# Temperature dependent $^{29}$Si incorporation during deposition of highly enriched $^{28}$Si films

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In this study, we examine the mechanisms leading to $^{29}$Si incorporation into highly enriched $^{28}$Si films deposited by hyperthermal ion beams at elevated temperatures in the dilute presence of natural abundance silane (SiH$_4$) gas. Enriched $^{28}$Si is a critical material in the development of quantum information devices because $^{28}$Si is free of nuclear spins that cause decoherence in a quantum system. We deposit epitaxial thin films of $^{28}$Si enriched *in situ* beyond 99.99998 % $^{28}$Si onto Si(100) using an ion beam deposition system and seek to develop the ability to systematically vary the enrichment and measure the impact on quantum coherence. We use secondary ion mass spectrometry to measure the

1

30    residual $^{29}$Si isotope fraction in enriched samples deposited from $\approx$ 250 °C up to 800 °C.

31    The $^{29}$Si isotope fraction is found to increase from $< 1$ x $10^{-6}$ at the lower temperatures, up

32    to $> 4$ x $10^{-6}$ at around 800 °C. From these data, we estimate the temperature dependence

33    of the incorporation fraction, $s$, of SiH$_4$, which increases sharply from about 2.9 x $10^{-4}$ at

34    500 °C to 2.3 x $10^{-2}$ at 800 °C. We determine an activation energy of 1.00(8) eV associated

35    with the abrupt increase in incorporation and conclude that below 500 °C, a temperature

36    independent mechanism such as activation from ion collisions with adsorbed SiH$_4$

37    molecules is the primary incorporation mechanism. Direct incorporation from the adsorbed

38    state is found to be minimal.

## I.  INTRODUCTION

40        In solid state quantum information (QI), enriched $^{28}$Si is a critical material for the

41    further development of silicon based quantum computing architectures, e.g., quantum

42    dots, quantum wells, and few dopant atoms in Si. By eliminating $^{29}$Si nuclei, which have

43    a non-zero nuclear spin and are present with roughly a 5 % natural abundance, pure $^{28}$Si

44    becomes an ideal spin-free environment in which to place the electron and nuclear spins

45    of qubits. Without the randomly fluctuating nuclear spins present, donor spins in $^{28}$Si

46    interact with their environment far less than in natural silicon leading to a greatly

47    enhanced coherence time (T$_2$*). Consequently, $^{28}$Si has been dubbed a "semiconductor

48    vacuum"[1]. Theoretical modeling and bulk electron spin resonance (ESR) experiments

49    predicted the enhancement in T$_2$* to be proportional to the reduction in $^{29}$Si

50    concentration[2,3], which further spurred interest in exploiting $^{28}$Si experimentally.

51    Numerous research groups have shown through bulk ESR and nuclear magnetic

52  resonance (NMR) experiments of $^{31}$P spins in $^{28}$Si that nuclear and electron spin

53  coherence (echoed, $T_2$) times can easily exceed seconds[1,4–6]. Si and Si/Ge based quantum

54  computing also can benefit from utilization of $^{28}$Si, e.g., quantum dots formed in Si and in

55  quantum wells within $^{28}$Si/SiGe heterostructures[7,8]. A few of these groups have begun to

56  show both long $T_2$ times and coherent manipulation in $^{28}$Si for both bulk donor spins[9] as

57  well as single electron spins in quantum wells[8] and quantum dots[4,10]. Additionally, qubit

58  manipulation schemes, which have been proposed for arrays of quantum dot qubits, and

59  which involve tuning the qubit ESR frequency via a Stark shift[11], have been demonstrated

60  in single quantum dots in $^{28}$Si. This Stark shifting mechanism relies on qubit spins that

61  have very narrow inhomogeneous ESR linewidths of a few kHz[1,12], which have only been

62  shown in a material with homogeneous mass such as highly enriched $^{28}$Si.

63       Despite these advantages, only a limited amount of the most highly enriched $^{28}$Si

64  (99.995 % $^{28}$Si) is available within the solid state quantum computing community for use

65  in ensemble spin QI experiments. Historically, $^{28}$Si has primarily been produced at great

66  cost and effort through international collaborations such as the International Avogadro

67  Coordination (IAC)[13], which produced bulk crystals. Other sources of $^{28}$Si include

68  enriched epilayers grown on natural abundance Si substrates, which are more abundant

69  within the community than bulk $^{28}$Si but are typically less highly enriched ($\approx$ 99.9 %

70  $^{28}$Si). QI experiments on single donor and dot spins largely utilized $^{28}$Si epilayer samples

71  and demonstrated the benefit of enriched $^{28}$Si to QI. A helpful review of some of the

72  different sources of $^{28}$Si that have been used in the QI field has been presented by Itoh

73  and Watanabe[14]. The lack of simply produced, readily available, and consistently highly

74  enriched $^{28}$Si has led us to develop a mass selected ion beam deposition system capable

75  of taking natural abundance silane ($SiH_4$) gas and enriching it *in situ* to an extremely high

76  level of $^{28}Si$ just prior to depositing it epitaxially on a target Si(100) substrate. Using this

77  system, thin films of highly enriched materials including $^{28}Si$ have previously been grown

78  amorphously on Si substrates at room temperature[15,16] as well as epitaxially at higher

79  temperatures (this work). Several other groups have also previously demonstrated

80  enriched $^{28}Si$ thin film deposition using an ion beam system, though not generally with a

81  focus on high quality material (highly enriched, chemically pure) for QI[17–19].

82      In addition to the general scarcity of $^{28}Si$ for semiconductor quantum computing

83  research, a specific need exists for enriched silicon with targeted levels of enrichment to

84  facilitate mapping the dependence of $T_2^*$ on $^{29}Si$ concentration in the few-spin regime.

85  Recent ESR measurements[4,10] of $T_2^*$ for single $^{31}P$ spins in $^{28}Si$ have disagreed with the

86  theoretical predictions for the same systems[2]. Our ion beam deposition system provides

87  us with a unique opportunity to produce $^{28}Si$ material at targeted levels of enrichment,

88  which can enable the mapping of $T_2^*$ as a function of enrichment in the single spin

89  regime. Understanding the sources of residual $^{29}Si$ in our films, and how to control them,

90  is a necessary step towards targeting specific enrichments.

91      In order for enriched $^{28}Si$ to be useful as a host material for qubit spins, it must not

92  only be isotopically pure, but chemically pure and highly crystalline so as to avoid

93  introducing other sources of decoherence such as impurity nuclear spins and dangling

94  bonds. Achieving single crystal epitaxial deposition of $^{28}Si$ films on Si(100) substrates

95  requires elevated substrate temperatures during deposition. We previously showed that

96  for amorphous room temperature deposition, the $^{29}Si$ in the film could be accounted for

97  by $^{29}SiH_4$ incorporation into $^{28}Si$ films due to a physical adsorption process which was

98    coincident with the ion beam deposition[16]. Depositing with an elevated substrate

99    temperature is expected to lead to a change in the activation of the $^{29}$Si contamination

100   through a chemical activation process described by a reactive sticking coefficient that is

101   similar in nature to chemical vapor deposition (CVD). Therefore, the goal of this study is

102   to determine how the $^{29}$Si and $^{30}$Si incorporation is affected by increasing the substrate

103   deposition temperature. Measurements of residual $^{29}$Si and $^{30}$Si isotope fractions

104   (amount-of-substance fraction in mol/mol, or isotopic concentration) are made using

105   secondary ion mass spectrometry (SIMS) which is extremely sensitive to isotope ratios.

