Bidirectional switching assisted by interlayer exchange coupling in asymmetric magnetic tunnel junctions

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We study the combined effects of spin transfer torque, voltage modulation of interlayer exchange coupling and magnetic anisotropy on the switching behavior of perpendicular magnetic tunnel junctions (p-MTJs). In asymmetric p-MTJs, a linear-in-voltage dependence of interlayer exchange coupling enables the effective perpendicular anisotropy barrier to be lowered for both voltage polarities. This mechanism is shown to reduce the critical switching current and effective activation energy.

Finally, we analyze the possibility of having switching via interlayer exchange coupling only.

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Magnetic tunnel junctions (MTJs) that can be switched bidirectionally by electrical means are highly desirable for low power consumption applications[1]. Current-induced magnetization reversal is one of the most promising and reliable technologies available for achieving bidirectional switching in MTJs[2–5].

Current-induced switching relies on spin transfer torque (STT), where the interaction between current-carrying spins which are misaligned with the magnetization leads to magnetic dynamics and reversal[4]. In addition to STT, a charge current modifies the interlayer exchange coupling (IEC) between fixed and free layers via an additional field-like torque[5–7]. Though frequently called “field-like spin transfer torque component”, in this work we refer to this torque component as interlayer exchange torque[6]. Denoting the free (pinned) magnetic layer orientation by \( \mathbf{m} \) (\( \mathbf{m}_p \)) [See inset Fig. 1(a)], the total current-induced torque density is

\[ \mathbf{N} = T_{IEC} \mathbf{m} \times \mathbf{m}_p + T_{STT} \mathbf{m} \times (\mathbf{m} \times \mathbf{m}_p). \] (1)

Unlike in spin valves where the IEC torque is negligible, it has been demonstrated that \( T_{IEC} \) is comparable to \( T_{STT} \) in MgO-based MTJs, considerably affecting the magnetization dynamics of the free layer[8–10]. However, while the importance of \( T_{STT} \) for magnetization switching is well understood, the contribution of \( T_{IEC} \) is often omitted in many analyses and poorly explored.

For perpendicular MTJs (p-MTJs), the critical switching current \( J_c \) is directly proportional to the total effective perpendicular anisotropy \( K_{eff}[11, 12] \). Such proportionality reflects the fundamental problem encountered in memory technology, where one seeks to improve \( K_{eff} \) for better retention of information while reducing the critical switching current \( J_c \) for low-power consumption[12]. Particularly, the voltage control of magnetic anisotropy (VCMA) is currently being quoted as one of the most promising methods to circumvent this problem, as it provides a mechanism to reduce the anisotropy barrier \( K_{eff}V \), where \( V \) is the volume of the free layer, only when a voltage is applied across the MTJ, enabling one to reduce \( J_c \) momentarily while maintaining a sizeable \( K_{eff} \) at zero applied voltage[12–15]. However, while it can reduce the critical switching current for a given applied voltage by reducing \( K_{eff} \), it tends to increase \( K_{eff} \) for the opposite voltage polarity. The ability to overcome the anisotropy barrier bidirectionally while decreasing the critical current density is highly desirable, and remains a long-standing goal in the search for low power consumption spintronics.

In this work, we show that \( T_{IEC} \) can assist STT switching by effectively reducing the anisotropy barrier for both voltage polarities in asymmetric p-MTJs. We demonstrate that \( T_{IEC} \) directly competes with the total effective intrinsic uniaxial anisotropy quantified by \( K_{eff} \), enabling one to reduce the critical switching current bidirectionally by tuning the degree of asymmetry of the p-MTJ. Our model includes the combined effects of STT, VCMA and IEC effects on p-MTJs, which are all known to be present in this kind of system[12, 16].

The total torque acting on the magnetization vector of the free layer is decomposed into different contributions, as given by the Landau-Lifshitz-Gilbert (LLG) equation[17]

\[ \frac{dm}{dt} = -\gamma m \times H_{eff} + \alpha m \times \frac{dm}{dt} + \frac{\gamma}{\mu_0 M_s \xi_{tree}} N, \] (2)

where \( \mathbf{m} = M/M_S \), with \( M \) being the magnetization of the free layer with saturation \( M_S \), \( \gamma \) is the gyromagnetic ratio, \( \alpha \) is the intrinsic damping parameter, \( \mu_0 \) is the vacuum permeability and \( \xi_{tree} \) is the thickness of the free layer. The effective field is \( H_{eff} = (2K_{eff}(V)m_z/\mu_0 M_S)z \) with \( z \) being the axis perpendicular to the free layer plane and \( m_z \) being the \( z \) component of \( \mathbf{m} \). The total effective anisotropy coefficient is given by \( K_{eff}(V) = K_{eff}(0) + \xi V \) with \( K_{eff}(0) = K_i/\xi_{tree} - \mu_0 M_S^2/2 \) being the effective perpendicular magnetic anisotropy at zero voltage with interfacial anisotropy \( K_i \). The VCMA coefficient is \( \xi \) and \( V \) the applied voltage across the p-MTJ. We assume
order in $V$. Our convention for the voltage is that $V > 0$ leads to an electron flow from the fixed layer to the free layer. For symmetric p-MTJs, $T_{\text{IEC}}$ is an even function of applied voltage, i.e., the spatial top-bottom symmetry requires that $C_1 = 0$ and $C_2 \neq 0$\cite{19}. In this case, one can solve Eq. (3) analytically for $V_c$ to find

