

# **Measurements and Modeling Thermophysical Properties of Lubricants**

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- **History**

- 2014 NAVAIR (Naval Air Systems Command) contacted NIST; interested in thermophysical property data for gas turbine engine oil MIL-PRF-23699 (used in most military aircraft and 95% of commercial aircraft)
  - Needed accurate properties to assist in their Modeling and Simulation programs
    - Properties of interest include: viscosity, specific heat, density, thermal conductivity, enthalpy
  - Used software GFSSP (General Fluid System Simulator Program) developed by NASA. Desired ability to incorporate fluid properties for MIL-PRF-23699 into this software.
- NIST did not have anything available at that time.

- **History**

- 2015 NIST and NAVAIR entered into an agreement for NIST to provide
  - Highly accurate thermophysical property measurements of 3 pure fluid base stock components (POE5, POE7, POE9).
  - Highly accurate thermophysical property measurements of a fully formulated lubricant meeting MIL-PRF-23699
  - Thermophysical property model within REFPROP software for a fully formulated lubricant.
  - A mini-course for up to 8 participants on the measurement and modeling of thermophysical properties
- 2018 Work completed and Final report submitted to NAVAIR.

- 2019 Slightly sanitized version made available to the public at <https://doi.org/10.6028/NIST.IR.8263>

NISTIR 8263

## Thermophysical Properties of Polyol Ester Lubricants

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National Institute of Standards and Technology  
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## • **Measurements Summary**

- Completed measurements on 3 pure fluids (POE5, POE7, POE9) and the fully formulated lubricant MIL-PRF-23699
  - Thermal decomposition
  - Compressed liquid density (270 – 470 K, to 50 MPa, vib. tube, unc. <0.15%)
  - Ambient pressure density (278 – 343 K, vib. tube, unc. <0.18%)
  - Sound speed (283 – 423 K, up to 70 MPa, pulse-echo apparatus, unc. < 0.04%)
  - Ambient pressure sound speed (278 – 343 K, time of flight, unc. <0.2%)
  - Ambient pressure  $C_p$  (208 – 503 K; DSC method, 2-3 % unc.)
  - Vapor pressure (gas saturation method, POE5 only)
  - Viscosity (275 – 450 K, up to 137 MPa, oscillating piston viscometer, unc. 5-10%)
  - Thermal conductivity (300 – 500 K, up to 69 MPa, transient hot wire apparatus, unc. 0.5%)
- All the gory details in NISTIR 8263  
<https://doi.org/10.6028/NIST.IR.8263>

## • Modeling Summary

- Use density,  $C_p$ , sound speed,  $p_{\text{sat}}$  data to develop an equation of state (EOS)
  - Can compute all thermodynamic properties from this equation
- Use viscosity and thermal conductivity data to develop individual correlations for viscosity and thermal conductivity as functions of density and temperature
- Initially tried to develop a “surrogate” fluid model for the lubricant
  - This had worked well in the past for complex fuels such as jet and rocket fuels, and diesel but did not work so well for the lubricant
- Successfully developed a pseudo-pure fluid model for the lubricant
  - EOS coefficients and coefficients for viscosity and thermal conductivity correlations are in the NISTIR 8263
  - Much better way to disseminate results - REFPROP
    - “fluid” files are in the NISTIR 8263 or email us

- **REFPROP Model** <https://www.nist.gov/srd/refprop>
  - **RE**ference **F**luid Thermodynamic and Transport **PRO**perties (NIST23) sold by NIST Standard Reference Data
    - Contains thermophysical properties of industrially important pure fluids (147 at present) and mixtures (up to 20 components)
  - **Easy-to-use computer program**
    - **Can provide tables or graphs of properties of fluids**
      - Thermodynamic properties (density, sound speed, heat capacity, enthalpy, entropy, boiling point, etc.)
      - Transport and other properties (viscosity and thermal conductivity, surface tension)
    - **Easy to add a new “fluid file” for the lubricant MILPRF23699**
      - Just place the MILPRF23699.FLD file (a plain text file) in a specific directory where all files of type .FLD reside, then run the program
  - **Source code (FORTRAN) included**
  - **Can Interface with common applications (Excel, MATLAB, LabView, Python, C/C++, etc.) through wrappers and DLL**
    - Info on wrappers here: <https://github.com/usnistgov/REFPROP-wrappers>