106   This means that our monoisotopic ion beam deposition system offers a unique method of

107   measuring the activated sticking of natural abundance SiH$_4$ on Si substrates because any

108   isotopic contaminants ($^{29}$Si and $^{30}$Si) incorporated via sticking from SiH$_4$ are easily

109   distinguished from the background of pure $^{28}$Si being deposited from the ion beam.

110          In this article, we deposit epitaxial thin films of $^{28}$Si and measure the residual $^{29}$Si

111   and $^{30}$Si isotopes in samples deposited in different SiH$_4$ partial pressures while varying

112   the substrate deposition temperature of each sample. From these measurements, we

113   extract the temperature dependence of the incorporation fraction, $s$, of $^{29}$SiH$_4$ due

114   primarily to reactive sticking and determine the associated activation energy, $E_c$. These

115   results give us an understanding of, and thus control over, the $^{29}$Si concentration in $^{28}$Si

116   films.

## 117   II. EXPERIMENTAL METHODS

### 118   A.   Ion beam system and selectivity

119          Enriched $^{28}$Si thin films are deposited using a hyperthermal energy ion beam

120   deposition system. This system injects commercial, natural abundance SiH$_4$ source gas

121    into a high vacuum Penning-type ion source generating a $Si^+$ ion beam and then mass

122    filters the ions in a magnetic field before depositing them onto heated Si(100) substrates.

123    The mass separation principle and ion beam system used here have been described in

124    more detail elsewhere[16,20]. Previously, we analyzed $SiH_4$ incorporation in samples

125    deposited at room temperature, but now we examine the temperature dependence of $s(T)$

126    at temperatures required to facilitate epitaxial growth. The $SiH_4$ used here is unenriched

127    and is thus assumed to have a Si isotopic abundance roughly the same as natural Si (92.2

128    % $^{28}Si$, 4.7 % $^{29}Si$, and 3.1 % $^{30}Si$). This $SiH_4$ is also 99.999 % pure according to the gas

129    vendor. This $SiH_4$ is used to form a plasma within the ion source that both cracks and

130    ionizes the $SiH_4$ molecules. From the plasma, singly charged $Si^+$ ions (charge of 1 $e$, the

131    elementary charge) are extracted into the beamline at high voltage and enter a system of

132    electrostatic optics, which steer them into the magnetic field of a 90° sector mass

133    analyzer. $^{28}Si$ has a mass ≈ 28 u (unified atomic mass units), and by tuning to the

134    appropriate magnetic field, ions with a mass-to-charge ratio ≈ 28 u/$e$ (± 0.16 u/$e$ at 28 u)

135    pass through an aperture while those with different mass-to-charge ratios are rejected.

136    Beyond the aperture, ions are focused onto the target substrate in an ultra-high vacuum

137    (UHV) deposition chamber. In parallel, gas diffusion of $SiH_4$ from the ion source to the

138    sample location in the deposition chamber provides the source of the $^{29}Si$ and $^{30}Si$

139    contamination concerning this report.

140        A mass spectrum of the constituents of the ion beam is generated by sweeping the

141    magnetic field of the mass analyzer while monitoring the intensity of the ion beam

142    current at the target. Each of the resulting series of peaks in the current vs. magnetic field

143    signal correspond to different integer mass-to-charge ratios of atomic or molecular ions.

144    In the mass spectrum of SiH$_4$, a series of mass peaks are formed starting at 28 u, which is

145    $^{28}$Si. The adjacent peak at 29 u corresponds to a combination of $^{29}$Si and $^{28}$SiH. We

146    calculate the intrinsic geometric mass selectivity (i.e. mass resolution) of the ion beam

147    system from the spectrum to estimate the amount of $^{29}$Si potentially contaminating the

148    $^{28}$Si beam. These calculations use Gaussian fits to the mass peaks to determine the

149    overlap of the 29 u peak on the 28 u peak. They give a peak separation of about 11 σ

150    (standard deviations) and a resolving power $m/\Delta m \approx 80$ for $m = 28$ u, which yields a

151    lower bound on the fraction of ions at 28 u consisting of $^{29}$Si of roughly $10^{-25}$, as

152    previously discussed elsewhere[16]. However, this argument neglects gas scattering effects,

153    which would likely be a dominant contributing factor to the contamination compared to

154    this extremely small geometric component. Gas scattering causes an ion at mass 29 u to

155    lose sufficient energy to be incorporated into the 28 u trajectory and pass through the

156    selecting aperture. This scattering tail effect, or abundance selectivity, for a single magnet

157    system can be estimated from literature to contribute $\approx 1 \times 10^{-6}$ of the higher mass peak to

158    the lower mass peak (for a mass of 28 u)[21–23], but it is difficult to measure experimentally

159    in our system. That scattering fraction combined with the $^{29}$Si natural abundance gives an

160    estimate for an upper bound on the $^{29}$Si concentration in the $^{28}$Si beam of roughly $10^{-7}$.

161    This concentration may be significant for the samples measured in this study with the

162    lowest $^{29}$Si isotope fractions approaching $10^{-7}$. However, we do not see any evidence that

163    we are reaching this scattering enrichment limit, e.g. attenuation of the $^{30}$Si isotope

164    fractions compared to $^{29}$Si, discussed further below. For the purposes of this paper, we

165    assume the scattering tail contribution is negligible in these experiments and the ion beam

166    is pure $^{28}$Si. In this study, we consider the difference between the expected (100 %

167    enriched) and measured enrichment by identifying only the natural abundance SiH$_4$ gas

168    diffusing from the ion source into the deposition chamber as the source of $^{29}$Si and $^{30}$Si.

169    ### B.  *Temperature and pressure determinations*

170         In order to extract the temperature dependence of the incorporation fraction, $s$, of

171    $^{29}$SiH$_4$ on $^{28}$Si(100), a good estimate of the SiH$_4$ partial pressure at the sample location

172    during deposition is needed. The base pressure of the deposition chamber was measured

173    to be approximately 1.3 x 10$^{-8}$ Pa (1 x 10$^{-10}$ Torr) for these experiments. During operation

174    of the ion beam, SiH$_4$ is leaked into the ion source at a pressure of about 4 x 10$^{-4}$ Pa (3 x

175    10$^{-6}$ Torr), and some SiH$_4$ gas diffuses into the deposition chamber, which typically sees

176    a factor of 50 to 100 increase from the base pressure. We estimate the partial pressure of

177    SiH$_4$ at the sample from measurements of the individual gas components using a residual

178    gas analyzer (RGA) in the chamber. Typically, while operating the ion beam, the fraction

179    of total pressure increase due to SiH$_4$ and other Si hydrides is estimated to be about 28 %,

180    while the rest is mostly H$_2$. This is because a lot of SiH$_4$ is cracked into SiH$_x$, where SiH$_x$

181    is a combination of Si hydrides ($1 < x < 4$), and thus results in a large amount of

