Germany

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Plasmonic nanostructures attract tremendous attention as they confine electromagnetic fields well below the diffraction limit while simultaneously sustaining extreme local field enhancements. To fully exploit these properties, the identification and classification of resonances in such nanostructures is crucial. Recently, a novel figure of merit for resonance classification has been proposed and its applicability was demonstrated mostly to toy model systems. This novel measure, the energy-based plasmonicity index (EPI), characterizes the nature of resonances in molecular nanostructures. The EPI distinguishes between either a single-particle-like or a plasmonic nature of resonances based on the energy space coherence dynamics of the excitation. To advance the further development of this newly established measure, we present here its exemplary application to characterize the resonances of graphene nanoantennas. In particular, we focus on resonances in a doped nanoantenna. The structure is of interest, as a consideration of the electron dynamics in real space might suggest a plasmonic nature of selected resonances in the low doping limit but our analysis reveals the opposite. We find that in the undoped and moderately doped nanoantenna, the EPI classifies all emerging resonances as predominantly single-particle-like and only after doping the structure heavily, the EPI observes plasmonic response.

I. INTRODUCTION

The field of plasmonics experienced huge interest in the last two decades with a recent shift of focus towards related quantum processes and applications at the nanoscale. The possibility of confining and enhancing electromagnetic fields attracts attention not only for fundamental research reasons but also due to many potential applications in plasmonic sensing, photodetection, optical metamaterials and single photon sources. Graphene supports intrinsic tunable plasmons and, therefore, is a well-suited platform for exploring and exploiting plasmonic phenomena. Recent progress in nanostructure fabrication allows to produce graphene flakes consisting of only a few hundred atoms that support a plasmonic response at near infrared frequencies. Since a classical description based on the Drude model fails to properly predict the properties of metallic nanoantennas with a size below 10 nm, more accurate attempts to model such systems should account for fine details at atomistic scale and are mostly based on quantum mechanical methods. Among these one can find density functional theory (DFT), the tight binding (TB) model or quantum fluid dynamics.

Graphene nanoantennas support both single-particle-like resonances as well as plasmonic ones, which leads to the important question how to identify the nature of resonances in such nanostructures. This complex issue has received substantial interest in the last years and several works have been devoted to address it. The collective charge density oscillation in real space is typically considered as the smoking gun to classify a specific resonance as plasmonic in nature. However, as will be shown below, the real space analysis cannot be the sole basis for decisions on the nature of the resonance. Therefore, it continues to be a major challenge in the field of plasmonics to decide whether a specific excitation is plasmonic or not. Associated to that characterization is, of course, the question how to actually define a plasmonic excitation in nanoscaled systems. This contribution addresses these questions and aims to provide an answer.

Early studies found that in graphene nanoantennas a single extra electron from doping can switch on infrared plasmons that were absent from the structure before doping and that adding further electrons causes a significant shift in plasmon frequency. Studying how the spectral position of a resonance changes with addition of doping electrons is one of the
clues that can serve as a guide to determine its character.

Another approach to this problem relies on scaling of the electron-electron interaction strength in simulations to find how the frequency of a given resonance depends on this variation. In this approach, the excitations that show little dependence on the scaling parameter are classified as single-particle-like, while those which blue shift considerably with the increase of the Coulomb interaction strength are deemed plasmonic.

Bryant and Townsend have used real space and real-time time-dependent DFT to examine jellium spheres. They were able to distinguish two different types of behavior that the occupations of electronic states in energy basis of a given resonance can show. The first one they called "sloshing". It is a pattern of oscillatory movement between shells above and below the Fermi energy. The second they called "inversion", which is associated with a continuous transition of electrons from occupied to unoccupied states. The ratio of "sloshing" and "inversion" that is linked to a given resonance can be used as a clue to determine its nature. Other attempts to classify resonances were based on a bi-local auto-correlation function or a model in which the electrons were confined to a potential box.

