- 1 Assessing Radiation Hardness of Silicon Photonic Sensors
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- 8 Abstract
- 9 In recent years, silicon photonic platforms have undergone rapid maturation enabling not only
- 10 optical communication but complex scientific experiments ranging from sensors applications to
- 11 fundamental physics investigations. There is considerable interest in deploying photonics-based
- 12 communication and science instruments in harsh environments such as outer space, where
- 13 radiation damage is a significant concern. In this study, we have examined the impact of cobalt-
- 14 60 γ-ray radiation up to 1 megagray (MGy) absorbed dose on silicon photonic devices. We do
- 15 not find any systematic impact of radiation on passivated devices, indicating the durability of
- 16 passivated silicon devices under harsh conditions.
- 17
- 18 Introduction
- 19 The last three decades have witnessed an exponential growth in photonics, driven in part by
- 20 improvements in micro-electronics fabrication techniques and by increasing adoption of
- 21 photonics components by the telecommunications industry. Tools originally developed for the
- 22 telecommunications industry are now being exploited to develop novel sensors for a wide variety
- 23 of applications and deployment scenarios.¹⁻⁹ Photonic sensors and communication systems are
- 24 particularly valuable for operation in harsh environments, e.g. outer space and nuclear power
- 25 plants, due to their small size, low power consumption, and tolerance to environmental variables
- 26 such as mechanical vibrations.¹⁰⁻¹³
- 27 Such devices are nevertheless quite sensitive to external stimuli that produce changes in
- refractive index of the host material. In suitably designed photonic devices, small changes in
- 29 temperature can produce measurable changes in resonance peak wavelength, thus making them
- 30 useful for photonic thermometry and similar applications.⁹ This sensitivity to refractive index is
- 31 geometrically increased in resonant devices, like the ring resonator or photonic crystal cavity,
- 32 where refractive index sensitivity grows with the device's quality factor. Whether this sensitivity
- 33 affects their usefulness in high radiation environments, however, is an open question. 10,13
- Radiation induced damage is known to cause dislocations and other defects in crystalline
- 35 structure that affect refractive index.¹⁴ We recently demonstrated that Ge-doped fiber Bragg
- 36 gratings (FBG) show complex dose-dependent changes in resonance peak center resulting in $\frac{15}{10}$
- 37 significant offset errors of up to \pm 16.5 °C in thermometry applications.¹⁵ These changes in
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- 38 Bragg resonance are independent of the polymer coating¹⁵ and likely derive from significant
- 39 change in Ge coordination.¹⁴
- 40 In silicon-on-insulator (SOI) based electronic devices, trapped charges and local changes in bond
- 41 structure are a known cause of device failure.¹⁶ In principle, changes in the refractive index due
- 42 to changes in free carrier population and damage to the Si lattice can significantly degrade the
- 43 measurement sensitivity and accuracy of a photonic sensor. Bhandaru *et al* 17 have reported that
- 44 unpassivated Si ring resonator devices exposed to relatively low levels of ionizing radiation (< 9
- 45 kGy) show a blue shift in resonance wavelength which was not observed for passivated devices 46 $\frac{1}{2}$ blue at \frac
- 46 exposed to ≈ 1.5 kGy of ionizing radiation. The authors attributed the observed shift in 47 unpassivated devices to accelerated growth of native oxide. Similar results have been reported
- 48 for amorphous silicon and silicon nitride devices.^{11,12} We note that a photonic sensor operating
- 49 in a high radioactivity environment such as a nuclear power plant is expected to receive about 1
- 50 MGy^{18} of dose per year. Under such conditions it is possible that sensor performance may be
- 51 negatively impacted by changes in refractive index, covalent bond breaking, radiation induced
- 52 densification and/or changes in surface chemistry. Such changes would result in increased
- 53 propagation losses resulting in lower quality factors and drift in resonance wavelength of
- 54 resonant devices.
- 55 In this study, we systematically examine the impact of γ -radiation, up to a cumulative dose of 1
- 56 MGy (1 Gy = 100 Rad) from ⁶⁰Co γ -ray radiation on silicon ring resonators and Bragg
- 57 waveguides across multiple devices and chips. The dose absorbed by such chips was modelled
- using a radiation transport Monte Carlo simulation based on engineering drawings of the source
- and previous measurements of the radiation field. Further details of the Monte Carlo simulations
- 60 used to calculate absorbed dose and the experimental setup are given in the Methods section. Our
- 61 results indicate that silicon photonic devices can withstand high cumulative doses without any
- 62 significant degradation in performance.
- 63
- 64 Results
- 65 Bragg waveguides
- 66 Bragg waveguides and ring resonators exposed to varying levels of γ -ray radiation do not show
- 67 any significant changes in spectral characteristics. A typical Bragg waveguide transmission
- 68 spectrum, shown in Figure 1, does not show any systematic changes in either the peak center or
- 69 the bandwidth of the Bragg waveguide rejection window. The variation in peak center observed
- between the different dose spectra is found to be 8 pm and is not correlated with dose ($R^2 =$
- 71 0.28). Similarly, variation in linewidth (2.6 pm) is poorly correlated with dose ($R^2 = 0.54$) and is
- 72 within the measurement uncertainty of \pm 7 pm. The linewidth in a Bragg device is directly
- 73 proportional to the refractive index contrast between the waveguide and etched step regions
- 74 (where the evanescent field interacts with the surrounding oxide material, sampling an
- effectively lower refractive index than the unetched waveguide region)¹⁹. A lack of significant
- change in Bragg linewidth, therefore, suggests the oxide layer immediately next to the Si does
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- 77 not suffer any significant changes such as bond breaking or densification of the oxide layer due
- to radiation exposure. Similarly, a lack of significant change in peak isolation suggests the
- 79 devices escaped with little to no damage to the Si surface or lattice.