182    byproduct H$_2$. The SiH$_x$ partial pressure is then estimated to vary from 1.4 x 10$^{-7}$ Pa to 9.6

183    x 10$^{-7}$ Pa (1.1 x 10$^{-9}$ Torr to 7.2 x 10$^{-9}$ Torr) across the high temperature samples in this

184    study. The previous room temperature samples were generally deposited in higher partial

185    pressures up to 4.4 x 10$^{-5}$ Pa (3.3 x 10$^{-7}$ Torr) for two samples. From the partial pressures,

186    we get an important quantity in this analysis, the SiH$_x$ molecular gas flux, $F_g$, which is

187    calculated using the estimated partial pressure during deposition and the Hertz-Knudsen

188    equation,

189         $$F_g = p(2\pi m k_B T_g)^{-1/2}, \tag{1}$$

190 where $p$ is the pressure, $m$ is the mass of the gas (SiH$_4$), $k_B$ is Boltzmann's constant, and

191 $T_g$ is the gas temperature (assumed to be 21°C). The pressures for the high temperature

192 samples correspond to $F_g$ gas flux values between 4 x 10$^{11}$ cm$^{-2}$s$^{-1}$ and 3 x 10$^{12}$ cm$^{-2}$s$^{-1}$.

193  The sample temperature during deposition was also carefully measured to ensure

194 an accurate mapping of enrichment vs. temperature and determination of $s$. Temperature

195 was measured in this study using an infrared pyrometer that viewed the sample through a

196 window from outside the vacuum chamber. The temperature readings were calibrated for

197 our system by monitoring eutectic samples in the chamber near their melting temperature

198 and adjusting the pyrometer emissivity to match the known melting point temperatures.

199 The two temperature standards used here were a Au-Si eutectic[24] and an Al-Si eutectic,

200 which were each held at their melting temperatures of 363 °C and 577 °C respectively

201 while calibrating the pyrometer. Multiple calibrations are needed because the emissivity

202 of Si is not constant with temperature. The emissivity as measured through the chamber

203 window changes from about 0.25 at 363 °C up to 0.42 at 577 °C and is expected to reach

204 a high value of 0.68 within the range of temperatures used in this study. This range of

205 values is similar to emissivity values for Si surfaces reported in the literature ($\approx 0.1$ at

206 100 °C and 0.68 at $> 800$ °C)[25]. Including uncertainties in the calibration, the pyrometer

207 temperature readings of the substrate are estimated to have a 5 % relative uncertainty due

208 to fluctuations in the current used for sample heating as well as temperature gradients

209 across the sample.

210 ### *C. Substrate preparation and deposition*

211  $^{28}$Si samples were deposited epitaxially on a variety of natural abundance Si(100)

212 substrates including p-type, n-type, and undoped (intrinsic) wafers that were cleaved into

213    chips measuring 4 mm by 10 mm. Substrates were cleaned *ex situ* using standard Si

214    cleaning procedures for metals and organics used in complementary metal-oxide-

215    semiconductor (CMOS) technology consisting of a piranha etch, hydrofluoric acid (HF)

216    strip, and "standard clean-2" (SC2)[26]. The chips are capped with a thin protective oxide

217    during the final SC2 cleaning step. After cleaning, the chips were immediately mounted

218    onto sample holders and loaded into the vacuum chamber via a load lock. Substrates were

219    then prepared for deposition *in situ* by first degassing them overnight at 600 °C and then

220    flash annealing them to 1200 °C for ≈ 10 s several times. This flash removes the oxide

221    and produces a clean (2x1) reconstructed Si(100) surface on which to deposit $^{28}$Si

222    epitaxially. Typically, flashed substrates were inspected using a UHV scanning tunneling

223    microscope (STM) to ensure a clean surface. The substrate temperature was then elevated

224    to the growth temperature prior to exposure to the ion beam for deposition. To map out

225    the $^{29}$Si temperature dependence, samples were deposited at substrate temperatures

226    ranging from 249 °C up to 812 °C in increments of roughly 100 °C. Also included in this

227    study for qualitative comparison are data from previous amorphous samples deposited at

228    room temperature (≈ 21 °C) on substrates that were only prepared *ex situ* with HF.

229          For the higher temperature samples, $^{28}$Si ions were deposited onto the substrates

230    in the hyperthermal energy regime with an average ion energy at the target of ≈ 40 eV.

231    This energy is selected to stay as high as possible to minimize space charge effects while

232    keeping the net sputter yield ≈ 0. Typical ion beam currents of around 500 nA were

233    achieved over an area on the chip of about 6 mm$^2$, which corresponds to an average ion

234    flux, $F_i$, that varied from 3 x 10$^{13}$ cm$^{-2}$s$^{-1}$ to 3 x 10$^{14}$ cm$^{-2}$s$^{-1}$. $F_i$ was calculated from the

235    film thickness measured *post facto* in combination with the deposition time for each

236     sample. These fluxes correspond to deposition rates between 0.3 nm/min and 3.9 nm/min.

237     The thicknesses of the deposited films were taken from the calibrations of the SIMS

238     depth profiles and ranged from about 50 nm to over 300 nm depending on the sample and

239     the measurement location on the deposition spot.

### 240     *D.   SIMS measurements*

241     Measurements of the enrichment of the $^{28}$Si films grown at different temperatures

242     were made *ex situ* using SIMS. The samples were sputter eroded using an $O_2^+$ primary

243     beam at an impact energy of 8 keV and a current of 1 nA while monitoring counts of $^{28}$Si,

244     $^{29}$Si, and $^{30}$Si to determine their relative abundances. The beam was focused to a probe

245     size of a few micrometers in diameter, and it was raster-scanned over a 50 μm x 50 μm

246     area. The analyzer's magnetic field was cycled to allow the positive secondary ions for

247     each isotope to be detected by a secondary electron multiplier. The mass resolving power

248     for the measurement conditions was m/Δm ≈ 6000 measured at 10 % of the peak

249     maximum. This resolving power is necessary to cleanly separate the $^{29}$Si signal from the

250     $^{28}$SiH signal that arises due to the SIMS process. Under these conditions, we estimate that

251     less than $10^{-5}$ of the $^{28}$SiH signal contributes to the $^{29}$Si measurement. Uncertainties of the

252     isotope ratios were determined from the standard deviation of the mean of the

253     measurements. A profilometer was used to calibrate the depth scale in the measurements,

254     and that allowed for determination of $^{28}$Si film thicknesses and growth rates.

255

## 256     III. ANALYTICAL APPROACH

257     In this study, we evaluate a multi-mechanism gas sticking deposition model to

258     correlate the SIMS measurements of enrichment to the deposition conditions (e.g. SiH$_x$

259     partial pressure and deposition rate) for samples deposited between $\approx$ 21 ℃ and 850 ℃.