$$V_c = \frac{2\alpha t_{\text{free}}}{\beta_{\text{STT}}} K_{\text{eff}}(0)m_z,$$  \hspace{1cm} (4)

where we have assumed $\xi = 0$, i.e., no VCMA effect, and neglected terms of order $\alpha^2$. Interestingly, Eq. (4) shows that $V_c$ does not depend on $C_2$ in this limit. Hence, this result is consistent with the fact that $T_{\text{IEC}}$ has little or no influence on the magnetization switching in conventional symmetric p-MTJs.

The situation for asymmetric p-MTJs is different. In this case, theoretical\cite{7, 20} and experimental\cite{21} analysis have shown that $C_1 \neq 0$, giving a sizable linear voltage-dependent contribution to $T_{\text{IEC}}$. In this situation, $T_{\text{IEC}}$ acts like a torque due to an effective field with sign determined by $V$ and direction aligned with the magnetization of the fixed layer. For a given applied voltage $V$, this results in an unidirectional anisotropy, to be contrasted with the intrinsic uniaxial magnetic anisotropy. We explore the consequences of this symmetry breaking induced contribution by assuming, for simplicity, $\xi = 0$ and $C_2 = 0$. Equation (3) can then be easily solved:

$$V_c = \frac{2\alpha t_{\text{free}}}{\beta_{\text{STT}}} K_{\text{eff}}(0)m_z (1 + \alpha C_1/\beta_{\text{STT}})^{-1},$$  \hspace{1cm} (5)

where $V_c$ is reduced by a factor of $1 + \alpha C_1/\beta_{\text{STT}}$. This simple analysis shows the relevance of $T_{\text{IEC}}$ in reducing the critical switching current. A comparison between experiments from Refs. \cite{8, 21} indicates that $C_1 = 0$ and $C_1 \approx 30$ kA/m for symmetric and asymmetric CoFeB/MgO/CoFeB MTJs, respectively. These results show the possibility of tuning $V_c$ via $C_1$.

The above analysis, albeit qualitative, demonstrates the possibility of reducing critical switching voltage when $T_{\text{IEC}}$ exhibits strong asymmetric dependence on voltage, i.e., $C_1 \gg 0$. According to Eq. (5), the sign of $C_1/\beta_{\text{STT}}$ must be positive in order to decrease the $V_c$. While $\beta_{\text{STT}}$ is usually positive, it was experimentally observed that one can tune the sign and magnitude of $C_1$ by controlling the relative composition between fixed and free magnetic layers\cite{21}. In the following section, we first evaluate the voltage modulation of both $T_{\text{STT}}$ and $T_{\text{IEC}}$ within a single orbital quantum transport model and explore the dependence of the critical current density with p-MTJ asymmetry.

Non-equilibrium torques. In the absence of spin-orbit coupling\cite{22}, the torque exerted on the magnetization of the $i$-th atomic plane of the free layer is related to the spin current flux into that plane as $\mathbf{T}_i = -\nabla \cdot \mathbf{Q}_i = \mathbf{Q}_{i-1,i} - \mathbf{Q}_{i+1,i}$ where $\mathbf{Q}_{i,j}$ is the spin-current density between atomic planes $i$ and $j$. The total torque exerted on the semi-infinite magnetic lead reads $\mathbf{T} = \sum_i \mathbf{T}_i = $
where $\mathbf{m}_p = z$ direction for the fixed layer, the $T_{\text{STT}}$ and $T_{\text{IEC}}$ components are obtained by extracting the $\mathbf{m} \times (\mathbf{m} \times \mathbf{m}_p)$ and $\mathbf{m} \times \mathbf{m}_p$ components, respectively, of the interface spin-current $Q_{\text{OX/FM}}$.[7, 19, 20]

We employ the single-orbital tight-binding model and express the spin-current density as[7, 19, 20]

$$Q_{ij} = \frac{1}{4\pi} \int_{\Omega_B} \frac{d^2k}{2\pi^2} \int dE \text{Tr}_\sigma \left((H_{ij} - H_{ji})\hat{G}^\dagger_{ij}\hat{G}^\dagger_{ij}\right)(\sigma \rangle,$$

where $\hat{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$ is the vector of Pauli matrices, $H_{ij}$ is hopping matrix between sites $i$ and $j$, $G_{ij}^\dagger$ is the lesser Green’s function of the whole coupled system and the $k_0$ integration is performed over the 2D in-plane Brillouin zone $\Omega_B$. This model provides an accurate description of the voltage dependence of the non-equilibrium torques in systems such as in Fe/MgO/Fe MTJs[24–27].

