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# Application of the Hartmann–Tran profile to analysis of H<sub>2</sub>O spectra



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## ABSTRACT

The Hartmann-Tran profile (HTP), which has been recently recommended as a new standard in spectroscopic databases, is used to analyze spectra of several lines of H<sub>2</sub>O diluted in N<sub>2</sub>, SF<sub>6</sub>, and in pure H<sub>2</sub>O. This profile accounts for various mechanisms affecting the line-shape and can be easily computed in terms of combinations of the complex Voigt profile. A multi-spectrum fitting procedure is implemented to simultaneously analyze spectra of H<sub>2</sub>O transitions acquired at different pressures. Multi-spectrum fitting of the HTP to a theoretical model confirms that this profile provides an accurate description of H<sub>2</sub>O line-shapes in terms of residuals and accuracy of fitted parameters. This profile and its limiting cases are also fit to measured spectra for three H<sub>2</sub>O lines in different vibrational bands. The results show that it is possible to obtain accurate HTP line-shape parameters when measured spectra have a sufficiently high signal-to-noise ratio and span a broad range of collisional-to-Doppler line widths. Systematic errors in the line area and differences in retrieved line-shape parameters caused by the overly simplistic line-shape models are quantified. Also limitations of the quadratic speed-dependence model used in the HTP are demonstrated in the case of an SF<sub>6</sub> broadened H<sub>2</sub>O line, which leads to a strongly asymmetric line-shape.

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## 1. Introduction

In recent papers [1–4] the partially Correlated quadratic-Speed-Dependent Hard-Collision profile (pCqSDHCP) was proposed as a standard model for isolated line-shapes to go beyond the widely used Voigt profile in spectroscopic databases and radiative transfer calculations. This profile is a version of the correlated speed-dependent Rautian profile of Pine [5] with the speed-dependence of collisional width

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http://dx.doi.org/10.1016/j.jqsrt.2015.06.012 0022-4073/© 2015 Elsevier Ltd. All rights reserved. and shift given in the quadratic form proposed by Rohart et al. [6,7]. The pCqSDHCP, which is also widely known as the partially Correlated quadratic-Speed-Dependent Nelkin– Ghatak profile (pCqSDNGP), was recently recommended in Ref. [8] as a standard profile, where it was proposed to be called the Hartmann–Tran profile (HTP). Indeed, the Voigt profile does not allow us to fully exploit tremendous advances in spectroscopic instrumentation [9–11] and it cannot fulfill the increasingly demanding precision requirements in Earth observation missions (e.g. [12–15]). Several non-Voigt effects on the line-shape must be taken into account in order to accurately describe the measured spectra. In [1], we have shown that the HTP can reproduce the spectral line shapes of different molecular systems within a few parts-per-thousand at atmospheric pressure conditions (from low pressure up to 1 atm). This profile accounts for various non-Voigt effects on the spectral shape through wellidentified line-by-line parameters: velocity changes due to collisions (i.e. the Dicke narrowing effect), speed dependencies of the broadening and shifting parameters and correlation between velocity and internal-state changes. Recently the HTP was fit to high signal-to-noise ratio spectra of CO<sub>2</sub> [16] and H<sub>2</sub>O [17], which illustrated the utility of the HTP and showed the importance of non-Voigt mechanisms on lineshape. Importantly, we have shown that this profile can be written as combinations of the complex Voigt function and hence can be quickly and easily computed. Its use is thus compatible with the analysis of laboratory measurements and atmospheric spectra.

In the remainder of this paper, we quantify the extent to which the HTP can model self- and foreign-broadened water vapor line shapes for various ranges of pressure and spectrum signal-to-noise ratios. To this end, we fit the HTP and other parameterized line-shape models to theoretically calculated (see [1]) and measured water vapor spectra using a multi-spectrum fitting technique, and we quantify fit residuals and systematic differences in retrieved line parameters. Measurements are based on two sets of cavity ring-down spectroscopy (CRDS) spectra for transitions in the  $2\nu_1 + \nu_3$  and  $4\nu_2$  bands near 10,687 cm<sup>-1</sup> and 6245 cm<sup>-1</sup>, respectively, and on difference frequency generation (DFG) absorption spectra for a transition in the  $\nu_3$  band near 3838 cm<sup>-1</sup>. Perturbers considered include N<sub>2</sub>, SF<sub>6</sub> and H<sub>2</sub>O. These results allow us to evaluate the systematic errors resulting from the use of simplified line-shape models. A similar study of O<sub>2</sub> was also recently done by comparing ab initio line shape calculations with a variety of semiclassical models [18].