260     We consider two distinct sources of Si atoms that contribute to the films. The dominant

261     (high flux) source is the ion beam, assumed to be pure $^{28}$Si as discussed above, and the

262     second is the diffusive partial pressure of SiH$_x$ from the ion source, which contains all

263     three Si isotopes in their natural abundance. The SIMS measurements provide the

264     resultant isotopic concentrations for $^{29}$Si or $^{30}$Si as a fraction of the total Si deposited. The

265     measured isotope fractions of $^{29}$Si and $^{30}$Si are modelled by the mixed ion beam

266     deposition and gas sticking, to provide a combined deposition model, $c_z$ (with $z$ denoted

267     as 29 for $^{29}$Si and 30 for $^{30}$Si), given by:

268     $$c_z = \frac{F_g a_z s}{F_g s + F_i} ,\tag{2}$$

269     where $F_g$ is the SiH$_x$ gas flux, $F_i$ is the $^{28}$Si ion flux, $a_z$ is the natural abundance of $^{29}$Si or

270     $^{30}$Si in the SiH$_4$, and $s$ is an effective incorporation fraction. We simplify $c_z$ by defining

271     the SiH$_4$ flux ratio $d = F_g/F_i$ that correlates the isotope concentrations to deposition

272     conditions:

273     $$c_z = \frac{a_z s d}{1 + s d} ,\tag{3}$$

274     where $c_z$ increases approximately linearly with $d$ in the dilute regime ($d \ll 1$) where

275     most experiments were performed. Additionally, when $F_g \gg F_i$ (never true in our

276     experiments), then the natural abundance source dominates and $c_z \rightarrow a_z$, the natural

277     abundance ratio. To add statistical weight and simultaneously consider the $^{29}$Si and $^{30}$Si

278     data, we generalize the isotope specific model of Eq. (3) by dividing it by each isotope's

279     natural abundance so that $^{29}$Si and $^{30}$Si data can be fit together within the same model.

280     This has the effect of changing the units from an isotope specific incorporation to total

281     (all isotopes) adsorbed SiH$_4$, which gives a total gas sticking deposition model, $c_{tot.}$,

282     where

283            $$c_{tot.} = \frac{c_z}{a_z} = \frac{sd}{1 + sd}.$$          (4)

284     Eq. (4) allows us to determine the incorporation fraction $s$ for each sample deposited at

285     different temperatures, to get the trend of $s$ vs. $T$. Additionally, since $s$ represents the

286     fraction of diffusing SiH$_4$ gas that become permanently incorporated in the film, at the

287     single molecule level, $s$ is the probability that a specific molecule becomes incorporated

288     on the timescale of an arriving ion.

289          To describe the anticipated phenomenological behavior of $s$ vs. $T$, we define a

290     temperature dependent incorporation model, $s(T)$, that considers two classical gas

291     incorporation mechanisms: a sticking term (physisorption), $s_p$, and a higher temperature

292     reactive mechanism, $s_c$, (e.g., hydrogen cracking or chemisorption). Both $s_c$ and $s_p$ are

293     expected to be thermally activated, where $s_p$ decreases with increasing temperature as

294     more molecules escape (desorb), and $s_c$ increases with increasing temperature as more

295     molecules react and bond to the surface. Since $c_{tot.}$ is normalized by the total flux, $s(T)$

296     is the probability per molecule that SiH$_4$ is incorporated. We define these individual

297     components to be:

298          $$s_p = 1 - A_p \exp\left(-E_p/k_B T\right) \quad \text{and} \quad s_c = A_c \exp(-E_c/k_B T),$$      (5)

299     where $E_p$ is the activation energy for "physisorption," $E_c$ is the activation energy for

300     "chemisorption," $k_B$ is the Boltzmann constant, and $T$ is the substrate temperature during

301     deposition. The prefactors $A_p$ and $A_c$ are free parameters that account for the average site

302     occupancy and the time integral over many activation attempts that occur at molecular

303 vibrational frequencies and other atomistic factors. From this, the total incorporation

304 fraction at a given temperature is the sum of the two sticking components,

305 $$s(T) = s_p + s_c + s_0 = 1 - A_p \exp(-E_p/k_B T) + A_c \exp(-E_c/k_B T) + s_0. \qquad (6)$$

306 An $s_0$ term accounts for temperature independent incorporation, like activation from a

307 collision with an ion in the depositing flux. The simple sum assumes that the two

308 mechanisms are independent, e.g., physisorption is not a requirement for chemisorption,

309 and that $E_c \gg E_p$ such that $s(T) \leq 1$ for all $T$.

## IV. RESULTS AND DISCUSSION

### A.  $^{28}$Si enrichment and pressure correlation

312    For all deposition temperatures (except room temperature and 249 °C), epitaxial

313 growth of the $^{28}$Si films was achieved. Interface widths of a few nanometers were found

314 for samples grown between roughly 350 °C and 420 °C, while the surface roughness

315 increased significantly for higher temperature samples. The sample with the best

316 enrichment and lowest $^{29}$Si isotope fractions in this study was deposited at 502 °C. A

317 SIMS depth profile of the isotope fractions ($^z$Si/Si$_{tot.}$) for this sample is shown in Fig. 1.

318 Between 40 nm and 280 nm into the film, the averaged isotope fractions are; $^{28}$Si:

319 99.9999819(35) %, $^{29}$Si: 1.27(29) x 10$^{-7}$, and $^{30}$Si: 5.5(19) x 10$^{-8}$. The average values for

320 $^{29}$Si and $^{30}$Si are represented by dashed lines in Fig. 1 and fall below the data because of

321 many zero counts on the SIMS detector for those measurement cycles. At a depth of

322 around 300 nm in this sample, the sputter beam erodes into the substrate and the isotope

323 fractions return to the natural values.

324
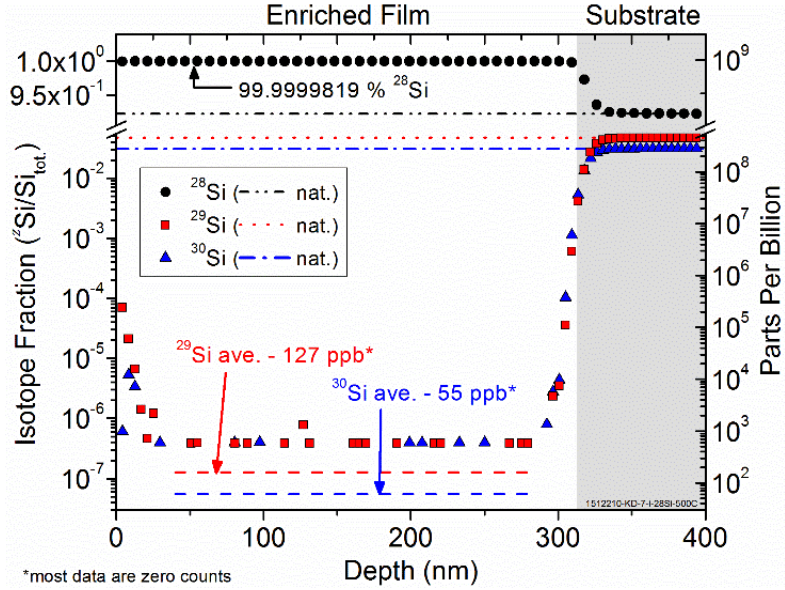
FIG. 1. (Color online) Semi-log SIMS depth profile of the 502 °C sample showing the isotope fractions of $^{28}$Si (circles), $^{29}$Si (squares), and $^{30}$Si (triangles). The sharp increase in $^{29}$Si and $^{30}$Si isotope fractions to the natural abundance levels (dotted lines) at 300 nm corresponds to reaching the substrate (gray shade). The average isotope fractions (from 40 nm to 280 nm) are shown as dashed lines. These averages lie below the visible data because many of the data were zero counts.