In experiments, asymmetry in the ferromagnetic contacts can be introduced by the use of different metals[23], or by considering ferromagnets with different compositions such as in Co$_{20}$Fe$_{40}$B$_{20}$/MgO/Co$_{20}$Fe$_{40}$B$_{20}$ MTJs[21]. In this work, we introduce asymmetry in the ferromagnets by adjusting their band fillings. The symmetry breaking is controlled by the asymmetry parameter $\delta = \epsilon_R^{(4)} - \epsilon_L^{(4)}$, where $\epsilon_R^{(4)}$ refers to the spin-up (down) band filling of the left (right) magnetic lead, as shown by the band diagram in Fig. 1(a). The exchange splitting inside the ferromagnets are kept constant and the same, i.e., $\Delta_L = \Delta_R$.

The voltage dependence of $T_{\text{STT}}$ and $T_{\text{IEC}}$ for different asymmetries ($\delta = 0.0$ eV (solid black), $\delta = 0.6$ eV (dashed red) and $\delta = 1.8$ eV (dot-dashed olive)) are shown in Fig. 1(b) and (c), respectively. The angular dependencies of both torque components are $\sin(\theta)$.

Hence, it suffices to show only their amplitudes. The results of Fig. 1(b) show that $T_{\text{STT}}$ presents an approximately linear behavior for small applied voltages, i.e., $T_{\text{STT}} \approx \beta_{\text{STT}}V$, with a slope that decreases as an increasing function of the asymmetry parameter $\delta$. In particular, for the most asymmetric case considered ($\delta = 1.8$ eV), the voltage behavior of $T_{\text{STT}}$ at negative $V$ deviates from linear and one can potentially achieve $T_{\text{STT}}$ sign reversal under applied voltages for one of the polarities[19].

Figure. 1(c) indicates that $T_{\text{IEC}}$ is quadratic in $V$ for symmetric p-MTJs, i.e., $T_{\text{IEC}} \approx C_2 V^2$ with $C_2 < 0$, as theoretically predicted and observed experimentally [4, 7, 8, 20]. As one increases the asymmetry via $\delta$, the voltage modulation of $T_{\text{IEC}}$ is enhanced while an additional linear-in-voltage contribution develops, i.e., $T_{\text{IEC}} \approx C_1 V + O(V^2)$. We also emphasize that the ratio $C_1/\beta_{\text{STT}}$ is positive if one choose $\delta > 0$.

**Critical current density.** The critical current density $J_c$ is computed by computing the current-voltage relation using Landauer’s formula and non-equilibrium Green’s function. This relation enables the previously computed voltage-dependent $T_{\text{IEC}}$ and $T_{\text{STT}}$ to be converted to their corresponding current-dependent. Figure 2(a) shows $J_c$ as a function of the asymmetry parameter $\delta$ for P to AP (red circles) and AP to P (blue triangles) switching with $K_1 \approx 1.3 \text{ mJ/m}^2$, and VCMA coefficient $\xi = 20 \text{ kJ/V m}^3$. The result clearly shows that $J_c$ decreases with asymmetry, which can be interpreted as follows: The presence of $T_{\text{IEC}}$ in asymmetric p-MTJs reduces $K_{\text{eff}}$ for both voltage polarities, as qualitatively described by Eq. (5). Therefore, the effective energy barrier between P and AP configurations decreases and less current is necessary for magnetization reversal.

The symmetry breaking also has important consequences for thermally activated switching. Following Ref. [28], we have derived expressions for the effective activation energy in the presence of $T_{\text{IEC}}$: 

$$E^\text{eff}_c = E_{\text{anis}} \left(1 - \frac{T_{\text{STT}}}{T_{\text{STT}}^c}\right) \left(1 - m_z \frac{T_{\text{IEC}}}{2m_{\text{eff}}}K_{\text{eff}}\right),$$

from which one can extract the switching time $\tau^{-1} = f_0 \exp(-E^\text{eff}_c/k_BT)$, with $f_0$ being an attempt frequency. The anisotropy energy barrier $E_{\text{anis}}(V) = K_{\text{eff}}(V)/V$ quantifies the thermal stability factor $\Delta = E_{\text{anis}}(0)/k_BT$. Figure 2(b) shows the voltage dependence of the normalized effective energy barrier $E^\text{eff}_c/E_{\text{anis}}$ for P to AP ($V > 0$) and AP to P ($V < 0$) switching considering several different asymmetry parameters $\delta$. In this plot we use the voltage dependence of non-equilibrium torques from the quantum transport model. As one can see, the activation energy drops faster with $V$ for asymmetric p-MTJs, allowing for higher switching probabilities at a given temperature $T$.