## Results for MIL-PRF-23699

Developed a Helmholtz-form EOS

All thermodynamic properties come from the EOS

$$\frac{\alpha(\rho, T)}{RT} = \alpha(\delta, \tau) = \alpha^0(\delta, \tau) + \alpha^r(\delta, \tau) \quad \delta = \rho / \rho_c \quad \tau = T_c / T.$$

$$\alpha^0 = \frac{h_0^0 \tau}{RT_c} - \frac{s_0^0}{R} - 1 + \ln \frac{\delta \tau_0}{\delta_0 \tau} - \frac{\tau}{R} \int_{\tau_0}^{\tau} \frac{c_p^0}{\tau^2} d\tau + \frac{1}{R} \int_{\tau_0}^{\tau} \frac{c_p^0}{\tau} d\tau$$

$$\alpha^r(\delta, \tau) = \sum N_k \delta^{d_k} \tau^{t_k} + \sum N_k \delta^{d_k} \tau^{t_k} \exp(-\delta^{l_k}) + \sum N_k \delta^{d_k} \tau^{t_k} \exp(-\eta_k (\delta - \varepsilon_k)^2 - \beta_k (\tau - \gamma_k)^2)$$

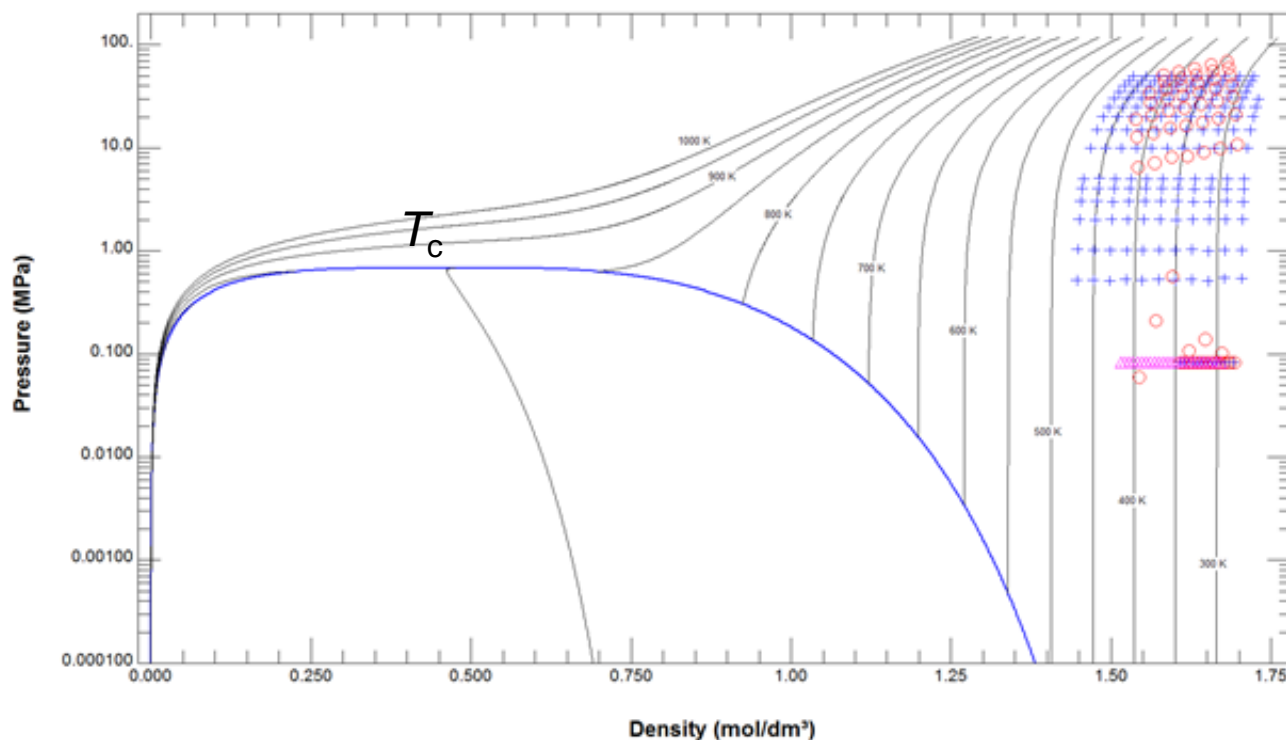
Uncertainties:

- density 0.2%
- sound speed 0.1%
- $C_p$  0.3%

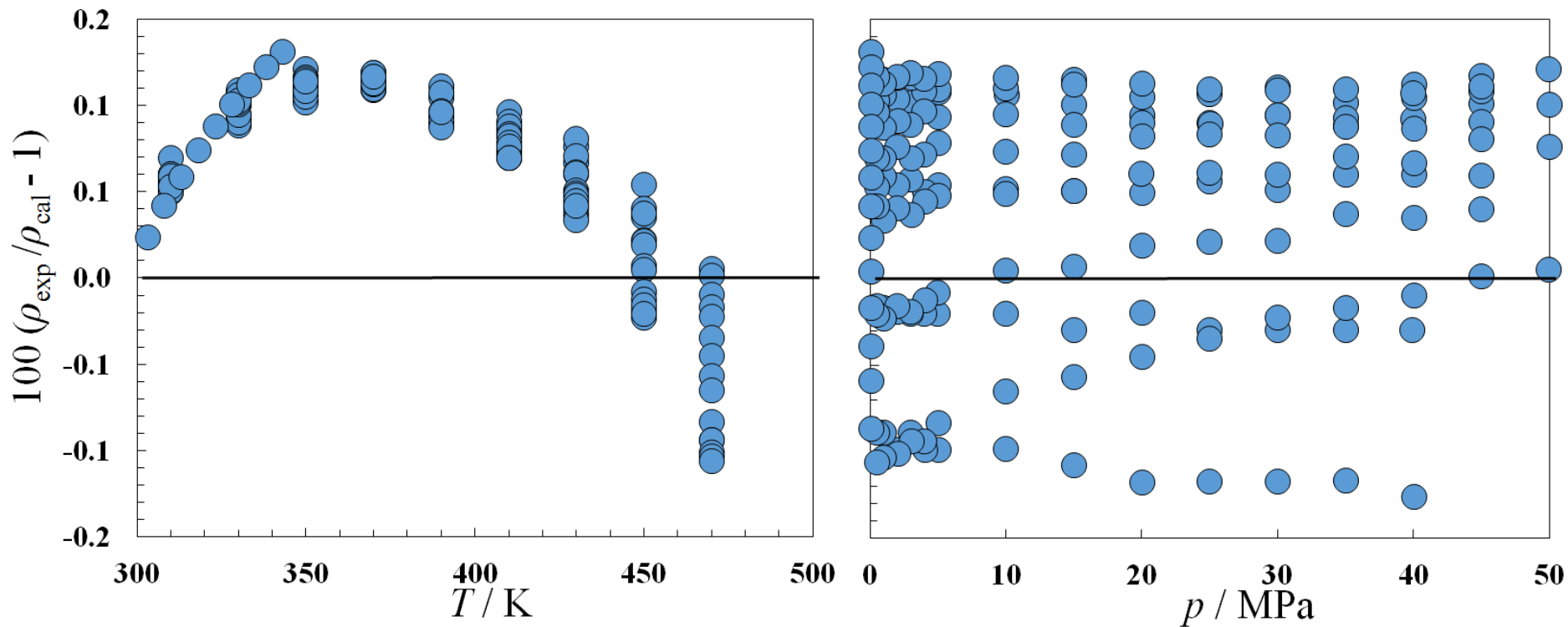


## Note on developing EOS

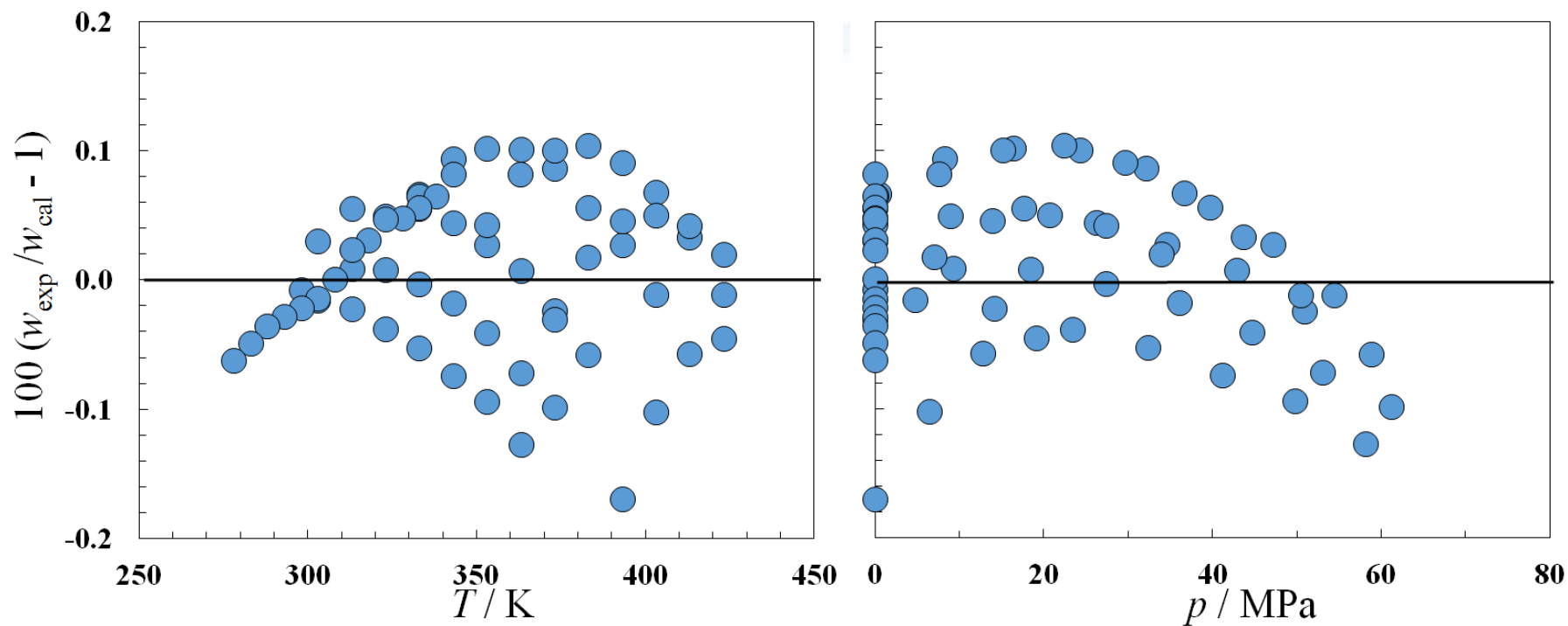
- Measurements, although seeming comprehensive, do not cover the entire fluid space
- Use a set of constraints during development to ensure appropriate behavior over entire fluid surface