## 2. Data used and analysis procedure

In order to quantify how the quality-of-fit (QF) [9,16] and biases in fitted line-shape parameters depend on the choice of line profile, spectra need to span a wide range of pressures and have a sufficiently high signal-to-noise ratio (SNR). This is because at a given pressure, there can be numerical correlations between parameters that result in similar changes to the line-shape. For example, the effects of velocity-changing collisions and speed-dependence of the collisional width both lead to reduction in line width. However these two line-narrowing mechanisms affect the Doppler and collisional components of the line shape, respectively, and therefore they can be distinguished by simultaneously fitting a properly constrained line profile to spectra acquired over pressures covering both the Doppler- and collisional-dominated domains.

First, the analysis of simulated spectra of the  $4_{04} - 3_{03}$  line from the  $\nu_3$  band of H<sub>2</sub>O perturbed by N<sub>2</sub> (see Ref. [1]) was extended to several commonly used semiclassical line shapes. These simulated spectra were analyzed by multispectrum fits for a wide range of the Lorentz-to-Doppler width ratio ( $\Gamma/\Gamma_D$ ) and resulted in conclusions which were verified by subsequent analysis of the measured spectra. In this case, the simulated spectra have  $\Gamma/\Gamma_D$  between 0.17 and 19.7, which corresponds to pressures from 9 hPa to 1040 hPa. Recall that these theoretical line-shape simulations were done with the Keilson–Storer model of velocity changes and semi-classical calculations of the speed-dependent line widths and shifts. Details can be found in Ref. [19], where a high level of agreement between these simulated and measured spectra was found.

The results and conclusions obtained from simulated spectra were then verified by fitting line profiles to measured spectra. Specifically, spectra of the  $\nu_3 4_{04} - 3_{03}$  line ( $\nu_0 = 3837.869 \text{ cm}^{-1}$ ) of H<sub>2</sub>O perturbed by N<sub>2</sub> were measured using DFG laser absorption spectroscopy. These data were acquired at 298 K and at 9 pressures between 100 hPa and 1200 hPa [20] leading to collisional-to-Doppler width ratios  $\Gamma/\Gamma_D$  of 1.8–23. The SNR of these experimental spectra is between 600 and 1400.

The second set of measured spectra is of the  $4_{04} - 3_{03}$ line in the  $2\nu_1 + \nu_3$  band ( $\nu_0 = 10,687.326 \text{ cm}^{-1}$ ) of H<sub>2</sub>O perturbed by N<sub>2</sub>. These spectra were measured with the frequency-stabilized cavity ring-down spectroscopy (FS-CRDS) technique at 295.8 K and for 4 pressures between 67 hPa and 533 hPa [21], which leads to  $\Gamma/\Gamma_D$  of 0.45–3.6. For each pressure, two spectra were measured with SNRs between 400 and 720. The third set of spectra considered here were for the same water transition diluted in  $SF_6$  [21]. This relatively heavy perturber (8.11 times the mass of H<sub>2</sub>O) is particularly interesting because the influence of the speed-dependent effects on observed line shape typically increases with perturber-to-absorber mass ratio [22]. In this case, spectra were measured at 295.1 K, at four pressures between 67 hPa and 533 hPa with SNRs between 320 and 710. The ratio  $\Gamma/\Gamma_D$  for these data spans from 0.37 to 2.9.

The fourth set of measured spectra is for the selfbroadened H<sub>2</sub>O 5<sub>14</sub>-5<sub>05</sub> line in the 4 $\nu_2$  vibrational band ( $\nu_0 = 6244.7193 \text{ cm}^{-1}$ ). This line was measured using CRDS at 296 K and for 8 pressures between 1 hPa and 18 hPa [23]. These conditions lead to  $\Gamma/\Gamma_D$  between 0.046 and 0.83. The achieved SNR ranges from 500 near the line peak to over 10,000 in the line wings.

The most commonly used line-shape models: Voigt profile (VP), Galatry profile - GP (also called the softcollision profile), Nelkin-Ghatak profile - NGP, speeddependent Voigt profile - qSDVP, speed-dependent Nelkin-Ghatak profile – qSDNGP, and Hartmann–Tran profile – HTP (which is the partially correlated speed-dependent Nelkin-Ghatak profile – pCqSDNGP) were fit to all simulated and measured spectra. In the last three speed-dependent profiles the quadratic model for the speed-dependence of collisional broadening and shifting [6,7] was applied, as indicated by "q" in the profile acronyms. Additionally, for one data set (line  $4_{04} - 3_{03}$  from the  $2\nu_1 + \nu_3$  band of H<sub>2</sub>O perturbed by SF<sub>6</sub>) profiles using the hypergeometric speed-dependence model [22] were used. These profiles have "h" in their acronyms instead of "q"; namely hSDVP, hSDNGP, pChSDNGP. It should be noted here that the Nelkin-Ghatak profile, based on the hard-collision model of the velocity-changing collisions, is also called hard-collision profile (HCP) and analogous alternative acronyms for the other hard-collision profiles are commonly used, e.g. qSDHCP and pCqSDHCP instead of qSDNGP and pCqSDNGP.