**Switching by voltage control of IEC.** So far, we have shown that in asymmetric p-MTJ, $T_{\text{IEC}}$ can assist STT switching by effectively reducing the anisotropy barrier
for both voltage polarities. Anisotropy and voltage dependent IEC torques can be written as derivatives of an effective energy, given by:

\[ E(\theta) = K_{\text{eff}} \sin(\theta)^2 + (T_{\text{IEC}}/t_{\text{free}}) \cos(\theta), \quad (8) \]

where \( \theta \) is the angle between \( \mathbf{m} \) and \( \mathbf{m}_p \). Stable equilibrium points are found at energy minima, where the total field-like torque vanishes.

Figures 3(a) and (b) show the energy landscape for negative and positive current densities of \( J = 5 \times 10^7 \, \text{A/cm}^2 \) for different degrees of asymmetries \( \delta \). We define \( \theta \) as the angle between the magnetization of free and pinned layers such that parallel and anti-parallel configuration, highlighted as P and AP, are found in \( \theta = 0 \) and \( \theta = \pi \), respectively. We have also plotted the energy at zero applied voltage in black solid lines for comparison purposes. One sees that \( K_{\text{eff}} \) alone gives rise to two metastable equilibrium configurations with P (\( \theta = 0 \)) or AP (\( \theta = \pi \)) alignment, emphasizing the axial nature of perpendicular anisotropy.

Figure 3(a) shows the angular dependence of the total energy for different asymmetries \( \delta \) at applied \( V < 0 \). For the symmetric case (\( \delta = 0 \) eV), a negative bias voltage gives rise to a negative \( T_{\text{IEC}} \) [See Fig. 1(c)] while decreasing \( K_{\text{eff}} \). The associated energy landscape for this case is shown as a dashed blue curve in Fig. 3(a). One sees that the stability of the P (AP) configuration is enhanced (suppressed) due to the unidirectional nature of the IEC torque. The dotted olive curve in Fig. 3(a) shows the angular dependence of energy for the same current density considering an asymmetric p-MTJ with \( \delta = 0.6 \) eV. In this case, the previously metastable AP configuration is now a maximum, indicating a current-induced instability and subsequent switching from \( \theta = \pi \) to \( \theta = 0 \).

The dash-dotted red curve shows that the effect is even more pronounced if one further increases the asymmetry to \( \delta = 1.8 \) eV.

For \( V > 0 \), \( K_{\text{eff}} \) now increases with \( V \). For symmetric p-MTJs, \( T_{\text{IEC}} \) is an even function of the bias and, therefore, remains negative with positive applied voltage [See Fig. 1(c)]. The resulting energy landscape is represented by the dashed blue curve in Fig. 3(b), where one observes an even greater stability in the P configuration, increasing the difficulty to switch from P to AP. In asymmetric p-MTJs, however, \( T_{\text{IEC}} \) changes sign under reversal of the voltage polarity. Such behavior results in the curves corresponding to \( \delta \neq 0 \) eV in Fig. 3(b). In these cases, the P (AP) configuration tends to become more unstable (stable) as one increases the asymmetry, favoring P to AP switching. In particular, the case \( \delta = 1.8 \) eV shows that one can completely destabilize the P configuration, showing pure IEC bidirectional bipolar switching.

**Conclusion.** We have studied the simultaneous impact of VCMA, IEC and STT for p-MTJs. We demonstrated that for asymmetric devices, linearly varying \( T_{\text{IEC}} \) plays an important role in STT switching by renormalizing the effective anisotropy barrier. Such effect leads to reduced critical switching current for magnetization reversal, and can even lead to switching based on IEC alone.

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Supplementary Information: Bidirectional switching assisted by interlayer exchange coupling in asymmetric magnetic tunnel junctions

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SINGLE ORBITAL TIGHT-BINDING AND NON-EQUILIBRIUM GREEN’S FUNCTIONS

We employ the single-orbital simple cubic tight-binding model in combination with the non-equilibrium Green’s functions (NEGF) formalism as discussed in Refs. [1, 2]. The spin-current density reads

\[
Q_{i,j} = \frac{1}{4\pi} \int_{\Omega_B} \frac{d^2k}{(2\pi)^2} \int dE \text{Tr}_\sigma \{ [H_{ji} G^{\sigma'}_{ij} - H_{ij} G^{\sigma}\sigma'] \delta \},
\]

where \( \delta = (\sigma_x, \sigma_y, \sigma_z) \) is a vector of Pauli matrices, \( H_{ij} \) is hopping matrix between sites \( i \) and \( j \), \( G^{\sigma'}_{ij} \) is the Lesser Green function of the whole coupled system and the \( \Omega_B \) integration is performed over the 2D in-plane Brillouin zone \( \Omega_B \).