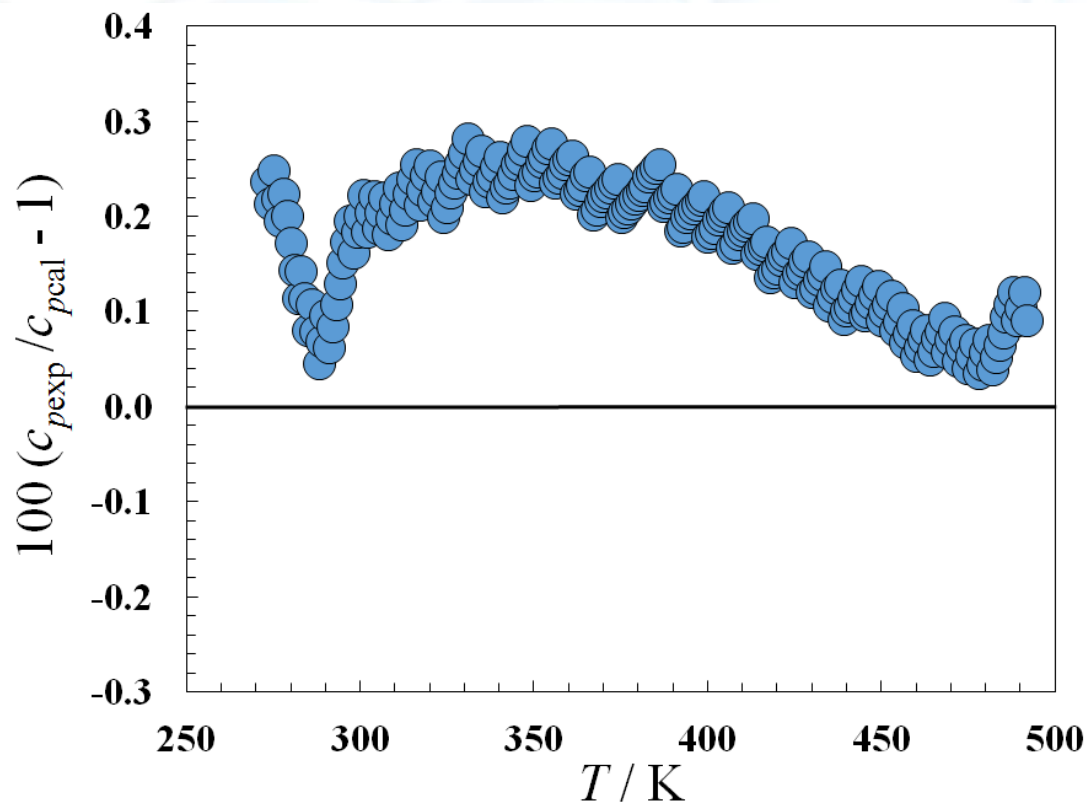
# Results for MIL-PRF-23699: density



## Results for MIL-PRF-23699: speed of sound

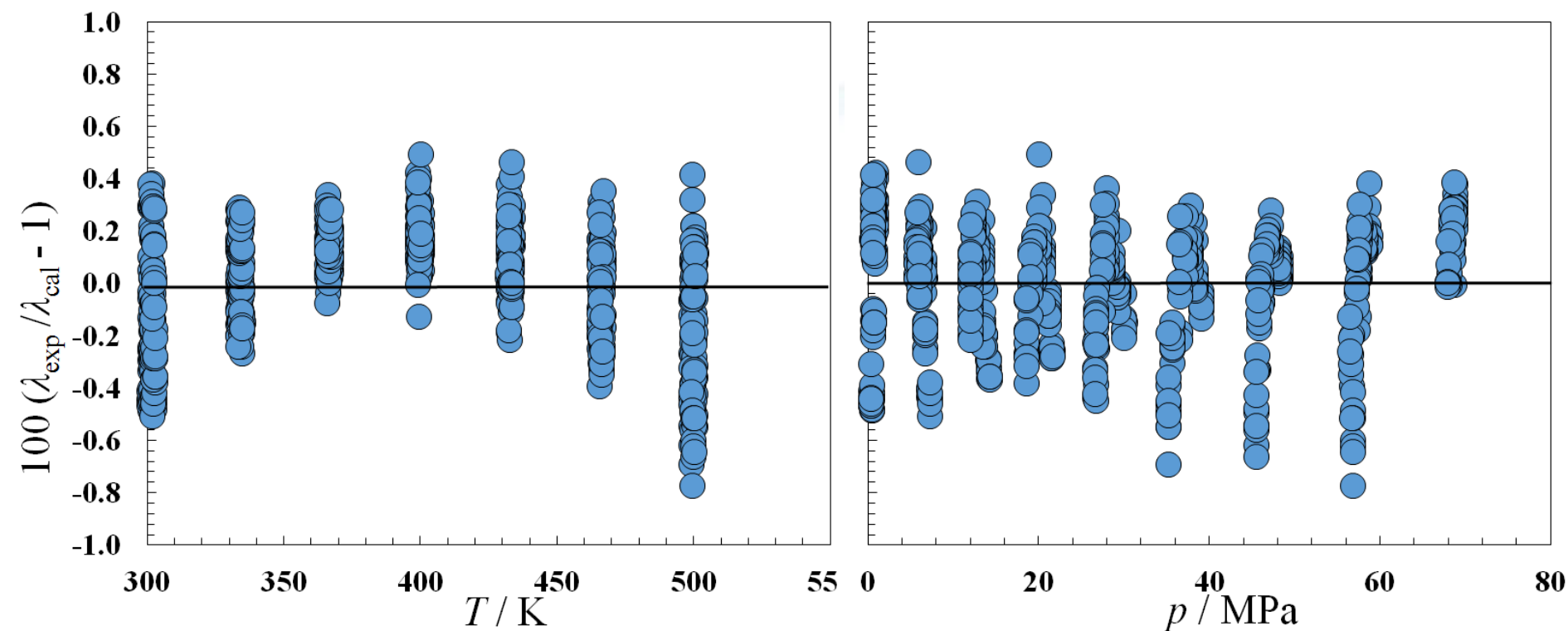


## Results for MIL-PRF-23699: heat capacity



All measurements at ambient pressure (0.083 MPa)