Among the numerous studies conducted on this topic, a line of research focused on the construction of a universal figure of merit for resonance classification. In 2011, Yasuie et al. introduced the "collectivity index" (CI) to characterize plasmonic behavior by the quantification of how many single-particle transitions contribute to an excitation. In 2017, Fitzgerald et al. refined this approach and proposed to build an index as the product of the CI and the dipole strength of an excitation. In 2016, Bursi et al. proposed the "plasmonicity index" (PI) to characterize and quantify plasmonic behavior based on how much the induced potential in a nanostructure deviates from a neutral case. Shortly afterwards, Zhang et al. defined a dimensionless, but unnormalized metric called generalized plasmonicity index (GPI) to distinguish plasmons from single-particle-like excitations based on a similar aspect.

Both of these measures can be determined using the real space charge distribution of the structure's resonances as the only input. However, as we outline below, there exist resonances of single-particle-like nature that reveal strong dipolar character even in non-interacting systems. On the other hand, Pines and Bohm state in their pioneering work in 1952, that charge oscillations may have individual and collective components, where the latter emerge only in systems with long-range electron-electron interaction.

As a contribution to resolve this issue, recently, a new figure of merit for resonance classification in quantum mechanically described nanostructures has been proposed. The energy-based plasmonicity index (EPI) is a normalized and dimensionless measure for characterizing the nature of resonances in nanostructures. It does not rely on charge carrier oscillation patterns on the nanostructure and, hence, cannot be determined by the analysis of atomic site population dynamics. Unlike the PI and the GPI, the EPI probes the manifestation of the resonance directly in energy space. It quantifies if the existence of a given resonance can be explained predominantly by the system’s energy landscape or if electronic interaction energy, e.g. Coulomb energy, needs to be taken into account to properly determine its spectral position. The definition of the EPI is based on the coherences of the system’s density operator and the single-particle energies. While the EPI has been applied so far mostly to toy model systems, it remains an open question how this measure can be used to explain and to understand resonances sustained in structures of practical relevance. Here, we concentrate on the study of an armchair-edged graphene nanoantenna with triangular shape that is of relevance in the context of nonlinear frequency conversion processes such as higher harmonic generation.

The paper is organized as follows. In the Methods section, we shortly introduce the basics of the model and the EPI measure. Further, we present a thorough analysis of a few chosen resonances in a graphene nanoantenna doped with various numbers of electrons. To fully understand the nature of each resonance, we analyze the dependence of the absorption spectra on doping with and without Coulomb interaction taken into account, the dependence of spectral positions and absolute strengths of the nanoantenna’s resonances on Coulomb interaction scaling, their real space charge distribution, and energy space fingerprints. Then, we compute and discuss the EPI for the shown resonances. As a conclusion, we find that in the undoped and moderately doped nanoantenna, the EPI classifies all emerging resonances as predominantly single-particle-like. Only in the 20-fold heavily doped nanoantenna, the EPI observes truly plasmonic response.

II. METHOD

Our general modelling framework is based on previous work by Cox and Garcia de Abajo. We model the graphene nanostructures relying on the tight binding (TB) approach in the nearest-neighbor approximation. The coupling to an externally applied laser field is considered in the quasistatic limit and dipolar approximation. To describe the Coulomb interaction between electrons at different carbon sites and , we employ a Coulomb interaction matrix with , where values are based on Ref. 56 for the onsite-, nearest neighbor-, and next-to-nearest neighbors. For the atomic sites that are further away from each other, we use the usual power law. The parameter is used to continuously vary the Coulomb interaction from being completely turned off ( ) to being fully taken into account ( ). To describe the dynamics of the system, we first construct the ground state density matrix from the TB-Hamiltonian eigenstates of the nanoantenna according to the aufbau principle. Then, we evolve this state with a master equation that contains the influence of an external optical illumination as well as a phenomenological damping term that accounts for the dissipative processes in the nanoantenna. This method allows to find the optical response of graphene nanoantennas in terms of the time dependent polarization function of the system and the absorption spectrum related to its Fourier transform. Different resonances observed in the absorption spectrum can then be related to either single-particle-like or collective effects, and in general both
physical mechanisms contribute to a given resonance and determine its spectral position. It is the main challenge to find out which resonance is caused by which effect.