Temperature is not the only significant experimental parameter affecting enrichment; the enrichment is also seen to depend linearly on the SiH$_x$ partial pressure (when $F_g \ll F_i$). We plot the raw SIMS data for the room temperature samples as a function of the SiH$_4$ flux ratio, $d = F_g/F_i$, in Fig. 2, with $^{29}$Si (squares) and $^{30}$Si (triangles) isotope fractions plotted together. The top axis of Fig. 2 shows the total gas flux ratio, $F_g^{tot.}/F_i$, using the total measured pressure increase during deposition without subtracting out the estimated H$_2$ fraction in the gas. The hydrogen subtraction only shifts

15

339
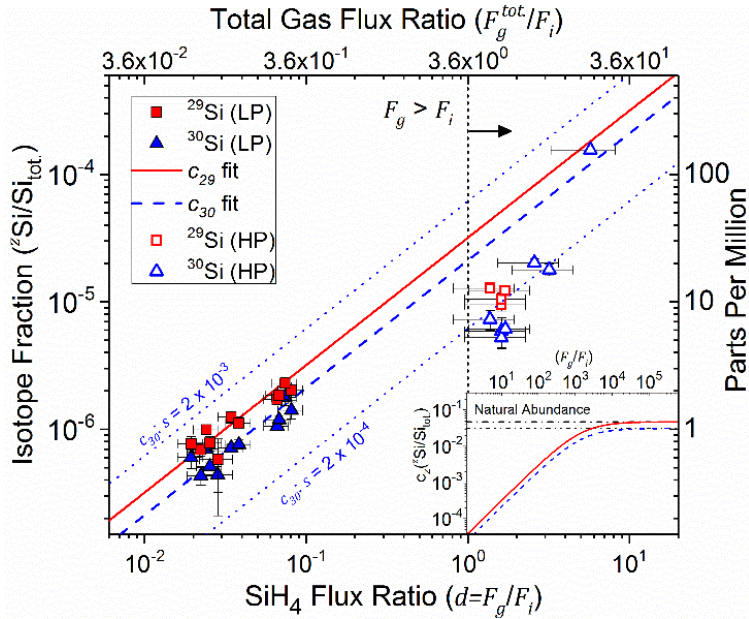
FIG. 2. (Color online) Correlation plot of isotope fractions ($^z$Si/Si$_{tot.}$) from SIMS vs. SiH$_4$ flux ratio $d = F_g/F_i$ shown on a log-log scale for samples deposited at room temperature ($\approx 21$ °C); $^{29}$Si (squares) and $^{30}$Si (triangles). The top axis is the flux ratio for the total gas flux during deposition. The gas sticking deposition model, $c_z$ is fit to the $^{29}$Si and $^{30}$Si data (solid and dashed line respectively) and gives a value of $s = 6.8(3) \times 10^{-4}$. $c_z$ is linearly proportional to $s$ over the range of the data, but asymptotes (see inset) to the natural abundance values when $F_g \gg F_i$ (dash-dotted lines). To demonstrate the sensitivity to changes in the free parameter $s$, $c_{30}$ for two other values of $s$ (blue dotted lines) are also shown. "LP" and "HP" denote data from two different experimental configurations, only the "LP" data is used for quantitative analysis. Horizontal error bars are dominated by the uncertainty in the pressure measurements, and vertical error bars represent the standard deviation of the SIMS data.

the axis laterally and both the $^{29}$Si and $^{30}$Si isotope fractions have a strong linear

correlation with the SiH$_4$ flux fraction (deposition conditions), showing that a higher SiH$_4$

flux fraction produces a larger isotope fraction in the sample. This high correlation is

strong evidence that the diffusive SiH$_x$ is the primary source of the minor isotopes.

16

357        To determine the probability of $SiH_x$ being incorporated during growth, we fit the

358    data in Fig. 2 using Eq. (3) to get $c_{29}$ and $c_{30}$ with $s$ as the only free parameter. These fits

359    are shown in Fig. 2 as solid and dashed lines respectively. They are approximately linear

360    over the range of the data with a slope proportional to $s$. For $d > 10^4$, $c_z$ asymptotes to

361    the natural abundance values (see Fig. 2 inset) of 4.7 % for $^{29}Si$ and 3.1 % for $^{30}Si$. The

362    best fit to the data yields a room temperature incorporation fraction of $s = 6.8(3)$ x $10^{-4}$.

363    The points at $d > 1$ were deposited in a different vacuum chamber with poorer pressure

364    measurement but are included to show continuation of the qualitative trend to much

365    higher pressures. Only the "LP" data is used for quantitative analysis at room temperature

366    and this configuration was used for all the higher temperature work. $c_{30}(d)$ is plotted for

367    two other values of $s$ which span an order of magnitude around the fit value so that the

368    reader can see the sensitivity of the fit to $s$. Note that when viewed as a log-log plot as in

369    Fig. 2, $c_z$ does not change slope as $s$ is varied, it only changes vertical offset.

370        Affirmation that the diffusive $SiH_4$ partial pressure is the dominant source of the

371    minor isotopes is found in the measured isotope ratios $^{29}Si/^{30}Si$ for each sample, shown in

372    Fig. 3. If the minor isotope contribution originated from the ion beam, $^{30}Si$ would be

373    attenuated compared to $^{29}Si$ and increase the $^{29}Si/^{30}Si$ ratio above the natural value, e.g.

374    datum 31. Instead, the measured isotope ratios for most samples are very close to the

375    natural value of about 1.5, indicating that the source of $^{29}Si$ and $^{30}Si$ has a natural

376    abundance of Si isotopes, e.g., the $SiH_4$ source gas.
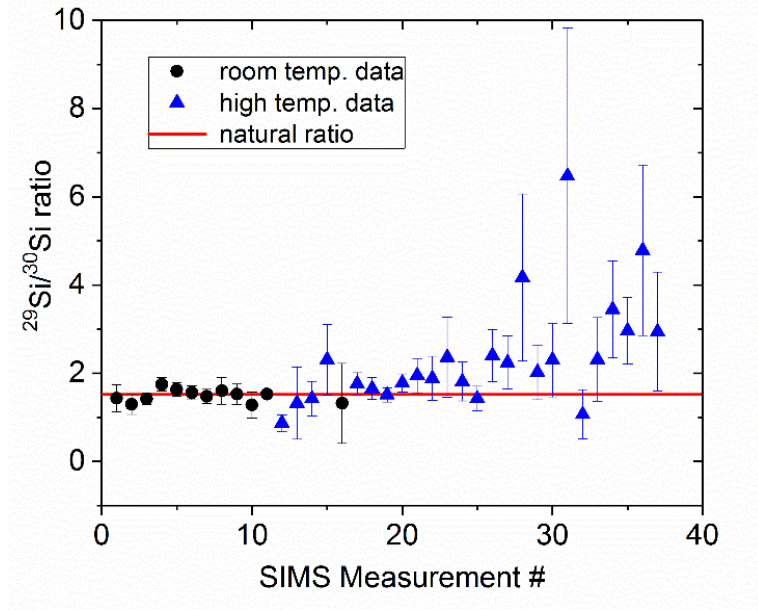
FIG. 3. (Color online) $^{29}$Si/$^{30}$Si isotope ratios for samples deposited at room temperature
(circles) and elevated temperatures (triangles). The ratios of these samples agree with the
natural abundance ratio of 1.5 (line) indicating that the source of $^{29}$Si and $^{30}$Si is naturally
abundant, probably the SiH$_4$ gas. Measurement numbers 28, 31, and 36, which lie above
a $^{29}$Si/$^{30}$Si ratio of four, suffer from discrete counting noise in the SIMS measurements
due to a total $^{30}$Si count < 10, which makes the ratio highly volatile. Error bars are
derived from the standard deviation of the SIMS data.