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Figure 1. Si ring resonator and Bragg waveguide (insert) show no significant changes in spectral characteristics as absorbed dose is increased from 0 Gy to 1048 kGy (see text for details).

83

84 Ring resonators

85 In ring resonators, where spectral consequences of small changes in device characteristics, such

86 as refractive index, are expected to magnify due to recirculation of light in the ring structure, we

do not observe any significant dependence on absorbed dose. We have examined the impact of
 radiation in several ring resonator devices with quality factors (O-factors) ranging from 5,000 to

- addation in several ring resonator devices with quality factors (Q-factors) ranging from 5,000 to
 30,000 at room temperature. As shown in Figure 2 and Figure 3, ring resonator devices do not
- 90 show any significant dose-dependent change in the free spectral range (FSR), Q-factor, and peak
- 91 position. The FSR was uncorrelated with dose ($R^2 = 0.08$), with a standard deviation for the 4
- 92 doses of 2.5 pm (0.031 %). The Q-factor did decrease over time, but that decrease was the same
- 93 for the control chip as for the irradiated chips and thus cannot be unambiguously ascribed to dose
- 94 (Figure 2 top). The observed decrease of ≈ 12 % in Q-factor is correlated with peak input power
- and is reproduced when input power is doubled, indicating the observed effect is due to the
- 96 device undergoing self-heating during the laser scan, not radiation damage. The small variation
- 97 in absolute peak position observed for Chips 1-3 between irradiations (average standard
- deviation of $[13 \pm 13]$ pm) is statistically indistinguishable to changes observed in the control
 - 3

99 chip. This small variability was found to be random, with the most stringent test coming from the

100 peak position at 20 °C (measured at 0 Gy dose), which was found to be uncorrelated to dose,

101 with $R^2 = 0.01$. We note that all four chips are from the same batch and contain the same devices.

102 The control chip traveled with the other chips to and from the photonics lab to the radiation

103 facility but was never exposed to radiation itself.



104

Figure 2. Q-value (top) and peak position (bottom) of a ring resonance across three different
 irradiated chips (plus control chip #4) are not significantly impacted by radiation dose (see text

107 for discussion). Number next to the symbols refer to dose (kGy) delivered on that particular date.

108

109 As quantified above, the FSR of the devices does not show any significant changes, clearly

110 indicating that neither the group index nor the dispersion (parameters important in

111 communication systems) is impacted by radiation exposure. Examination of the temperature-

dependent response of ring resonator devices shows that the temperature sensitivity is also not

113 impacted by radiation dose. For the data shown in Figure 3, the average and standard deviation

of the three responses was (76.9 ± 0.2) pm/°C. A linear regression of response as a function of

115 dose returned a slope of $(-4 \pm 2) \cdot 10^{-4} \frac{\text{pm}}{\text{°C} \cdot \text{Gy}}$, which was not significant at the 95 % level (t = -

116 1.8, p = 0.32). The slight offset variability observed between doses (residuals shown in Figure 3

117 insert) is within the limited precision of the thin film resistance thermometer (± 0.1 °C) when 118 employed using nominal coefficients.