-0.07 0.07

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-0.09 0.09

The multi-spectrum fitting procedure used here differs slightly from that used in Ref. [1]. Here we treat the integrated line areas as free parameters for each pressure. This is because, contrary to the case of simulated spectra, for most of these measured spectra, the relative uncertainty in the partial pressure of H<sub>2</sub>O is significantly greater than the inverse of the SNR. Therefore, constraining line areas to the expected values would lead to systematic distortions of residuals from the fit. The other line-shape parameters are shared for all pressures. The collisional broadening  $\Gamma$  and shifting  $\Delta$ , and frequency of the velocity-changing collisions (which leads to Dickenarrowing and which is called the frequency of optical collisions  $\nu_{opt}$ ) depend on the perturber pressure *p*. This quantity is well-known experimentally and therefore the linear dependencies on pressure of these quantities,  $\Gamma/p$ ,  $\Delta/p$ ,  $\nu_{\rm opt}/p$ , are fitted. The quadratic speed-dependencies of the collisional width  $\Gamma$  and shift  $\Delta$  are described by the dimensionless and pressure-independent parameters,  $a_W$ and  $a_{s}$ , respectively, see e.g. [24]. The relations of these parameters to the speed-dependent collisional width and shift parameters in the notation used in Refs. [1,3,8],  $\Gamma_0$ ,  $\Gamma_2, \Delta_0, \Delta_2$ , are as follows:  $\Gamma = \Gamma_0, \Delta = \Delta_0, a_W = \Gamma_2/\Gamma_0$ , and  $a_5 = \Delta_2/\Delta_0$ . In the case of the hypergeometric speeddependence, the corresponding fitted parameters are  $m_w = (q-3)/(q-1)$  and  $n_s = -3/(q-1)$  for speeddependencies of the width and shift, respectively. They may be interpreted in terms of an exponent q in the absorber-perturber interaction energy which is proportional to the inverse power  $r^{-q}$  of the intermolecular distance *r*. Finally, the parameter*η* describing correlations between velocity- and phase/state changing collisions is pressure independent.

#### 3. **Results and discussion**

## 3.1. Simulated $H_2O \nu_3 4_{04} - 3_{03}$ line

In this section we analyze the influence of the spectra SNR on the ability to obtain non-Voigt line-shape parameters from multi-spectrum fits of the HTP. In Fig. 1 simulated profiles of the H<sub>2</sub>O  $\nu_3 4_{04} - 3_{03}$  line perturbed by N<sub>2</sub> are presented with residuals from multi-spectrum fits for various line-shape models. Although this line was previously analyzed with the VP and HTP in Ref. [1], the present residuals are slightly different because the individual line areas were varied in the fitting procedure, as explained in Section2. The Voigt profile deviates from the simulated one by up to 2% and the HTP only by less than 0.05%. It is also clear that the simulated line shapes can be better reproduced by assigning the non-Voigt effects to speed-dependent effects (qSDVP) rather than collisional narrowing (GP, NGP). Taking both speed dependence and collisional narrowing into account (qSDNGP) does not improve the fit quality compared to the qSDVP, for which residuals are as much as 0.3%. The same set of spectra were then simulated with the addition of Gaussian white noise. The SNR of the simulated spectra was varied from 250 to 8000 by corresponding adjustment of the noise standard deviation. These spectra were fitted with the HTP, as described above for the case without noise. Instead of



-0.2 0.2

Fig. 1. Simulated profiles of  $H_2O \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$  and residuals from multi-spectrum fits with various line-shape models. Spectra correspond to gas pressures: 9, 18, 36, 70, 138, 379, 743, and 1040 hPa

visually comparing residuals from the fits for each SNR it is convenient to define the quality of fit (QF) parameter [9], which is defined as the ratio of the peak absorption to the standard deviation of the fit residuals. In the case of a perfect fit QF should be equal to the SNR. In the multispectrum fit the QF can be calculated for the whole set of pressures [16].