The band diagram is sketched in Fig. 1. The hopping matrices and the lesser Green’s functions for a given pair of indexes \( i, j \) are both \( 2 \times 2 \) matrices in spin space with elements \( H_{ij}^{\sigma\sigma'} \) and \( G^{\sigma\sigma'}_{ij} \), respectively, with \( \sigma, \sigma' = \uparrow, \downarrow \). In this picture, the general block Hamiltonian element between sites \( i \) and \( j \) assuming a spin quantization axis along \( z' \) rotated by \( \theta \) in relation to the \( z \) axis is \( H_{ij}^{\sigma \theta} = \mathcal{R}^{\sigma \theta}(\theta) H_{ij} \mathcal{R}^{\sigma \theta}(\theta) \), where \( \mathcal{R}^{\sigma \theta}(\theta) \) is the rotation operator and \( H_{ij} = \text{diag}[H_{ij}^{\uparrow \uparrow}, H_{ij}^{\downarrow \downarrow}] \) is the block Hamiltonian element in spin space with spin quantization along the \( z \) direction.

The spin dependent block Hamiltonian elements for each region is given in terms of spin-dependent onsite energy \( \epsilon_\sigma \) and nearest-neighbor hopping parameter \( t_\sigma \) as \( H_{ij}^{\sigma \theta} = \epsilon_\sigma \delta_{ij} + t_\sigma (\delta_{i,j+1} + \delta_{i,j-1}) \) (\( \sigma = \uparrow, \downarrow \)), with Kronecker delta \( \delta_{ij} \). For the calculations presented in this letter, we assume \( \epsilon_\uparrow = E_F = 3.0 \) eV, \( \epsilon_\downarrow = E_F = 5.6 \) eV for the right lead (free layer) with spin quantization along the \( z \) direction and \( \epsilon_\uparrow = E_F = 3.0 + \delta \) eV, \( \epsilon_\downarrow = E_F = 5.6 + \delta \) eV for the left lead (fixed layer) with spin quantization axis along the \( z \) direction, where the Fermi level is fixed at \( E_F = 0 \) eV and the parameter \( \delta \) controls the asymmetry between the magnetic leads [see Fig. 1]. Additionally, the tunnel barrier is assumed to be composed of \( N = 2 \) atomic planes with onsite energies \( \epsilon_\uparrow = \epsilon_\downarrow = 9.0 \) eV and the hopping parameters assume the values \( t_\uparrow = t_\downarrow = -1.0 \) eV in all regions. The particular choice of parameters provides a good estimate of the right order of magnitude of spin torques, exchange coupling and tunneling magneto resistance (TMR) of Fe/MgO/Fe MTJs [3–5].

The Lesser Green’s function appearing in the spin-current density, Eq. (1), is determined by solving the Keldysh equation \( G^< = G^< \Sigma^< G^> \), where \( G^>(=) \) is the retarded (advanced) Green’s function and the non-equilibrium self-energy matrix is \( \Sigma^< = i f_L \Gamma_L + i f_R \Gamma_R \) with the Fermi-Dirac distribution of left (L) and right (R) reservoirs at chemical potentials \( \mu_{L(R)} \) given by \( f_{L(R)} = [\exp(\beta(E - \mu_{L(R)}))] + 1 \)^{-1}, being \( \beta = 1/k_B T \) where \( k_B \) is the Boltzmann constant and the temperature is assumed to be \( T = 300 \) K in all results. The broadening functions \( \Gamma_{L(R)} = i (\Sigma^r_{L(R)} - \Sigma^a_{L(R)}) \) are defined in terms of the self-energies \( \Sigma^r_{L(R)} = H_{S,L(R)} g_{L(R)} \mathcal{H}_{L(R)}, \mathcal{S} \), where \( g_{L(R)} \) is the retarded (advanced) surface Green’s function of the left (right) lead. Additionally, \( H_{S,L(R)} \) connects the scattering region to the left (right) magnetic leads. Finally, the retarded Green’s function for the scattering region, with Hamiltonian \( H_S \), is \( G^r = (E - H_S - \Sigma_L - \Sigma_R + i\eta)^{-1} \) with \( \eta \to 0^+ \) while the advanced Green function is \( G^a = (G^r)^\dagger \). When the system is driven out of equilibrium under an applied voltage \( \mu_L - \mu_R = eV \) we assume that the potential drops linearly inside the oxide layer.