The figure of merit we will use to quantify the contribution of collective effects to a specific resonance is the energy-based plasmonic index (EPI). It is based on the stationary density matrix $\rho^\omega$ of a nanoantenna subject to continuous wave (CW) illumination at the resonance frequency $\omega$. To define the EPI, we introduce an auxiliary quantity $\tilde{\rho}^\omega$ related to $\rho^\omega$ as follows:

$$\tilde{\rho}_{ij}^\omega = \frac{|\rho_{ij}^\omega|}{|E_i - E_j| - \hbar\omega + i\epsilon}^2,$$  \hspace{1cm} (1)

where the elements $\rho_{ij}^\omega$ of the density matrix are given in the basis of TB-Hamiltonian eigenstates. The parameter $\epsilon = 0.05\,\text{eV}$ in the denominator prevents a divergence if the incident illumination frequency $\omega$ happens to be perfectly resonant to the transition frequency between the electronic energy states $E_i$ and $E_j$. Since information on electronic transitions that contribute to the density-matrix dynamics is already contained in its off-diagonal elements (coherences), we deplete the diagonal of the density matrix $\rho_{ij}^\omega \rightarrow 0$ before it enters the definition of $\tilde{\rho}$ in Eq. 1. Please note again, that in this way, no information about the occupations of energy states enters the definition of the EPI.

Having introduced $\tilde{\rho}$, we define the EPI according to

$$\text{EPI}(\omega) = 1 - \langle \tilde{\rho}^\omega, \rho^\omega \rangle \in [0,1],$$  \hspace{1cm} (2)

where we use a scalar product of two matrices $a$ and $b$ which is defined as

$$\langle a,b \rangle := \frac{\sum_{mn} |a_{mn}b_{mn}|}{(\sum_{mn} |a_{mn}|^2 \cdot \sum_{mn} |b_{mn}|^2)^{1/2}} \in [0,1].$$  \hspace{1cm} (3)

For a resonance that comprises the single-particle-like transition from state $|j\rangle$ to $|f\rangle$, the density operator’s coherence element $\rho_{jf}^\omega$ is non-zero. In the definition of $\tilde{\rho}_{jf}^\omega$, these elements get enhanced in case the excitation energy $\hbar\omega$ matches the energy difference of the single-particle states, $|E_j - E_f|$. On the other hand, if coherence elements in the density operator $\rho^\omega$ exist, which cannot be related to the excitation energy, they get suppressed in $\tilde{\rho}^\omega$. Consequently, if a resonance is predominantly composed of single-particle-like transitions, we find $\tilde{\rho}^\omega \approx k \cdot \rho^\omega$ with a constant $k$, furthermore $\langle \tilde{\rho}^\omega, \rho^\omega \rangle \approx 1$, and therefore $\text{EPI}(\omega) \approx 0$, which renders the resonance single-particle-like. On the other hand, if a resonance is comprised predominantly by coherences that cannot be associated with the excitation energy (which is the case in plasmonic resonances), we find $\tilde{\rho}^\omega \approx 0$, because most of the coherence elements in $\rho^\omega$ get suppressed, furthermore $\langle \tilde{\rho}^\omega, \rho^\omega \rangle \approx 0$, and therefore $\text{EPI}(\omega) \approx 1$. With that we get an explicit normalized measure of whether a resonance is single-particle-like or plasmonic. More details concerning the EPI, especially graphical illustrations of the density operator coherence elements for the single-particle-like and plasmonic resonances, and a thorough analysis of the measure, as well as a complete description of the used methodology, can be found in literature\(^1\).

III. RESONANCE ANALYSIS

In this section, we examine the absorption spectrum of a triangular armchair-edged graphene nanoantenna consisting of $N = 270$ atoms. The eigenenergies of the non-interacting system that are located near the Fermi energy of an undoped flake $E_F = 0\,\text{eV}$ are shown in Fig. 1a. We label the eigenstates corresponding to different energy levels with Greek letters. Note...
that some of these might be degenerate, e.g. in Fig. 1a the letter $\alpha$ denotes the 133rd and 134th eigenstates.