In Fig. 2 the ratios QF/SNR are plotted as a function of SNR for multi-spectrum fits of various profiles. A QF/SNR close to unity corresponds to a nearly perfect fit. The results also depend on the range of the collisional-to-Doppler broadening ratio  $\Gamma/\Gamma_D$  of the simulated spectra. Fig. 2(a) corresponds to fitting spectra for all pressures (9-1040 hPa), with  $\Gamma/\Gamma_D$  varying from 0.17 to 19.7. Fig. 2(b) and (c) corresponds to the collisional regime, with  $\Gamma/\Gamma_D$  > 3.7, and the Doppler regime with  $\Gamma/\Gamma_D$  < 0.35, respectively. Clearly in the case of a broad range of pressures (Fig. 2(a)) the speed-dependent profiles (qSDVP, qSDNGP) which ignore correlations between velocity- and phase-changing collisions begin to deviate from the reference profile at a SNR greater than 500. Profiles which consider velocity-changing collisions, but not the speeddependent effects deviate from the reference data even at SNR equal 250. The HTP is able to reproduce the simulated spectra up to a SNR of 4000. These conclusions are in good agrement with comparison of the maximum deviations of the fit residuals of spectra without noise, shown in Fig. 1 for given profiles.

In the case of the collisional regime (Fig. 2(b)) the HTP yields even better fits to the reference spectra. A decrease of the QF/SNR from unity was only 3.1% for a SNR of 8000, compared to 10.6% for a broad range of  $\Gamma/\Gamma_D$ . Also the two other speed-dependent profiles (qSDVP, qSDNGP) lead to



**Fig. 2.** QF/SNR ratios plotted as a function of SNR for multi-spectrum fits of various profiles to the simulated  $H_2O \nu_3 4_{04} - 3_{03}$  line perturbed by N<sub>2</sub>. Panels (a)–(c) corresponds to various ranges of collisional-to-Doppler width ratios  $\Gamma/\Gamma_D$ .

near-perfect fits for SNRs up to 1000. This can be explained by the weak influence of velocity-changing collisions when the line-shape is dominated by pressure broadening. A different situation can be observed for the low  $\Gamma/\Gamma_D$ range, shown in Fig. 2(c). Here, the velocity-changing collisions are more important than the speed-dependent effects for proper description of the line shape. In this case, the NGP can reproduce the simulated spectra with a SNR up to 1000, and the qSDNGP even up to over 2000. The HTP leads to a near-perfect fit for all SNRs considered here. Interestingly the qSDVP fails at a SNR below 500 and this profile leads to the same fit quality as the GP. It was demonstrated earlier [7,25] that at low pressures these two profiles lead to very similar shapes, even if they describe different physical non-Voigt effects.

We used the fits to simulated, noisy spectra to estimate the uncertainties (both precision and systematic effects) in non-Voigt line-shape parameters which would be determined from fits to real spectra. It is expected that these uncertainties will depend on SNR and various ranges of the collisional-to-Doppler width ratio  $\Gamma/\Gamma_D$ . In Fig. 3 ratios of fitted HTP line-shape parameters for a given SNR to the same parameters obtained from noise-free spectra are



**Fig. 3.** Ratios of fitted line-shape parameters of HTP for a given SNR to the reference parameters vs. the SNR of the fitted spectra. (a) Collisional broadening *Γ*, (b) frequency of optical collisions  $\nu_{opt}$ , (c) quadratic speed-dependence of collisional width  $a_W$ , (d) correlations between velocity-and phase/state changing collisions  $\eta$ . Error bars correspond to the standard uncertainty of the fitted parameter ratios. Red circle plots correspond to multi-spectrum fit of all simulated data, with  $0.17 < \Gamma/\Gamma_D < 19.7$ ; green square plots correspond to the collisional regime ( $\Gamma/\Gamma_D < 0.35$ ). The reference parameters are obtained from spectra without noise for  $0.17 < \Gamma/\Gamma_D < 19.7$ . (For interpretation of the references to color in this figure caption, the reader is referred to the web version of this paper.)

plotted as a function of the SNR of the fitted spectra. Panels (a)–(d) of Fig. 3 present results for the collisional broadening parameter  $\Gamma$ , the frequency of optical collisions  $\nu_{opt}$ , the quadratic speed-dependence of collisional width  $a_{W}$ , and the parameter describing correlations between velocity- and phase/state changing collisions  $\eta$ .

The advantage of using a multi-spectrum fit that simultaneously covers both the Doppler- and collisional regimes is clearly visible in Fig. 3. The standard uncertainties of all parameters are about an order of magnitude smaller than in the case where the fitted data were limited to low or high  $\Gamma/\Gamma_D$  ratios. Also it is worth noting that even for the lowest SNR of 250, for which differences between HTP and two other speed-dependent profiles are barely visible in the fit residuals (see Fig. 2(a)), all of the fitted parameters are consistent within their standard uncertainties with results of the fit to the noise-free spectra.