**LANDAU-LIFSHITZ-GILBERT EQUATION**

The Landau-Lifshitz-Gilbert (LLG) equation reads

\[
\frac{dm}{dt} = -\gamma m \times H_{\text{eff}} + \alpha m \times \frac{dm}{dt} + \frac{\gamma}{\mu_0 M_{\text{St,free}}} N,
\]

(2)
with $N = T_{IEC} \mathbf{m} \times \mathbf{m}_p + T_{STT} \mathbf{m} \times (\mathbf{m} \times \mathbf{m}_p)$, where $\mathbf{m}$ ($\mathbf{m}_p$) is the unit vector along the magnetization of the free (pinned) layer. Here, $T_{IEC}$ and $T_{STT}$ are the interlayer exchange coupling (IEC) and spin transfer torque (STT) components of the non-equilibrium torque. We introduce the dimensionless time unit $\tau = \gamma M_S t$, where $\gamma = 2.4 \times 10^5$ m/(A·s) is the gyromagnetic ratio and $M_S = 1270$ kA/m [6] is the saturation magnetization. Since the length of the magnetization vector of the free layer is unchanged, we can rewrite the equation in spherical coordinates with $\mathbf{m} = \sin \theta \cos \phi \hat{x} + \sin \theta \sin \phi \hat{y} + \cos \theta \hat{z}$, with Cartesian coordinate unit vectors $\hat{x}$, $\hat{y}$ and $\hat{z}$. The result is

\[ \frac{d\theta}{d\tau} + \alpha \sin \theta \frac{d\phi}{d\tau} = h_{\theta}^o + \tau_{DL} \sin \theta, \]

\[ \frac{d\theta}{d\tau} - \alpha \frac{d\phi}{d\tau} = -(h_{\phi}^o + \tau_{FL} \sin \theta), \]

where $\alpha = 0.2$ [7] is the damping, $\tau_{DL} (FL) = T_{STT} (IEC)/t_{free}\mu_0 M_S^2$ and $h_{\phi}^o (\phi)$ is the polar (azimuth) component of the dimensionless effective field $h_{\phi} = H_{\phi}/M_S$. We convert Eqs. (3) into the Landau-Lifshitz form

\[ (1 + \alpha^2) \frac{d\theta}{d\tau} = (h_{\theta}^o + \tau_{DL} \sin \theta) + \alpha (h_{\phi}^o + \tau_{FL} \sin \theta), \]

\[ (1 + \alpha^2) \sin \theta \frac{d\phi}{d\tau} = -(h_{\phi}^o + \tau_{FL} \sin \theta) + \alpha (h_{\theta}^o + \tau_{DL} \sin \theta), \]

and solve it for $m_x = \sin \theta \cos \phi$, $m_y = \sin \theta \sin \phi$ and $m_z = \cos \theta$ with $T_{STT}$ and $T_{IEC}$ obtained from the NEGF calculations.

**Critical switching current analysis**

For a perpendicularly magnetized magnetic tunnel junctions (MTJ) with total effective perpendicular anisotropy coefficient $K_{eff}$, the dimensionless effective field, $h_{\phi} = H_{\phi}/M_S$, reads $h_{\phi} = h_{\phi}^o + h_{\phi}^o \hat{\phi}$ where

\[ h_{\phi}^o = \frac{2K_{eff}}{\mu_0 M_S^2} \cos^2 \theta, \]

\[ h_{\theta}^o = -\frac{2K_{eff}}{\mu_0 M_S^2} \sin \theta \cos \theta, \]

and $h_{\phi}^o = 0$. Equations (4) assume the form

\[ (1 + \alpha^2) \frac{d\theta}{d\tau} = (\tau_{DL} + \alpha \tau_{FL}) - 2\alpha \frac{K_{eff}}{\mu_0 M_S^2} \cos \theta \sin \theta, \]

\[ (1 + \alpha^2) \sin \theta \frac{d\phi}{d\tau} = (\tau_{DL} - \tau_{FL}) + 2\frac{K_{eff}}{\mu_0 M_S^2} \cos \theta, \]

The switching dynamics is described by the first equation, which gives the rate of change of $\theta$, the polar angle, as a function of time. If the magnetization is initially pointing along the positive $z$ direction, $\theta \approx 0$, switching will take place if all torques conspire to give $d\theta/d\tau > 0$. This condition is equivalent to $(\tau_{DL} + \alpha \tau_{FL}) > 2\alpha \frac{K_{eff}}{\mu_0 M_S^2}$, enabling us to extract the minimum STT magnitude for achieving switching: $T_{STT} = \alpha (2K_{eff}/\mu_0 M_S^2 - \tau_{FL})$ or

\[ T_{STT} = 2\alpha t_{free} \left( K_{eff} - \frac{T_{IEC}}{2t_{free}} \right). \]