In the absorption spectrum of the considered nanostructure, one can identify a few resonances that correspond to single-particle-like transitions. This can be seen particularly well in Fig. 1b, where the Coulomb interaction and, therefore, collective interaction-mediated processes are turned off. Some prominent resonances are present, e.g. at 1.12 eV (associated with the $\alpha \rightarrow \alpha'$ transition), at 2 eV ($\delta \rightarrow \beta'$ transition) and at 2.2 eV ($\delta \rightarrow \delta'$ transition). Moreover, after doping the system with one electron, which populates the $\alpha'$ state and enables transitions from it, three new resonances in the absorption spectrum appear in the energy range between 0.2 eV and 0.5 eV. These clearly correspond to the $\alpha \rightarrow \alpha'$ transitions. Moreover, after doping with four additional electrons, since the $\alpha'$ states are fully occupied and cannot serve as acceptors for any transition any more.

When the Coulomb interaction is taken into account (Fig. 1c), the character of some resonances is modified. In particular, some excitations blue shift with increasing number of doping electrons. If they appear only when the interaction between a collection of electrons is allowed, we expect them to originate from electron-electron interaction. We will denote the fundamental mode as $P_1$ and the higher-order mode as $P_2$ (Fig. 1c). Apart from these resonances, we find resonances of a different type. They are mostly of a single-particle character, but are dressed (superscript $d$) by interaction energy, as we argue below. These can still be attributed to a transition between a single pair of eigenstates, e.g. the resonance denoted as $E_{\alpha \rightarrow \alpha'}^d$ in Fig. 1c. While plasmonic resonances are in general known to blue shift with increasing charge carrier density, this specific example of a dressed single-particle-like resonance appears to red shift as additional electrons are introduced into the system. Interestingly, another example of a dressed resonance, the one associated with the $\alpha \rightarrow \delta'$ transition, behaves differently and blue shifts. From this observation and from the similar charge carrier distribution of these two resonances in real space (see Fig. 4 later in the manuscript), we conclude that the shifting behavior of a resonance as a function of charge carrier density cannot be used to unambiguously determine the nature of said resonance.

For a closer inspection, we employ the scaling approach and smoothly scale the Coulomb interaction strength by a parameter $\lambda \in [0,1]$. A look at how the absorption spectrum changes with $\lambda$ shows that in the undoped structure, there is a continuous transition from the $E_{\alpha \rightarrow \alpha}$ resonance at 1.12 eV for $\lambda = 0$ to the dressed $E_{\alpha \rightarrow \alpha'}^d$ resonance at 1.4 eV for $\lambda = 1$ (Fig. 2a). Therefore, we can argue that the $E_{\alpha \rightarrow \alpha'}^d$ resonance in Fig. 1c exists also without Coulomb interaction and that it is dominated by the single-particle component, hence it is not predominantly plasmonic. Interestingly, the same resonance in the case of the two-fold doped nanostructure ($d = 2$) behaves similarly (Fig. 2b) which suggests it is also more of a single-particle-like nature. A qualitative difference appears in the scaling of the most prominent resonances in the absorption spectra in the case of 10 or 20 doping electrons (Figs. 2c and d). A close look at the absolute strength of these resonances highlights the difference between the undoped/two-fold doped and the 10/20-fold doped cases even more (Fig. 3). While the first pair of resonances ($d = 0, 2$) decreases in strength with increasing value of Coulomb interaction, the latter two behave differently. In the structure with strongest doping ($d = 20$) the relation is exactly opposite and the resonance becomes stronger with growing Coulomb interaction. The resonance in the 10-fold doped structure is an intermediate case that grows with $\lambda$ to a certain point, then decreases. From this, we deduce that there is a qualitative difference between the resonance $P_1$ in the 20-fold doped nanoantenna and the resonance $E_{\alpha \rightarrow \alpha'}^d$ in the two-fold doped structure.

A. Real Space Dynamics

Another important feature of a resonance is its real space dynamics. We compare the resonances in a two-fold doped and in a 20-fold doped nanoantenna. In Fig. 4, the results for a structure with 2 doping electrons are shown. The real
space distribution of the induced charge at resonances corresponding to the $\alpha' \rightarrow \delta'$ (at 0.55 eV for $\lambda = 0$ and 0.72 eV for $\lambda = 1$) and $\alpha \rightarrow \alpha'$ (at 1.12 eV for $\lambda = 0$ and 1.36 eV for $\lambda = 1$) transitions shows dipolar character (Figs. 4a, b, d, and e). This dipolar character can cause some of the real space based plasmonicity metrics to qualify these resonances as plasmonic. The GPI, for instance, exhibits peaks both for the $E_{\alpha' \rightarrow \delta'}$ resonance around 0.72 eV and the $E_{\alpha \rightarrow \alpha'}$ resonance around 1.4 eV of strengths 3 and 5.5, respectively, for the very same structure in the two-fold doped case. Thus, in the sense of the GPI, they are both classified plasmonic.