## B.   Temperature dependence of $^{29}$Si and s

Isotope fractions were measured by SIMS on samples grown at many different
temperatures. For each SIMS measurement at each temperature, an average isotope
fraction is found in the depth region where the minor isotope counts reach a minimum.
The SIMS measurements from $^{28}$Si samples grown at the low end of the epitaxial
temperature range (249 °C) had a residual $^{29}$Si isotope fraction of 7.9(12) x 10$^{-7}$. The
sample grown at the highest temperature, 812 °C, has a $^{29}$Si isotope fraction of 4.32(46) x

18

394    $10^{-6}$. This factor of five increase in isotope fraction is the focus of our analysis and

395    discussion. We note that for the samples deposited at 705 °C, 708 °C, and 812 °C,

396    significant morphological roughness may have resulted in some substrate mixing during

397    the SIMS measurement. Therefore, these data are an upper bound since the SIMS may

398    not have reached the minimum isotope fraction before breaking into the substrate. In this

399    report, we excluded data that were clearly influenced by this effect (did not reach a stable

400    isotope fraction minima), however, it is possible that this measurement artifact still

401    weakly contributed to the measured values of the isotope ratios reported here for the

402    highest temperature samples.

403        In this work, we primarily report the dependence of the $^{29}$Si and $^{30}$Si incorporation

404    from the SiH$_4$ partial pressure on the different substrate temperatures. The raw $^{29}$Si

405    isotope fraction increases rapidly in the range from 502 °C (1.27 x $10^{-7}$) to 812 °C (4.32 x

406    $10^{-6}$), however, maintaining an identical SiH$_4$ partial pressure and ion beam flux was not

407    possible for each sample. Using the $c_z$ function though, we can adjust the isotope fraction

408    values at each temperature for the variations in deposition parameters. To do this, the raw

409    SIMS measurements are adjusted to a common SiH$_4$ flux ratio $d = F_g/F_i$. We choose the

410    $d$ value corresponding to an area of the sample deposited at 502 °C, i.e., the lowest

411    measured isotope fractions of $^{29}$Si and $^{30}$Si.

412        The procedure for the adjustment is as follows: multiple values of the isotope

413    fractions are determined from SIMS plots at each temperature, e.g., Fig 1. Each SIMS

414    value is adjusted by solving Eq. (3) using the corresponding $d$ value to determine $s$ for

415    each datum independently, denoted as $s_T^n$, where $n$ is the $n$th datum measured for a

416    sample deposited at temperature $T$. Then, using the specific $s_T^n$ value put back into Eq

417    (3), we can adjust the isotope ratio to the $d$ value of the 502 °C sample ($d_{502} = 0.0073$)

418    and denote the adjusted value as $c_z(s_T^n, d_{502})$.

419        In Fig. 4, the isotope fractions adjusted for pressure and ion beam flux (deposition

420    rate) are plotted as a function of temperature to isolate the enrichment's temperature

421    dependence. The $^{29}$Si adjusted isotope fractions appear to initially trend downwards from

422    $\approx 7.9 \times 10^{-7}$ at 249 °C to a minimum at the 502 °C average of about $1.3 \times 10^{-7}$. The room

423    temperature data appears to deviate from the low temperature trend, which is likely

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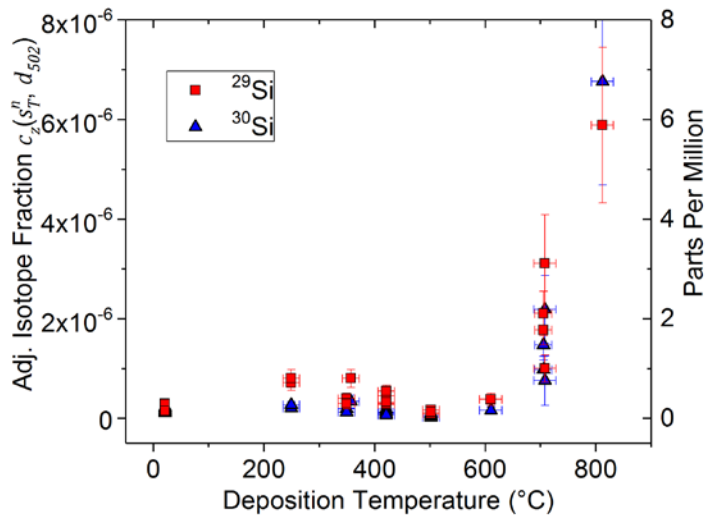


425

426    FIG. 4. (Color online) Adjusted isotope fraction, $c_z(s_T^n, d_{502})$, vs. temperature for $^{29}$Si

427    (squares) and $^{30}$Si (triangles). The raw isotope fractions are adjusted to the deposition

428    conditions ($F_g$ and $F_i$) of the 502 °C sample to account for differences in pressure and

429    deposition rate among different samples. This shows the expected increase in isotope

430    fraction at a given temperature for a sample deposited under the same conditions as the

431    502 °C sample. Horizontal error bars are due to uncertainty in the pyrometer calibration

432    and temperature fluctuation during deposition, and vertical error bars represent the

433    standard deviation of the SIMS data.

434    due to unaccounted for systematic variations, e.g., because those samples were

435    amorphous and were grown in a different experimental configuration. Surface orientation

436    and crystallinity are known to affect the adsorption of $SiH_4$ on Si surfaces[27], which may

437    lead to a lower effective sticking coefficient compared to that of the crystalline samples.

438    Above 502 °C, the adjusted $^{29}$Si isotope fraction sharply increases up to 5.9 x $10^{-6}$ at 812

439    °C. This increase is emblematic of the thermal activation of a chemical process, perhaps

440    similar to a CVD reaction, and appears to dominate over the incorporation mechanism at

441    lower temperatures.

442          We can analyze these mechanisms better by evaluating the values of $s$ at each

443    temperature and comparing them to the temperature dependent incorporation model. The

444    measured isotope fractions are first converted to isotope independent $SiH_4$ fractions using

445    their natural abundance values according to the generalization to obtain Eq. (4) for the

446    total gas sticking deposition model, $c_{tot.}$. The generalized $^{29}$Si and $^{30}$Si data $(^z$Si/Si$_{tot.})/a_z$

447    for each deposition temperature are then plotted together in Fig. 5 against their $SiH_4$ flux

448    ratios and fit together using $c_{tot.}$ to get a single $s_T$ value for each temperature.