**FIG. 1:** (Color online) Band diagram for the Magnetic Tunnel Junctions. The asymmetry is controlled by the parameter $\delta = \epsilon_{L}^{u} - \epsilon_{R}^{u}$, where $\epsilon_{L}^{u}$ refers to the spin-up (down) parameter controlling the band filling of the left (right) magnetic lead. We assume $N = 2$ atomic planes in the oxide layer and the magnetic leads are semi-infinite.
This result shows that the IEC torque directly reduces the critical STT by reducing the effective anisotropy barrier $K_{\text{eff}}$ by $T_{\text{IEC}}/2t_{\text{free}}$ if $T_{\text{IEC}} > 0$, as in the case of the asymmetric MTJ under positive applied bias. Equation (7) is the condition to determine the critical current for switching. For AP to P switching, the condition is $d\theta/dt < 0$, giving $T_{\text{STT}}^c = -2\alpha t_{\text{free}}(K_{\text{eff}} + T_{\text{IEC}}/2t_{\text{free}})$. Both expressions are unified by defining writing $T_{\text{STT}}^c = 2\alpha t_{\text{free}}(K_{\text{eff}}m_z - T_{\text{IEC}}/2t_{\text{free}})$, where $m_z = \pm$ is the z component of the unit magnetization vector in the P (+) or AP (−) configuration.

We proceed by analyzing the critical applied voltage, $V_c$, necessary to equate both sides of the equation, taking into account the non-equilibrium torques obtained from the NEGF simulations and the assumed voltage dependence of the effective anisotropy coefficient. From the critical voltage $V_c$, one can then determine the critical current density $J_c$ from the NEGF IV curves. The figure in the main text show the result of this analysis for different MTJ asymmetries δ.

Equation (7) can also be derived by following Ref. [8]. The critical switching current for a perpendicular MTJ derived from Eq. 2 considering only $\mathcal{N} = T_{\text{STT}}m \times (m \times m_p)$ is given by

$$J_c = \frac{2e}{h} \alpha \frac{\mu_0 M_s}{q} H_{\text{eff}},$$

where $H_{\text{eff}} = |H_{\text{eff}}|$. We now consider the more general situation where $\mathcal{N} = T_{\text{IEC}}m \times m_p + T_{\text{STT}}m \times (m \times m_p)$. The fixed layer is also magnetized out-of-plane $m_p = z$ and $H_{\text{eff}} = (2K_{\text{eff}}/\mu_0 M_s)m_z z$. This enable us to rewrite the LLG equation as

$$\frac{dm}{dt} = -\gamma m \times B_{\text{eff}} + \alpha m \times \frac{dm}{dt} + \frac{\gamma}{\mu_0 M_s t_{\text{free}}} T_{\text{STT}}m \times (m \times m_p),$$

where we defined

$$B_{\text{eff}} = \frac{2K_{\text{eff}}}{\mu_0 M_s} m_z - \frac{T_{\text{IEC}}}{\mu_0 M_s t_{\text{free}}}. \quad (10)$$

Equation (7) has exactly the same form as the one considered by Sun[8] with a different effective field $B_{\text{eff}}$. The critical switching current is therefore modified by the presence of $T_{\text{IEC}}$ as

$$J_c = \frac{2e}{h} \alpha \frac{\mu_0 M_s}{q} B_{\text{eff}} = \frac{4e}{h} \frac{\alpha}{q} (t_{\text{free}} K_{\text{eff}} m_z - \frac{T_{\text{IEC}}}{2}). \quad (11)$$

Therefore, the critical switching current-density directly depends on the IEC torque. In particular, in asymmetric MTJs the $T_{\text{IEC}}$ is positive for positive applied voltages, directly reducing $J_c$ by subtracting an extra factor of $T_{\text{IEC}}/2t_{\text{free}}$ from $K_{\text{eff}}$ in the parallel configuration, i.e., $m_z = 1$. The same picture hold for a negative applied voltage in the antiparallel configuration ($m_z = -1$).

Equations (7) and (11) are shown to be equivalent by writing the critical STT efficiency as $\eta_c = (2e/h)T_{\text{STT}}^c/J_c$.

**Effective activation energy**

The effective activation energy is modified by the presence of STT by a multiplicative factor of $(1 - T_{\text{STT}}/T_{\text{STT}}^c)$, where $T_{\text{STT}}$ is the critical STT magnitude for switching[9]. Therefore, the STT gives rise to an effective energy barrier between parallel and antiparallel configurations given by

$$E^b = K_{\text{eff}} \mathcal{V} \left(1 - \frac{T_{\text{STT}}}{T_{\text{STT}}^c}\right), \quad (12)$$