The EPI, however, yields results of 0.05 for the resonance at 0.55 eV and 0.02 for the resonance at 1.12 eV when Coulomb interaction is turned off and gives only slightly higher values of 0.13 and 0.23 for the respective resonances when the Coulomb interaction is included, e.g., for the $E_{\alpha' \rightarrow \delta'}$ and $E_{\alpha \rightarrow \alpha'}$ resonances. Consequently, they are both classified predominantly single-particle-like. For comparison, in Fig. 4c and Fig. 4f we present real space induced charge patterns for the 2.98 eV and 3.06 eV resonances, which are typical single-particle-like excitations (which barely change their spectral position both with doping and with Coulomb interaction scaling). The distributions of induced charge for the resonances $P_1$ and $P_2$ in the same nanoantenna doped with 20 electrons also show regular patterns (see Fig. 5). These resonances, however, exhibit much higher EPIs of 0.49 and 0.78, respectively, which is in accordance with the qualitative discussion of Fig. 3. The EPI takes a comparably low value for the $P_1$ resonance because a prominent single-particle-like transition is located at the same spectral position that also contributes to the excitation. From Fig. 4 we conclude, that the presence of electron-electron interaction is apparently not a necessary prerequisite for long-range structured (e.g. dipolar) charge oscillation in real space. Since the existence of plasmons, however, is linked to long-range electron-electron interaction energy\(^4\), we prefer to define a plasmon at the nanoscale not by charge occupation characteristics in real space, but rather by coherence considerations in energy space. From the charge occupation patterns in real space only, one can hardly tell apart bare single-particle-like resonances (Fig. 4b) from dressed single-particle-like resonances (Fig. 4e) and plasmonic resonances (Fig. 5a).

B. Energy Space Dynamics

Finally, to get a systematic picture of the population dynamics in the nanoantenna under consideration, we examine the energy space dynamics as well. In Fig. 6 we depict the difference of the occupation of the eigenstates located near the Fermi energy with respect to the initial state of the system as a function of time. We show the last five optical cycles of the simulation period both for non-interacting ($\lambda = 0$) and for interacting ($\lambda = 1$) electrons. Without the Coulomb interaction, one can recognize pairs or groups of states among which charge transfer appears. When the Coulomb interaction is taken into account, the oscillatory movement of occupation emerges on top. This "sloshing" effect appears both in the two-fold and 20-fold doped nanoantenna, but it is more pronounced in the latter one.

The close relation between the subfigures in Fig. 6 corresponding to the case of non-interacting electrons (left) and interacting electrons (right) reveals that the investigated resonances share a significant component of single-particle-like transitions. Population transfer between the pairs of states that contribute to a transition in the non-interacting case, is present also in the interacting case. On top of that, the sloshing-type (Figs. 6b and d) or even the inversion-type (Figs. 6c and f) population dynamics in the interacting case may engage additional states, building up the complex collective interaction-mediated response. The EPI is a measure of such collective influence and naturally its larger values correspond to larger differences between the dynamics in the case of non-interacting and interacting electrons.
FIG. 6. Population difference $\rho_{ij}(t) - \rho_{ij}^0$ of the energy states of the triangular 270-atom graphene nanoantenna doped with 2 electrons (upper row, subfigures (a), (b), and (c)) and 20 electrons (lower row, subfigures (d), (e), and (f)) under CW illumination for the last five optical cycles of the simulation period with respect to the ground state $\rho_{ij}^0$. The illumination frequencies coincide with those in Figs 4 and 5 and represent the (a) $\alpha' \rightarrow \delta'$, (b) $\alpha \rightarrow \alpha'$, (c) $\hbar \omega \approx 3$ eV, (d) $P_1$, (e) $P_2$, and (f) $\hbar \omega \approx 3$ eV modes. The left panel in each subfigure shows results for non-interacting electrons ($\lambda = 0$), whereas the right panel shows data for interacting electrons ($\lambda = 1$).