In the case of data sets that are limited to either high or low pressures, the fitted line-shape parameters are systematically different than those retrieved from spectra spanning a broad pressure range. The magnitude of these differences is parameter dependent and is significantly larger than the standard uncertainty of the fitted parameters for the spectra with SNR above 2000. On the other hand for spectra with the lowest SNR (below 500) the uncertainties of the non-Voigt line shape parameters ( $\nu_{opt}$ ,  $a_W$ ,  $\eta$ ) increase to nearly 100% of their values, making their determination impossible.

It should be noted that the present analysis was made for the case where the number of data points in the spectra was significantly larger than the number of fitted parameters. Obviously, the ability to determine the non-Voigt line-shape parameters is also related to the number of data points. In the case of random Gaussian noise, spectra having *N*-times higher number of uncorrelated data points would be approximately equivalent to increasing the SNR by the factor  $\sqrt{N}$ .

## 3.2. Measured H<sub>2</sub>O spectra

The results of the simulations described above can be compared with the analysis of measured spectra for the same transition. These measured profiles and fit residuals are presented in Fig. 4. The fit residuals from the VP are up to 1.5%, and their distribution with pressure is slightly different than for the simulated spectra. This is likely because of the different pressure ranges and weighting of the spectra caused by different peak absorptions and spectrum point densities. The limited signal-to-noise ratio of these spectra causes the residuals of the three speeddependent profiles to look the same. This is consistent with results of the simulation in Fig. 2(b) for line shapes dominated by collisional broadening and a SNR of about 1000. The observations that the VP leads to up to about 2% disagreement and that the qSDVP fits better than GP and NGP are similar to those obtained from the simulated profiles in Fig. 1.

The QF values presented in Fig. 4 confirm that all three speed-dependent profiles can equally well reproduce the experimental data. We note that one should be careful about comparing the QF values for different data sets, because for an imperfect fit QF depends on the length of the measured line wings.

The next set of experimental data, which corresponds to a line with the same rotational quanta but from a different band  $(2\nu_1 + \nu_3)$ , is shown in Fig. 5. The ratio of collisional-to-Doppler width is much smaller (0.45–3.6) than in the  $\nu_3$  band. The use of the VP leads to about 0.5% of mainly systematic deviations in the fitted spectra,



**Fig. 4.** Measured profiles of the  $H_2O \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$  and residuals from multi-spectrum fits with various line-shape models. Spectra correspond to gas pressures: 99, 197, 294, 398, 499, 600, 797, 1000, and 1200 hPa.



**Fig. 5.** Measured profiles of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$  and residuals from multi-spectrum fits with various line-shape models. Spectra correspond to gas pressures: 67, 133, 267, and 533 hPa.

whereas the GP and NGP reduce this deviation to about 0.1%. All three speed-dependent profiles can reproduce the measured spectra to nearly the experimental noise level, but a small improvement of the fit quality at the lowest pressure is visible for the HTP residuals. A more quantitative analysis using the QF factor confirms this conclusion, which is also consistent with results of simulations in Fig. 2. For the range of pressures that covers both  $\Gamma < \Gamma_D$  and  $\Gamma > \Gamma_D$  the difference between the HTP and the two

other speed-dependent profiles is more visible even at lower SNR (about 500) than in the collisionally dominated region of spectra in Fig. 4 at higher SNR (about 1000).

Another set of experimental spectra considered here is the  $2\nu_1 + \nu_3 4_{04} - 3_{03}$  line of H<sub>2</sub>O perturbed by heavy SF<sub>6</sub> molecules. In this case the relatively large collisional line shifting  $\Delta$  (6.3 times bigger than for perturbation by N<sub>2</sub>) leads to significant line asymmetry caused by the speeddependence of  $\Delta$  [21]. Experimental profiles and multispectrum fit residuals corresponding to various line-shape models are presented in Fig. 6. Line asymmetry is clearly seen by inspection of the residuals from fits of the symmetric profiles VP, GP, NGP, The maximum residual amplitudes of 2.3% for the GP and NGP are only slightly lower than those of the VP. Unlike the other investigated spectra in the case of perturbation by SF<sub>6</sub> the HTP is not able to reproduce the experimental profiles to within the random noise limit. Therefore, in addition to the three profiles (qSDVP, qSDNGP, HTP) which assume quadratic speed-dependence, spectra were fitted with profiles in which the hypergeometric speed-dependent model was applied (hSDVP, hSDNGP, pChSDNGP). The hypergeometric speed-dependence is more physically justified than quadratic model and was previously reported to give better agreement with measured spectra of  $H_2O$  [26]. Also for the case presented in Fig. 6 it is clear that the hypergeometric speed-dependence model can better reproduce the mea-



**Fig. 6.** Measured profiles of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by SF<sub>6</sub> and residuals from multi-spectrum fits with various line-shape models. Spectra correspond to gas pressures: 67, 133, 267, and 533 hPa.

sured spectra than the quadratic model, for which systematic deviations of the residuals are up to about 1%.