where $K_{\text{eff}} \mathcal{V}$ is the energy barrier due to perpendicular anisotropy only, where $\mathcal{V}$ is the volume of the free layer. The thermal stability factor is defined as $\Delta = K_{\text{eff}}(0) \mathcal{V}/k_BT$. From the previous analysis, the presence of $T_{\text{IEC}}$ gives rise to a correction to the voltage-dependent anisotropy coefficient, i.e., $K_{\text{eff}} \rightarrow K_{\text{eff}} - m_z T_{\text{IEC}}/2t_{\text{free}}$. Therefore, the effective energy barrier for switching is

$$E_{\text{eff}}^b = \mathcal{V} \left(1 - \frac{T_{\text{STT}}}{T_{\text{STT}}^c}\right) \left(K_{\text{eff}} - m_z T_{\text{IEC}}/2t_{\text{free}}\right), \quad (13)$$

from where we can write down the switching time as $\tau^{-1} = f_0 \exp(-E_{\text{eff}}^b/k_BT)$ or

$$\tau^{-1} = f_0 \exp \left[ -\frac{\mathcal{V}}{k_BT} \left(1 - \frac{T_{\text{STT}}}{T_{\text{STT}}^c}\right) \left(K_{\text{eff}} - m_z T_{\text{IEC}}/2t_{\text{free}}\right) \right], \quad (14)$$

for parallel to anti-parallel switching, where $f_0$ is the attempt frequency.
FIG. 2: (Color online) Total field-like torque for several different perpendicular magnetic anisotropies (PMA) $K_{\text{eff}}(0)$ for an asymmetric magnetic tunnel junction with $\delta = 1.8$ eV. We consider (a) negative and (b) positive applied bias voltage giving a charge current-density of $J = 5 \times 10^7$ A/cm$^2$.

PERPENDICULAR ANISOTROPY VERSUS NON-EQUILIBRIUM INTERLAYER EXCHANGE COUPLING

In Figs. 2(a) and (b) we show the total field-like torque acting on the magnetization of the free layer considering $\delta = 1.8$ eV, $\xi = 0$ and different effective PMA constants $K_{\text{eff}}$ for negative and positive applied bias voltage, respectively. One observes that the non-equilibrium IEC torque is able to overcome the anisotropy barrier bidirectionally for a large range of perpendicular magnetic anisotropy (PMA) coefficients, enabling p-MTJs higher thermal stability factor.

SPIN TRANSFER TORQUE EFFICIENCY

We show in Figs. 3(a) and (b) the angular dependence of the charge current-density and STT efficiency, respectively, considering an applied voltage of $V = 250$ mV and different lead asymmetries. The current is clearly a cosine function of $\theta$ for the different degree of asymmetries considered and can be written in the general form $J = J + \Delta J \cos(\theta)$, with $J = (J_P + J_{AP})/2$ and $\Delta J = (J_P - J_{AP})/2$ being the average and asymmetry, respectively, of the charge current-density in the parallel (P) and anti-parallel (AP) configurations. As one increases the asymmetry $\delta$ between left and right leads, the total charge current-density decreases. We observe that $J$ drops faster for roughly all $\theta > \pi/2$ leading to states of even higher resistances in the AP configuration. Additionally, $J$ tends to vary very little with $\delta$ in the most asymmetric cases we have considered ($\delta = 1.2$ eV and $\delta = 1.8$ eV), where the corresponding curves tend to superpose each other. Thus, the asymmetry decreases the charge current density for most of the angular range including at $\theta = \pi/2$, where the non-equilibrium torques assume their maximum values. Figure 3(b) shows the angular dependence of the STT efficiency at $V = 250$ mV for the same asymmetries $\delta$. As we increase $\delta$, the STT efficiency becomes more pronounced for $\theta > \pi/2$. The angular dependence is given by $\frac{T_{\text{STT}} \sin(\theta)}{(J + \Delta J \cos(\theta))}$, which gives the distorted shape shown in Fig. 3(b). At the vicinity of $\theta = \pi$, the current density for the Asymmetric MTJ is smaller than that of the symmetric case [See Fig. 3(a)]. At the same time, $\sin(\theta) \approx 0$ such that $T_{\text{STT}} \sin(\theta)$ for different MTJ asymmetries are numerically close to each other. Therefore, the charge-current density drops faster than the STT and the torque efficiency is enhanced. The situation is different for the highest asymmetric case we have considered $\delta = 1.8$ eV. Here, we notice that the STT efficiency drops in relation of the previous asymmetric case ($\delta = 1.2$ eV). This is due to the fact that $J$ has essentially converged to that of $\delta = 1.2$ eV while the STT magnitude decreases. Therefore, the torque efficiency decreases.
FIG. 3: (Color online) Enhancement of the spin transfer torque efficiency for asymmetric magnetic tunnel junctions. Angular dependence of the (a) charge current-density and (b) spin transfer torque efficiency for different MTJ asymmetries $\delta$ at fixed applied voltage $V = 250$ mV.

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