C. The EPI in the Classical Limit

In Ref. 57, the transition between the classical and quantum regimes in graphene nanotriangle plasmonics has been reported in detail. Classically, the intra-band dynamics of conduction band electrons in graphene can be described in the local Drude model by an ac surface conductivity $\sigma(\omega) \propto E_F/(\omega + i/\tau)$, where $E_F$ denotes the Fermi energy and $\tau$ is an inelastic relaxation time. From that, one can derive that the resonance frequency of the fundamental plasmonic mode scales as $\omega_0 \propto \sqrt{E_F/L}$, where $L$ is a characteristic length of the nanoantenna. In the quantum mechanical structures at hand in this paper, we identify the Fermi energy $E_F$ with the energy of the HOMO and $L$ with the triangle sidelength. In Fig. 7, we show the EPIs of the lowest-energy dipolar mode for graphene triangles with various sidelenaths, but constant Fermi energy $E_F \approx 0.75$ eV. For a triangle with sidelength $L \approx 5(6,7)$ nm, this translates to 8 (12,16) doping electrons. We can observe that the EPI of the lowest-energy dipolar mode is increasing for larger flake sizes and, therefore, the more plasmonic the resonance gets. For small flakes, this low-energy dipolar mode is intrinsically still associated to a single-particle transition (see also Fig. 4). For larger flakes, in the classical limit (EPI $\rightarrow 1$), the energy level diagram becomes continuous and single-particle transitions cannot occur any more.

IV. CONCLUSIONS AND SUMMARY

We have inspected selected resonances in a triangular graphene nanoantenna to distinguish those of predominantly single-particle-like from those of collective character. Based on the fact, that the resonances corresponding to the transitions $\alpha \rightarrow \alpha'$ and $\alpha' \rightarrow \delta'$ are clearly visible in the spectrum of an undoped/two-fold doped structure when the Coulomb interaction is turned off, we claim that they are predominantly of a single-particle-like nature. Even though their real space charge distributions show dipolar patterns, the EPI does not classify these resonances as plasmonic, like the GPI, for instance, does. This classification is supported by the fact,
that the real space charge distribution pattern is also dipolar for non-interacting electrons. Moreover, said resonances exhibit a qualitatively different dependence on the Coulomb scaling parameter $\lambda$, than the resonances in 10-/20-fold doped structures which appear to be plasmonic. Their energy patterns show a stronger “sloshing” behavior in the strongly doped structure as compared to a weak presence of this effect in the two-fold doped nanoantenna. This behavior arises due to Coulomb interactions among electrons, whose influence on their dynamics is significantly stronger in the case of collective plasmonic resonances. We want to emphasize that there is no inconsistency when the GPI and EPI classify certain resonances differently, but simply another definition of a plasmon at the nanoscale. The GPI relies on the Coulomb energy of a given charge distribution associated to an excitation; the EPI relies on the impact of long-range electron-electron interaction on the spectral position of a given resonance. In classical macroscopic system, these two characteristics go hand in hand, but not necessarily in nanostructures.

The EPI takes a low value for $\alpha \rightarrow \alpha'$ and $\alpha' \rightarrow \delta'$ resonances and significantly higher values for the $P_1$ and $P_2$ resonances, which is in agreement with the predictions that those pairs of resonances are of different nature. This is a qualitative difference beyond analyzing the real space induced charge patterns that requires a careful look at both the absorption spectra of the nanostructure and the coherence dynamics in energy basis.

These conclusions ultimately raise the question, whether one can find plasmons in the sense of the EPI, i.e., originating from long-range electron-electron interactions, in weakly or moderately doped nanoantennas at all. Our research rather suggests that in these structures, resonances are predominately single-particle-like and only modestly dressed by interaction effects. To obtain truly plasmonic resonances in the sense of the EPI, which in the first place emerge due to long-range electron-electron interaction, one needs heavy doping.

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DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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