The last set of spectra shown in Fig. 7 represents a selfbroadened H<sub>2</sub>O  $4\nu_2 5_{14} - 5_{05}$  line in the case of mostly Doppler-dominated regime ( $\Gamma/\Gamma_D < 0.83$ ). For this data it was not possible to fit the HTP, because the fit residuals were too weakly dependent on the correlation parameter  $\eta$ . Therefore our analysis was limited to the uncorrelated model qSDNGP, which is equivalent to the HTP with  $\eta = 0$ . This observation is consistent with results of simulations for the low-pressure case shown in Fig. 2(c) in which the HTP and qSDNGP lead to equal fit qualities up to a SNR of above 2000.

As was demonstrated earlier, see e.g. [16,21,27,28] subpercent deviations of the fit residuals for various model profiles may be associated with significant differences of fitted line parameters and line intensities. In Fig. 8 ratios of the fitted line areas to the reference (the most accurate) areas are shown as a function of perturber pressure. Graphs (a), (b), (c), (d) and (e) of Fig. 8 correspond to the five data sets presented in Figs. 1, 4, 5, 6 and 7, respectively. The reference line areas are based on the exact simulated area (Fig. 8(a)), fitting with the HTP (Fig. 8(b) and (c)), fitting with the pChSDNGP (Fig. 8(d)) and fitting with the qSDNGP (Fig. 8(e)). Systematic errors of the fitted line areas generally increase with perturber pressure. Using the VP always leads to an underestimation of the area and this effect is up to 6% for data considered here. Also the use of GP and NGP causes underestimation of the line areas in most cases, but the effect is smaller than for the VP. Only for asymmetric line  $2\nu_1 + \nu_3 4_{04} - 3_{03}$  perturbed by  $SF_6$  (Fig. 8(d)) does the GP give surprisingly good line areas which agree to within 0.25% of the reference values. The speed-dependent profiles with the quadratic model, gSDVP, gSDNGP and HTP, overestimate line areas. which is especially visible in Fig. 8(a) and (d) for which the HTP is not a reference. However, systematic error of line area caused by the use of the HTP is smaller than 0.04% for the  $N_2$ -broadened line (Fig. 8(a)) and smaller than 0.5% for the  $SF_6$ -broadened line (Fig. 8(d)). For the self-broadened  $H_2O$  line at low pressures (Fig. 8(e)) all profiles except for the VP, lead to errors in the line area of less than 0.5%.

We note however that the magnitude of systematic error in the line area depends not only on the simplifications inherent in the line-shape model. This error also depends on the pressure range used in the multi-spectrum fit, the distribution of measured spectra within this pressure range, as well as on the length of the line wings measured for each spectrum. For example, as demonstrated in Ref. [29] in the case of the H<sub>2</sub>O  $\nu_1 + \nu_3$  3<sub>22</sub> - 2<sub>21</sub> line perturbed by N<sub>2</sub>, systematic error associated with the use of the VP varies between 2% and 11% depending on the length of the line wings.

Other line-shape parameters may be much more dependent on the fitted profile than the line area. Ratios of the lineshape coefficients to the corresponding coefficients obtained from the reference model HTP are presented in Fig. 9 for the collisional broadening parameter  $\Gamma/p$  (Fig. 9(a)), the frequency of optical collisions  $\nu_{opt}/p$  (Fig. 9(b)) and the collisional shifting parameter  $\Delta/p$  (Fig. 9(c)) for all four data sets considered here. The horizontal axis in Fig. 9 indicates the



**Fig. 7.** Experimental profiles of the self-broadened  $H_2O 4_{\nu_2} 5_{14} - 5_{05}$  line and residuals from multi-spectrum fits with various line-shape models. Spectra correspond to gas pressures: 18.23, 15.87, 13.3, 10.65, 7.99, 5.33, 2.66, and 0.666 hPa.

fitted line-shape model. These results allow us to quantify the systematic error incurred when line-shape parameters obtained from fits of one profile are used to simulate spectra using a different profile. For example if the collisional width  $\Gamma$  obtained from the VP is used with the HTP, it will cause a 3–9% systematic error in the collisional width. The relative differences between the collisional narrowing parameters  $\nu_{\rm opt}$  obtained from various profiles (9(b)) are very large and mainly associated with whether or not speed dependent effects are taken into account. In the case of the speedindependent profiles (GP, NGP) the fitted  $\nu_{opt}$  accounts for both line narrowing mechanisms (the collisional narrowing and speed-dependent effects) and therefore the fitted value is always larger than that obtained from the gSDNGP and hSDNGP. Taking the correlation effect into account (HTP and pChSDNGP) leads to a significant increase in the fitted  $\nu_{opt}$ , compared to those obtained with the qSDNGP and hSDNGP, for all presented cases.