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Figure 3. Temperature response of silicon ring resonator. Top plot shows residuals from a common fit to all the data. Propagated uncertainty due to temperature measurement is shown for one point. The temperature response is not impacted by absorbed radiation dose (see text for details).

125



127 In this study, we have examined the impact of ionizing radiation on silicon photonics devices.

128 Devices were irradiated within a self-contained, commercially produced ⁶⁰Co irradiator, and

129 delivered doses were estimated using well-established widely available Monte Carlo codes.

- 130 Measurement of device characteristics such as peak center, peak width, FSR and temperature
- 131 sensitivity do not reveal any significant dose-dependent changes, indicating that for all devices
- 132 tested, the characteristic group index, dispersion and thermo-optic coefficient remain constant for
- aggregate doses up to 1 MGy (the maximum absorbed dose delivered in this study). These
- results are in stark contrast with those of FBG-based sensors, where radiation induced changes in Bragg resonance result in significant drift in device characteristics.^{10,13,15} Our results bode well
- for efforts to leverage existing infrastructure in silicon photonics to develop communication and
- 137 sensor platforms for operating in harsh environments, such as industrial sterilization of health
- 138 care products or radiation processing systems where doses can be in the range 15 kGy to 300
- 139 $kGy^{20,21}$, or nuclear power plants where dose rates of 10 kGy/h are possible¹⁸. Precision photonic
- 140 sensors could find additional use in instrumentation used in radiotherapy clinics or space-based
- 141 systems, where much lower aggregate doses (< 100 Gy) are more commonplace but high
- reliability and accuracy are paramount.²²⁻²⁴
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144 Methods

145 Photonic Interrogation

The experimental measurement apparatus has been described in detail elsewhere.^{9,25} Briefly, a C-146 band laser (New Focus TLB-6700 series 1) is swept over the sensor resonance. Ten percent of 147 laser power was immediately picked up from the laser output for wavelength monitoring 148 149 (HighFinesse WS/7) while the rest is evanescently coupled to the photonic device under test 150 using an optical fiber held within a few microns of the chip surface. The photonic chip itself was 151 mounted on a Peltier assembly atop a 3-axis stage (Newport). Input from a platinum resistance 152 thermometer (measurement accuracy ± 0.1 °C) is fed to a proportional-integral-derivative controller that drives a thermoelectric cooler and maintains the temperature to within 0.02 °C of 153 154 the set value. Photonic chips were fabricated at the CEA-LETI (Laboratoire d'Electronique des 155 Technologies de l'Information, France) fabrication facility using standard CMOS technology. Three of the representative chips from the batch were systematically exposed to varying levels of 156 γ -ray radiation at the NIST high-dose dosimetry laboratory, while a fourth chip, used as a 157 158 control, was never exposed to radiation, though it traveled with the other three chips between the

- 159 photonics testing facility and the radiation facility.
- 160
- 161 Gamma-ray irradiation
- 162 Photonic sensors were irradiated with γ -rays in the NIST high-dose dosimetry laboratory. Three
- 163 Gammacell (GC) 220 ⁶⁰Co irradiators (Nordion, Canada) were used with dose rates between 0.2
- 164 kGy/h and 3.9 kGy/h. Most of the irradiations were done using irradiator number GC207, which
- 165 contained a nominal activity of $1.76*10^{14}$ Bq on a reference date of December 31, 2016 and
- 166 delivered an absorbed dose rate to water, determined using alanine dosimetry, of R=1.08 Gy/s
- 167 on the reference date, with an expanded uncertainty²⁶ of about 2 %. This amounts to a dose rate $\frac{60}{10}$ for $\frac{10}{10}$ for $\frac{10}{$
- 168 per ⁶⁰Co activity of $D = 6.12*10^{-15}$ Gy/s/Bq.
- 169
- 170 Monte Carlo Calculations of absorbed dose
- 171 Monte Carlo simulations were undertaken to calculate the dose to the silicon devices based on
- measured dose to alanine calibration pellets. A simplified geometry for the GC 220 was created
- based on the irradiator specification sheet²⁷ using the EGSnrc code DOSRZnrc.²⁸. The 1-cm
- diameter ⁶⁰Co rods were simulated as a single cylindrical shell. Following Rodrigues et al.²⁹,
- aluminum and steel shells of 2 mm thickness each were implemented between the sources and

- 176 the exposure chamber. The 60 Co emission spectrum was simplified to consist of two 1.25 MeV 177 y-rays.
- 178 Two irradiation geometries were simulated- the chamber calibration and chip irradiation, shown
- in Figure 4. The calibration geometry, used to transfer calibration from the primary standard of
- absorbed dose to water, consists of 5-mm diameter alanine pellets stacked inside a polystyrene
- 181 cylinder (pedestal) of wall thickness 3.7 mm³⁰. For the chip irradiation, one chip at a time was
- 182 placed inside a glass beaker of diameter and wall thickness of 30.5 mm and 1.3 mm,
- 183 respectively. Although the chip device layer was only a few μ m thick, the simulated dose to the
- 184 chip was averaged over the top 100 μ m of the chip, to achieve adequate Monte Carlo statistics.