# Results for MIL-PRF-23699: thermal conductivity

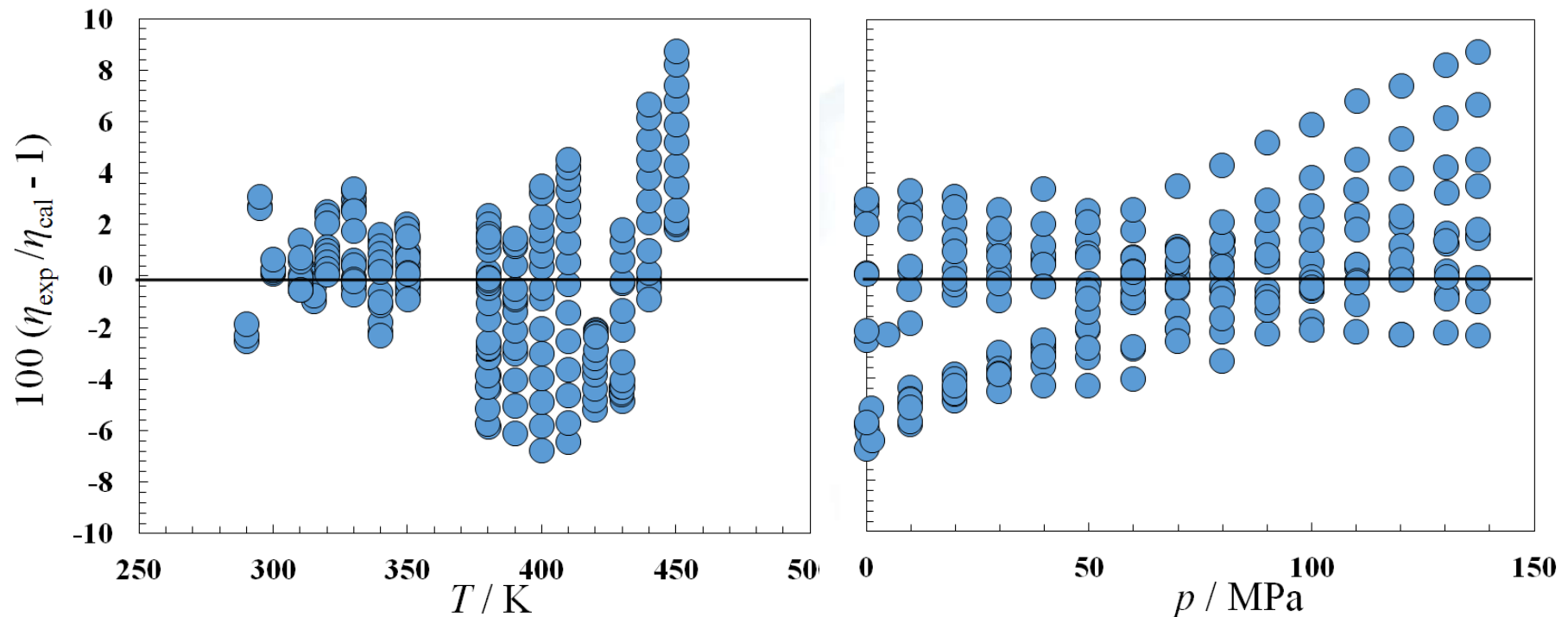


$$\lambda(T_r, \rho_r) = \lambda^0(T_r) + \Delta\lambda^{\text{res}}(T_r, \rho_r) + \lambda^{\text{crit}}(T_r, \rho_r),$$

$$\lambda^0(T_r) = \sum_{k=0}^n \alpha_k T_r^k \quad \Delta\lambda^{\text{res}}(T, \rho) = \sum_{l=1}^3 (\beta_{1,l} + \beta_{2,l}(T/T_c))(\rho/\rho_c)^l$$

$$\lambda^{\text{crit}}(T_r, \rho_r) \text{ found with generalized method } f(T_c, \rho_c, p_c, \text{MW}, \omega)$$