In the case of collisional shifting  $\Delta$  the profiles can be divided to two groups: symmetric profiles (VP, GP, NGP) and asymmetric (all speed-dependent profiles). Both groups lead to systematically different  $\Delta$  values, ranging from 10% to 19%. Even for asymmetric profiles the collisional shift may differ by up to 3% between profiles which use the quadratic and hypergeometric speed dependence model. These systematic errors in the collisional shifting coefficients are crucial to estimating systematic line-shape-induced error in the measurement of unperturbed transition frequency, because this frequency is usually determined from line positions extrapolated to zero pressure.

A complete list of line-shape parameters obtained from the multi-spectrum fits of the HTP to the four data sets studied here is given in Table 1. For the last line  $4\nu_2 5_{14} - 5_{05}$  the parameters of the qSDNGP are reported in Table 1 because it was not possible to fit  $\eta$  from the experimental data. It is worth noting that the fitted collisional narrowing and correlation parameters for the experimental spectra of  $\nu_3 4_{04} - 3_{03}$  line are about half that of the simulated one. This may be associated with the limited signal-to-noise of the measured spectra or the occurrence of asymmetry that cannot be completely described by a quadratic speed dependence of the collisional shift.

## 4. Conclusions

We have measured non-Voigt line-shape effects in near- and mid-IR H<sub>2</sub>O spectra for various physical and experimental conditions, which leads to several general conclusions. The use of the Voigt profile causes several percent deviations in the fit residuals and systematic errors of several percent in the line area. This systematic error typically increases with pressure. Profiles that take into account collision-induced velocity changes effect but not the speed-dependent effects (GP and NGP) usually lead to less than 2% deviations in the fit residuals and line areas. However, for asymmetric lines, like the SF<sub>6</sub> broadened water line presented here where there is a large speeddependent collisional shift, the magnitude of the fit residuals from the symmetric GP or NGP may be similar to that from VP. The speed-dependent profiles with the quadratic model lead to sub-percent deviations in the fit residuals and fitted line areas.

By incorporating both the speed-dependence and collisional narrowing effects simultaneously in the fitted profile, one can further reduce the fit residuals especially at a low range of collisional-to-Doppler line widths ratios  $\Gamma/\Gamma_D$  as shown in Fig. 2c. However, a sufficiently high spectrum signal-to-noise ratio (SNR above 1000) is needed to observe improvement of the fit quality for the qSDNGP, compared to the qSDVP. The use of the HTP reduces the fit



**Fig. 8.** Ratio of the fitted line area to the reference (the most accurate) area vs. perturber pressure, obtained from multi-spectrum fits of (a) simulated spectra of  $H_2O \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$ , the reference areas are exact; (b) measured spectra of  $H_2O \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$ , the reference areas are from the HTP fits (c) measured spectra of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$ , the reference areas are from the HTP fits; (d) measured spectra of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$ , the reference areas are from the HTP fits; (d) measured spectra of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by  $N_2$ , the reference areas are from the HTP fits; (d) measured spectra of  $H_2O 2\nu_1 + \nu_3 4_{04} - 3_{03}$  line perturbed by SF<sub>6</sub>, the reference areas are from the pChSDNGP fits; (e) measured spectra of self-broadened  $H_2O 4\nu_2 5_{14} - 5_{05}$  line, the reference areas are from the qSDNGP fits.

residuals to less than 0.05%. Moreover, multi-spectrum fits of the HTP to measured N<sub>2</sub>-broadened H<sub>2</sub>O lines did not reveal any systematic deviations. The simulations in Fig. 2 suggest that a SNR higher than 4000 and a wide range of  $\Gamma/\Gamma_D$  is needed in the multi-spectrum fit procedure to clearly distinguish between the HTP and measured spectra. On the other hand, the results shown in Fig. 3 suggest that if the pressure range of the measured spectra is sufficient to cover both the Doppler and collisional regimes then all parameters of the HTP can be properly obtained from the multi-spectrum fit even if SNR of spectra is lower than 1000. This is also confirmed by the reasonably low uncertainties of the fitted HTP parameters for the  $2\nu_1 + \nu_3 4_{04} - 3_{03}$  line in Table 1. However, even at very high SNR the fitted parameters  $\nu_{opt}$ ,  $a_W$ , and  $\eta$  of the HTP can be systematically different by even 20% for different ranges of  $\Gamma/\Gamma_D$  ratios in the measured spectra.