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Figure 4. Simulated geometry for the calibration pedestal (left), and chip in beaker (right)

geometry (right). The radiation absorber material in the model could be varied among water,silicon, and silica, as needed.

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- 190 For the calibration geometry, the EGSnrc simulated result was $D = 6.23 \cdot 10^{-15}$ Gy/s/Bq, which
- is 2 % higher than the nominal calibrated value. This agreement is adequate, considering the
- approximate source geometry of the EGSnrc model and the Monte Carlo counting statistics of
- about 2 %. Despite the adequate agreement in absolute dose per activity, the EGSnrc model was
- not used for an absolute calculation of dose, but only used to scale the dose from the calibration
- 195 geometry to the chip geometry. For the chip geometry, the EGSnrc result was $D = 5.42 \cdot 10^{-15}$

- 196 Gy/s/Bq. Thus, the ratio of the calculated dose for the chip geometry to the calibration geometry
 197 was 0.870, with a total Monte Carlo uncertainty of about 3 %.
- 198 Scaling the calibrated value for *R* by the ratio of the EGSnrc-calculated *D* values for the chip
- 199 geometry to the calibration geometry, results in a dose rate to the chip of 0.94 Gy/s with an
- 200 expanded uncertainty of 7 % (k = 2).
- 201 An approximate gamma-ray field map was calculated by numerically solving an integral
- 202 representing the γ -ray flux, *F*, inside a chamber consisting of a thin, radiating, cylindrical shell,

$$F(x,h) = \int_{-(\frac{L}{2}+h)}^{L/2-h} \int_{0}^{2\pi} \frac{r}{(r\cos(\theta)-x)^2 + (r\sin(\theta))^2 + z^2} d\theta dz$$
(1)

where L = 210 mm is the shell length, r = 105 mm is the shell radius, and (x, h) is the test

- 205 position within the chamber. No interactions were considered. The field map, relative to the
- value in the center of the chamber, is shown in Figure 5. Along the vertical axis of the chamber
- 207 (*x*=0), the field changes by -1 % at $z = \pm 18$ mm. Along the midplane of the chamber (*h*=0), the 208 field changes by +1% at $x = \pm 14$ mm. Therefore, the ≈ 5 mm positioning accuracy of the chip
- would not significantly affect the absorbed dose beyond the Monte Carlo and calibration
- 210 accuracy.
- 211

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- 215
- 216 To explore the issue of transient charged particle equilibrium (TCPE), a Geant4³¹ Monte Carlo
- 217 model was constructed for a version of the chip geometry. A 1.25 MeV γ -ray source was
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- 218 incident from the side of the chip, aligned with the center of the top layer, which was 200 μ m
- thick much thicker than the actual device layer, but still not thick enough to achieve TCPE.
- 220 Only about 1 out of 50 γ -rays interact with the chip. Of those that do, about 80 % produce
- 221 Compton-scattered electrons that escape into the air from the top layer. Since there is not an
- equal energy flux of electrons produced in the air that pass into the top Si layer, TCPE is not
- 223 achieved. Therefore, the absorbed dose to the chip cannot simply be calculated based only on the
- relative linear-energy transfer and density of silicon relative to water. Rather, full Monte Carlo
- simulations are required, as were done here.
- 226
- 227 Disclaimer
- 228 Certain equipment or materials are identified in this paper in order to specify the experimental
- 229 procedure adequately. Such identification is not intended to imply endorsement by the National
- 230 Institute of Standards and Technology, nor is it intended to imply that the materials or equipment
- 231 identified are necessarily the best available.
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- 239
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- The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.
- 243 Author Contributions
- 244 RET planned the irradiation scheme. LTC and IMP irradiated the chips. ZA and NNK made the
- 245 photonic measurements. ZA and RF analyzed the data. RF performed the Monte Carlo
- simulations. ZA and RF drafted the manuscript, RET and IMP made significant edits, and all
- authors provided final review.

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