449          The values of $s$ determined from data (slopes of the lines in Fig. 5) are shown in

450    Fig. 6. These incorporation fractions are a total net sticking probability; i.e., the

451    probability that a $SiH_x$ molecule that struck the surface was permanently incorporated

452    into the film. The dependence of $s$ on temperature closely follows the trend of the $^{29}$Si

453    and $^{30}$Si isotope fractions in Fig. 4. In the lower temperature regime, $s$ trends downwards

454    slightly from a value of 1.6(2) x $10^{-3}$ at 249 °C to a minimum of 2.9(4) x $10^{-4}$ at 502 °C.

455    In this temperature range, the decrease of $s$ suggests reduced incorporation due to

456    increasing thermally activated escape from physisorption $(s_p)$. The room temperature

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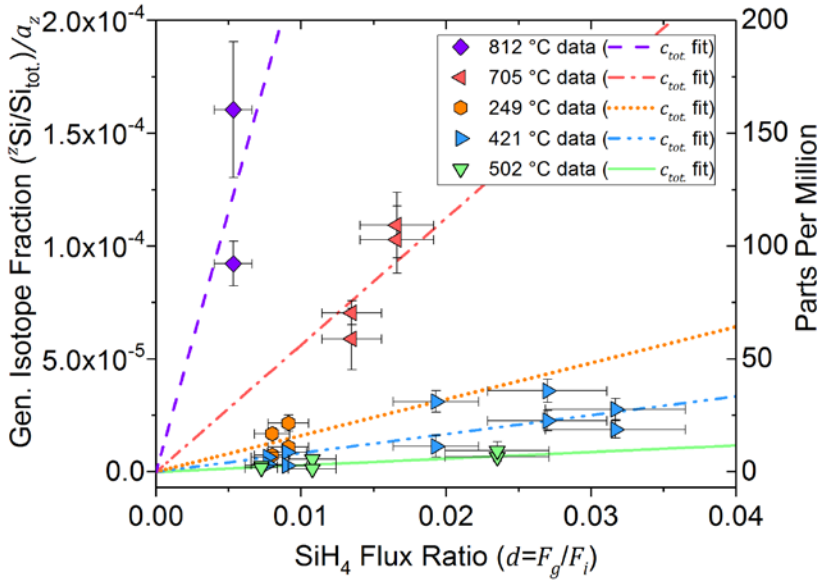
FIG. 5. (Color online) Correlation plots of the generalized isotope fractions $(^zSi/Si_{tot.})/a_z$ vs. $SiH_4$ flux ratio shown on a linear scale for samples deposited at several elevated temperatures. The raw SIMS isotope fractions for $^{29}Si$ and $^{30}Si$ are each generalized using their natural abundance, $a_z$, to get the estimated total adsorbed $SiH_4$. Then $c_{tot}$ is fit to the data for each temperature (solid, dashed, dotted lines) to determine $s_T$. The fits originate at the point $(0, 0)$ because zero $SiH_4$ flux results in an adsorbed $SiH_4$ fraction of zero. Horizontal error bars are dominated by the uncertainty in the pressure measurements, and vertical error bars are derived from the standard deviation of the SIMS data.

datum is excluded since the amorphous nature of the sample will not have the same adsorption kinetics. Then as $T$ is increased above 600 °C, $s$ rapidly increases to 2.3(5) x $10^{-2}$ at 812 °C. This increase suggests thermal activation of the reactive sticking coefficient, i.e., chemisorption, $s_c$, which increases with increasing temperature. These values of $s$ are consistent with previously reported values of the reactive sticking coefficient of silanes on Si surfaces, although there is a large variation in the literature, e.g., Si CVD studies have shown the reactive sticking coefficient, $s_r$, to range from 5 x
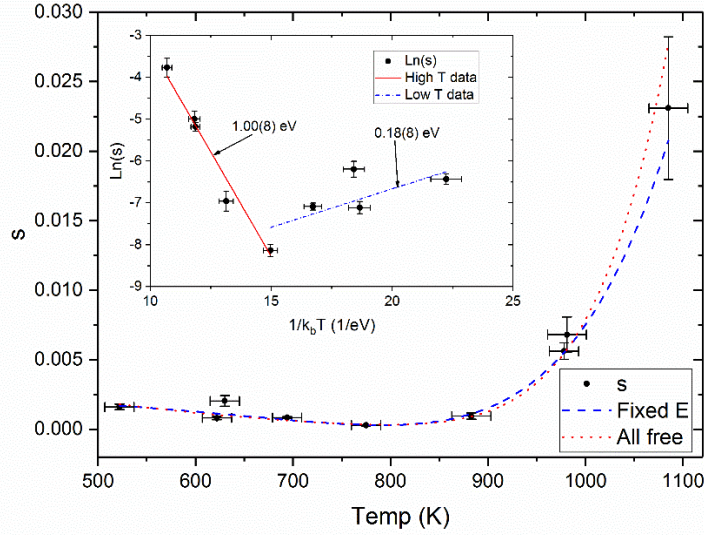
FIG. 6. (Color online) Incorporation fraction, $s$ (circles) vs. deposition temperature. $s$ is determined from the fits of $c_{tot.}$ to the data for each temperature in Fig 5. The fit to Eq. (6) is shown in the red dotted line with all parameters free. The inset presents the same data in Arrhenius form, ln(s) vs. $1/k_B T$, with linear fits to the activation energies above and below 502 °C ($1/k_B T \approx 15$ eV$^{-1}$). Using the energies determined in the inset as fixed inputs to Eq. (6), the model is refit and shown as the blue dashed line. Horizontal error bars are due to uncertainty in the pyrometer calibration and temperature fluctuation during deposition, and vertical error bars represent the standard deviation of the fit values of Fig. 5.

$10^{-4}$ to 5 x $10^{-3}$ for polycrystalline Si deposition at 600 °C to 800 °C[28], and from 1 x $10^{-3}$ to 3 x $10^{-5}$ for Si(111) surfaces below 500 °C[29,30].

Next, we fit the data in Fig. 6 using the temperature dependent incorporation model of Eq. (6). This model considers physisorption ($s_p$) with thermally activated escape (desorption), thermally activated incorporation ($s_c$), e.g., due to reaction, as well as temperature independent process like ion activation ($s_0$). The fit to Eq. (6) while leaving all five parameters free is shown as a red dotted line in Fig. 6. Visually, this

23

494     appears to be a good fit, but several aspects of the fit parameters suggest problems, e.g.,

495     the numerical value for $E_p \approx 2 \times 10^{-4}$ eV, $s_0 \ll 0$, and several parameters have a high-

496     degree of cross-correlation, suggesting too many degrees of freedom.