For the case of perturbation by heavy  $SF_6$  the quadratic speed-dependence model used in the HTP is clearly not sufficient to properly describe measured spectra at a SNR of about 500. In this case the hypergeometric speed-dependence model leads to significant improvement in the fit quality.

It should be noted here that although the HTP leads to a very good agreement with the calculated  $H_2O$  line



**Fig. 9.** Ratios of the line shape coefficients: (a) collisional broadening parameter  $\Gamma/p$ ; (b) frequency of optical collisions  $\nu_{opt}/p$ ; (c) collisional shifting parameter  $\Delta/p$ , obtained from the multi-spectrum fits of various line shape models, to the corresponding coefficient  $\Gamma_{ref}$ ,  $\nu_{opt_{ref}}$ ,  $\Delta_{ref}$  obtained from the reference model HTP. For the self-broadened H<sub>2</sub>O line the reference model is the qSDNGP. Standard uncertainties of parameters are indicated only if larger than symbols.

## Table 1

Line shape parameters obtained from multi-spectrum fits of the HTP to simulated and experimental H<sub>2</sub>O spectra: collisional broadening parameter  $\Gamma/p$ , collisional narrowing parameter  $\nu_{opt}/p$ , quadratic speed-dependence of collisional broadening  $a_W$  and shifting  $a_S$  parameters, correlation parameter  $\eta$ . The collisional shift coefficients  $\Delta/p$  of  $2\nu_1 + \nu_3 4_{04} - 3_{03}$  line were constrained to previously reported values [21]. Unperturbed transition wavenumbers are from HITRAN [30].  $\Gamma/p$ ,  $\nu_{opt}/p$  and  $\Delta/p$  are in units (kHz/Pa). These values can be converted to more commonly used units using the conversion 1 cm<sup>-1</sup> atm<sup>-1</sup>=295.872 kHz Pa<sup>-1</sup>.

Band and line	$\nu_0  ({ m cm}^{-1})$	Perturber	$\Gamma/p$	$ u_{ m opt}/p$	a <sub>W</sub>	a <sub>s</sub>	η	$\Delta/p$
$\nu_3 \ 4_{04} - 3_{03} \text{ simul.} \\ \nu_3 \ 4_{04} - 3_{03} \\ 2\nu_1 + \nu_3 \ 4_{04} - 3_{03} \\ 2\nu_1 + \nu_3 \ 4_{04} - 3_{03} \\ 4\nu_2 \ 5_{14} - 5_{05} $	3837.86925 3837.86925 10,687.361176 10,687.361176 6244.71929(19)	$\begin{array}{c} N_2 \\ N_2 \\ N_2 \\ SF_6 \\ H_2 O \end{array}$	31.6089(12) 31.48(15) 31.63(6) 25.65(6) 130.3(14)	15.930(15) 7.1(18) 14.8(12) 4.7(9) 17.22(22)	0.1843(2) 0.164(11) 0.198(6) 0.124(6) 0.0677(8)	- 0.79(24) 0.55(12) 0.40(6) - 0.11(17)	0.550(1) 0.24(12) 0.49(4) 0.08(3) -	- 0.547(27) - 1.66(16) - 10.49(16) 3.6(54)

 $\nu_3$  4<sub>04</sub>-3<sub>03</sub> perturbed by N<sub>2</sub> (shown in Fig. 1), we have tested that replacing the quadratic speed-dependence model to the hypergeometric one leads to further reduction (about two times) of the fit residuals.

Finally, it is clear from results shown in Fig. 9 that lineshape parameters  $\Gamma/p$ ,  $\nu_{opt}/p$ ,  $a_W$ , and  $\eta$  retrieved from fits of one of the profiles considered here cannot be directly used in another profile if a sub-percent level of accuracy is expected. Incorporation of high-accuracy measured lineshape parameters into spectroscopic databases based on the HTP requires fitting the data with HTP rather than converting parameters retrieved from different profiles. However, to make use of spectra with insufficiently high SNR or a too-limited range of  $\Gamma/\Gamma_D$  one could set some parameters, e.g.  $\eta$ ,  $a_s$  to zero, to enable fit convergence and to preserve compatibility with the HTP.

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