# Results for MIL-PRF-23699: viscosity



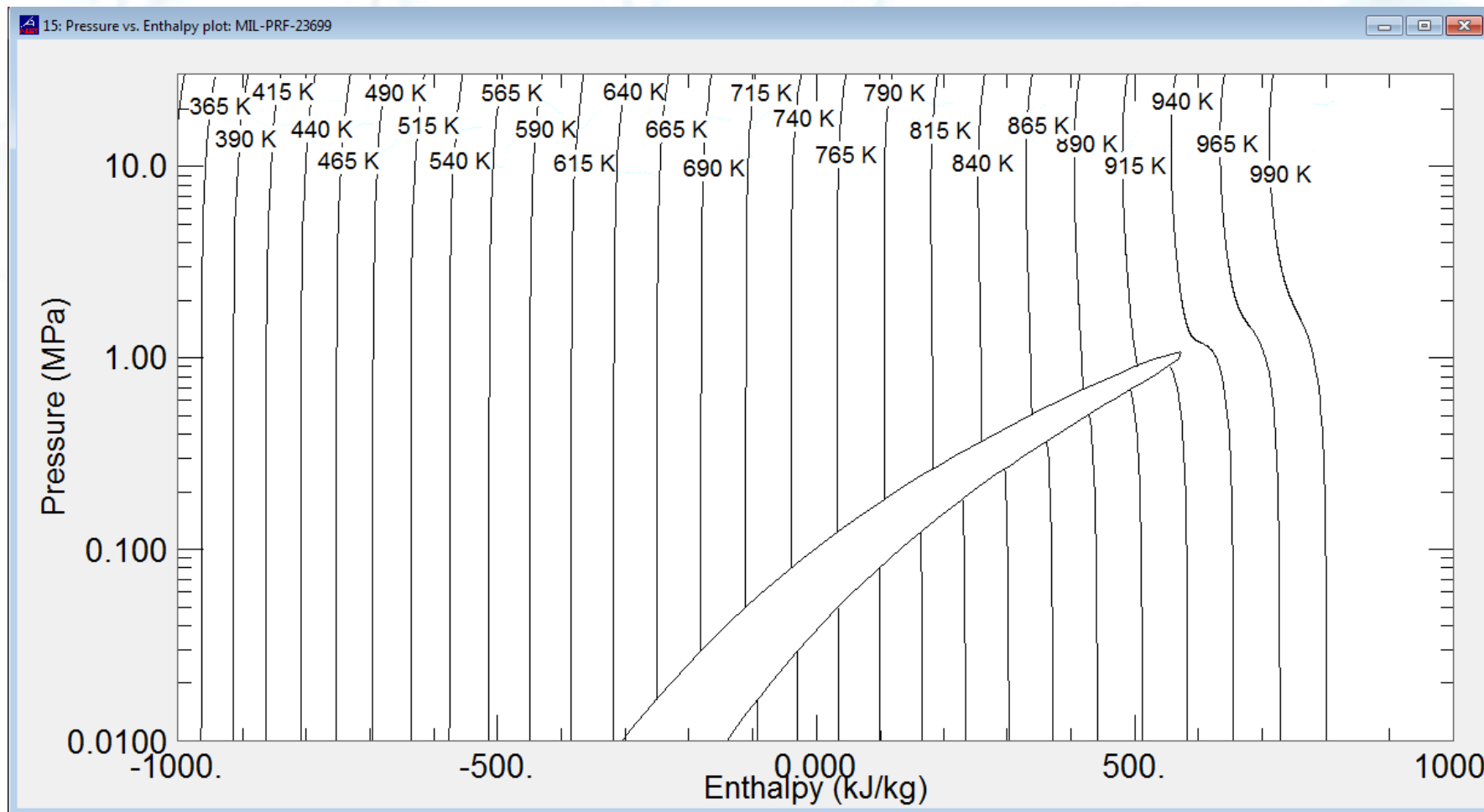
$$\eta(\rho_r, T_r) = \eta_0(T_r) + \Delta\eta(\rho_r, T_r) + \Delta\eta_c(\rho_r, T_r)$$