497          In order to break the correlations and isolate $E_p$ and $E_c$, we replot the data of Fig.

498     6 in an Arrhenius form, $\ln(s)$ vs. $1/k_B T$ in the inset of Fig. 6. One can see two regimes

499     of data, corresponding to above and below the 502 °C datum at $1/k_B T \approx 15$ eV$^{-1}$. We

500     approximate each regime as being dominated by a distinct physical mechanism so that

501     each segment individually can be fit to a line $\ln(s) = \ln(A) - E(1/k_B T)$ where the

502     slope is the effective activation energy in that regime. The fit line for the higher

503     temperature data is shown as a solid red line with a slope of 1.00 eV $\pm$ 0.08 eV while the

504     fit to the lower temperature data is shown in a dash-dotted blue line with a slope of 0.18

505     eV $\pm$ 0.08 eV and has R$^2$ values of 0.98 and 0.61, respectively. The higher temperature

506     value of 1.00 eV is consistent with reported activation energies for SiH$_4$ CVD between

507     600 °C and 800 °C. The literature values are found to vary between about 0.4 eV to 2.2

508     eV depending heavily on experimental conditions such as surface orientation, gas

509     pressure, and hydride species[27–29,31–34].

510          Using the energy values determined from the slopes in the Arrhenius fits, we can

511     input these as known values back into Eq. (6) supposing that they correspond to the

512     energies in that model and perform the fit with fewer degrees of freedom. A plot of this

513     fit is shown as a blue dashed line in Fig. 6. The best fit values are $s_0 = -0.9977(3)$,

514     $A_p = 0.035(6)$, $A_c = 1023(141)$ with some correlation remaining between $s_0$ and $A_p$,

515     but the fit yields reasonable relative errors and a $R^2 = 0.91$.

516    Examining the values of the best fit parameters yield some physical insights. First,

517    if we consider the zero-temperature limit (albeit a substantial extrapolation), then

518    $s(T \to 0) = s_0 + 1 = 0.0023(6)$, as opposed to our initial assumption that $s(T \to 0) =$

519    1 and $s_0 \geq 0$, i.e. all the SiH$_4$ would be incorporated in the zero-temperature limit. The

520    implication of needing $s_0 < 0$ to fit the data is that this initial assumption is incorrect,

521    and that adsorbing SiH$_4$ is not guaranteed to be incorporated. Rather, under these

522    conditions, only $\approx 1/400$ adsorbed molecules would become incorporated. Ultimately,

523    another mechanism (besides adsorption) must be acting as a gateway to incorporation,

524    accounting for the $s_0 + 1$ terms discussed above. We then look to possible temperature

525    *independent* activation processes that can lead to incorporation, the most obvious being a

526    collision from the ion beam. Focusing on the low temperature regime where we neglect

527    ($s_c$), we can write a differential equation (below the activation of $s_c$) where

528    $$\frac{dn_s}{dt} = (1 - n_s)F_g - n_s \nu \exp\left(-\frac{E_p}{k_B T}\right) - p\, n_s\, F_i \,, \qquad (7)$$

529    with $n_s$ being the probability a surface site is occupied, $\nu$ is the molecular vibration

530    frequency and $p$ corresponds to the probability that an ion collision results in the

531    incorporation of a SiH$_4$ molecule. The first term is the source term from the gas flux,

532    which becomes diminished if a substantial portion of the surface is covered by SiH$_4$; the

533    second term is thermally activated desorption (similar to $s_p$ but without the implicit

534    integral over the gas flux rate) and the last term represents collisional activation from the

535    ion beam. We set this equation to zero (corresponding to the steady state condition during

536    growth) and then look at the zero temperature limit for the conditions corresponding to

537    $d_{502}$ at each atomic site ($F_g = 0.0013$ s$^{-1}$, $F_i = 0.179$ s$^{-1}$) and with $p = 1$. We find a

538   steady state occupation probability $n_s = \frac{F_g}{pF_i + F_g} = 0.0072$, and assuming all other sites

539   would become occupied by $^{28}$Si from the ion beam, then $c_{tot.} = n_s$. Considering the

540   isotopic abundance $a_{29} = 0.047$, then the probability that a surface site is occupied by a

541   $^{29}$SiH$_4$ is $n_{s-29} = 3.4$ x $10^{-4}$, and the corresponding $^{29}$Si isotope ratio would also be

542   3.4 x $10^{-4}$. By comparison, using the alternate $T = 0$ limit from the fit of Eq. (6) above

543   for $s(T \rightarrow 0) = 0.0023$, and using $d_{502} = \frac{F_g}{F_i} = 0.0073$ we can extrapolate that the zero

544   temperature concentration of silicon from the gas $c_{tot.}(\text{fit}) \approx d_{502} \cdot s(T \rightarrow 0) = 1.7$ x

545   $10^{-5}$and the $^{29}$Si isotope fraction would be 0.8 x $10^{-6}$. These two zero temperature limits

546   can be reconciled if we calculate $c_{tot.} = n_s \cdot p$ and drop the assumption of $p = 1$, where

547   we use $c_{tot.} = 1.7$ x $10^{-5}$ from the fit of Eq. (6) and $n_s = 0.0072$ following Eq. (7)

548   above. From this, we find the implied ion collision activation probability $p = 0.0023$,

549   which is numerically equal to the $s(T \rightarrow 0)$. Considering the value $p = 0.0023$, an

550   activation probability of 1 in 400 is plausible (although probably low) for a 40 eV ion at

551   normal incidence, but considering the uncertainties present and the extreme extrapolation

552   to well below the limits of the data, this value should not be taken too seriously.

553       We do feel that the data provide good evidence for 1) a thermally activated

554   incorporation mechanism with an activation energy of 1.00(8) eV, probably

555   corresponding to breaking an H bond; 2) a temperature-independent activation

556   mechanism proportional to the surface population, probably ion collisional activation;

557   and 3) a diminishing surface population due to thermal desorption that reduces the

558   absolute incorporation from (2).

559

## V. SUMMARY AND CONCLUSIONS

We analyzed the measured enrichment from SIMS (i.e. residual $^{29}$Si and $^{30}$Si isotope fractions) of samples deposited at temperatures ranging from 249 °C to 812 °C to understand how enrichment changes as a function of temperature due to SiH$_4$ incorporation. From this analysis, we determined the temperature dependence of the incorporation fraction, $s$, and modeled it using two sticking terms. The lowest $^{29}$Si isotopic concentration was found for deposition at 502 °C at 1.27(29) x 10$^{-7}$. A reactive incorporation mechanism due to CVD-like chemisorption is observed and increases minor isotope concentration between 502 °C up to 812 °C. While we achieve epitaxial growth for all samples deposited above 249 °C, the temperature range above 502 °C coincides with increased film roughness and crystalline defect formation, although several mechanisms are believed to contribute to this behavior. In this work, the optimal deposition temperature for minimizing the $^{29}$Si isotopic concentration is found to be $\approx$ 500 °C, however, we consistently use 450 °C to produce high quality, smooth epitaxial films with reduced risk of chemical contamination and expect to suffer little or no decrease in enrichment.

We find an activation energy for this reactive incorporation of $E_c = 1.00(8)$ eV. Below the activation of the reactive process, the data suggest that incorporation directly from adsorption is rare and that a temperature independent mechanism like an ion collision is likely. Understanding the role of SiH$_4$ gas sticking for a range of deposition temperatures is the first step in enabling production of $^{28}$Si samples with targeted levels of enrichment ($^{29}$Si isotope fractions) facilitating a study of T$_2$ coherence times as a function of $^{29}$Si concentration.

## ACKNOWLEDGMENTS

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