$\eta_0(T_r)$  found from method of Chung *et al.* (1988)

$$\Delta\eta(\rho_r, T_r) = (a_1\Gamma + a_2\Gamma^2 + a_3\Gamma^3 + a_4\Gamma^{11})\sqrt{T_r}\rho_r^{2/3}, \quad \Gamma = \rho_r^{3.36}/T_r,$$

$\Delta\eta_c(\rho_r, T_r)$  set to zero

# Results for MIL-PRF-23699: PH chart generated by REFPROP



## Results for MIL-PRF-23699: tables generated by REFPROP

16: MIL-PRF-23699: Specified state points

	Temperature (K)	Pressure (MPa)	Density (kg/m <sup>3</sup> )	Enthalpy (kJ/kg)	Entropy (kJ/kg-K)	Cp (kJ/kg-K)	Sound Speed (m/s)	Therm. Cond. (W/m-K)	Viscosity (mPa-s)
1	315.02	79.941	1018.8	-998.87	-2.0982	1.8429	1618.9	0.16236	75.570
2	315.02	69.898	1014.2	-1006.8	-2.0920	1.8417	1585.8	0.16033	66.052
3	315.01	59.865	1009.4	-1014.7	-2.0856	1.8407	1551.5	0.15824	57.548
4	315.00	49.827	1004.4	-1022.6	-2.0791	1.8399	1515.7	0.15606	49.937
5	315.01	39.787	999.12	-1030.5	-2.0722	1.8394	1478.2	0.15378	43.113
6	315.01	29.759	993.56	-1038.3	-2.0651	1.8391	1438.9	0.15140	37.079
7	315.02	19.733	987.66	-1046.1	-2.0577	1.8393	1397.6	0.14889	31.726
8	300.01	0.051000	986.76	-1088.6	-2.1311	1.8010	1358.2	0.14580	44.160
9	300.02	9.7320	992.84	-1081.1	-2.1388	1.8001	1401.4	0.14832	52.491
10	300.03	19.737	998.75	-1073.3	-2.1464	1.7998	1443.6	0.15078	62.320
11	300.04	29.740	1004.3	-1065.5	-2.1537	1.7998	1483.6	0.15312	73.505
12	300.04	39.759	1009.6	-1057.7	-2.1608	1.8002	1521.7	0.15535	86.240
13	310.09	0.030000	978.77	-1070.3	-2.0711	1.8279	1324.9	0.14429	28.114
14	310.08	9.7170	985.13	-1062.9	-2.0790	1.8267	1369.3	0.14694	33.178
15	310.08	19.721	991.28	-1055.1	-2.0866	1.8262	1412.4	0.14952	39.115
16	310.07	29.725	997.07	-1047.4	-2.0940	1.8260	1453.3	0.15196	45.881
17	310.07	39.748	1002.5	-1039.5	-2.1011	1.8263	1492.2	0.15430	53.533
18	310.08	49.776	1007.7	-1031.7	-2.1079	1.8269	1529.3	0.15653	62.136
19	310.07	59.807	1012.7	-1023.8	-2.1146	1.8277	1564.9	0.15867	71.862
20	310.08	69.868	1017.4	-1015.9	-2.1210	1.8288	1599.1	0.16073	82.712
21	310.08	79.917	1021.9	-1008.0	-2.1272	1.8300	1632.0	0.16271	94.839
22	290.04	0.064000	994.74	-1106.4	-2.1915	1.7750	1392.0	0.14725	72.968
23	290.05	4.7480	997.61	-1102.8	-2.1953	1.7747	1412.7	0.14843	79.603



## Conclusions

- We developed, based on our experimental measurements, models for the thermophysical properties of MIL-PRF-23699 (and 3 pure POE's)
  - including  $p$ , density,  $T$ , heat capacity, sound speed, vapor pressure, enthalpy, entropy, viscosity, thermal conductivity
- Models implemented in easy-to-use computer program REFPROP
- Details and REFPROP-compatible files in freely available publication  
<https://doi.org/10.6028/NIST.IR.8263>

## Questions?

