

# Neutron inelastic scattering measurements of low-energy phonons in the multiferroic BiFeO<sub>3</sub>

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We present neutron inelastic scattering measurements of the low-energy phonons in single crystal BiFeO<sub>3</sub>. The dispersions of the three acoustic phonon modes (LA along [100], TA<sub>1</sub> along [010], and TA<sub>2</sub> along [1 $\bar{1}$ 0]) and two low-energy optic phonon modes (LO and TO<sub>1</sub>) have been mapped out between 300 and 700 K. Elastic constants are extracted from the phonon measurements. The energy linewidths of both TA phonons at the zone boundary clearly broaden when the system is warmed toward the magnetic ordering temperature  $T_N = 640$  K. This suggests that the magnetic order and low-energy lattice dynamics in this multiferroic material are coupled.

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## I. INTRODUCTION

Being both ferroelectric and antiferromagnetic at room temperature, BiFeO<sub>3</sub> holds tantalizing promise for novel device applications and has become one of the most studied multiferroic materials [1]. The direct coupling between the static ferroelectric order ( $T_C \approx 1100$  K) [2,3] and antiferromagnetic order ( $T_N \approx 640$  K) is relatively weak, resulting in a cycloidal spin structure with long wavelength modulations ( $\lambda \approx 620$  Å) [4]. Yet there has been a growing interest in the coupling between dynamical properties in recent years. For example, a “magneto-optical” resonance has been proposed theoretically [5], and extra modes located below the lowest-lying optic phonon energies have been observed in Raman measurements [6–9]. Zone-center optic phonon modes have been studied extensively using Raman spectroscopy [10–13] and infrared reflectivity [14]. A full understanding of the energy-momentum dependence of the dynamics in BiFeO<sub>3</sub> is, however, still far from complete. Only with the recent achievements in the growth of large BiFeO<sub>3</sub> single crystals have researchers been able to start carrying out neutron inelastic and x-ray scattering measurements on both the lattice and spin dynamics [15–19].

In this paper, we present neutron inelastic scattering measurements of the low-energy phonon modes in a large BiFeO<sub>3</sub> single crystal from 300 to 700 K. The dispersions of the three acoustic phonon modes (TA<sub>1</sub>, propagating along [010] and polarized along [100]; TA<sub>2</sub>, propagating along [1 $\bar{1}$ 0] and polarized along [110]; and LA, propagating and polarized along [100]) and the lowest-lying optic modes are mapped out in three different Brillouin zones. The measured phonon dispersions and intensities (after removing the Bose factor) show no significant change with temperature outside of experimental errors. However, the transverse acoustic modes at the zone boundary clearly broaden in energy when the sample is

heated towards  $T_N$ ; this suggests that a coupling exists between the low-energy lattice dynamics and antiferromagnetic order in this multiferroic system.

## II. EXPERIMENT

Single crystals of BiFeO<sub>3</sub> were grown using the traveling-solvent floating-zone technique [20]. The crystal used in this study has a cylindrical shape, a mass of 4 g, and a mosaic full width at half maximum (FWHM) of less than 1°. Neutron inelastic scattering experiments were performed on the HYSPEC time-of-flight spectrometer [21], which is located at the Spallation Neutron Source (SNS) at Oak Ridge National Laboratory. The incident neutron energy  $E_i$  was fixed at 20 meV. We will refer to the pseudocubic unit cell with  $a = 3.9$  Å when describing our results. In this coordinate system, the magnetic ordering wave vector is (0.5,0.5,0.5). The crystal  $c$  axis was oriented vertically to allow access to reflections of the form ( $HK0$ ) in the horizontal scattering plane. During the measurements, the crystal was rotated about the  $c$  axis by 90° in steps of 2° in order to provide full coverage of the reciprocal lattice scattering plane (within kinematical constraints).

## III. RESULTS AND DISCUSSION

In Fig. 1, we plot the dynamic response function  $\chi''(\mathbf{Q}, \hbar\omega) = (1 - e^{-\hbar\omega/k_B T})S(\mathbf{Q}, \hbar\omega)$ , which is simply the measured neutron scattering intensity divided by the Bose factor, at 300, 500, and 700 K. Each panel contains data obtained from two-dimensional (2D) slices through energy-momentum space. The left panels show LA phonons propagating along [100] between the  $\Gamma$  points at (100) and (200). The center panels show phonons propagating along [1 $\bar{1}$ 0] between (110) and (200). Near the (110) zone center, these are TA<sub>2</sub> and TO<sub>2</sub> modes. The right panels show phonons propagating along [010] between (200) and (210), which are TA<sub>1</sub> and TO<sub>1</sub> phonons near (200). We see that whereas the LA, TA<sub>1</sub>, and

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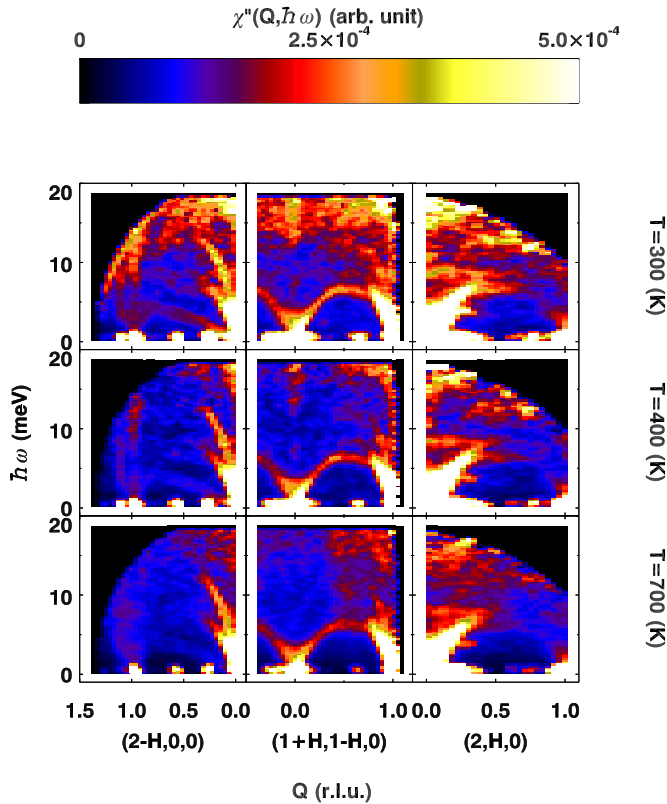


FIG. 1. (Color online) The dynamic response function  $\chi''(Q, \hbar\omega)$  of single crystal  $\text{BiFeO}_3$ , at 300 K (top row), 500 K (middle row), and 700 K (bottom row). The intensities are shown in the  $(HKO)$  plane, for  $q$  along  $[100]$  (left column),  $[1\bar{1}0]$  (middle column), and  $[010]$  (right column), respectively. The strong intensities visible near the top of each panel are spurious and occur when  $\hbar\omega$  approaches  $E_i$ . These spurious intensities are temperature independent. They appear stronger at 300 K (top row) because the data have been divided by the Bose factor.

$\text{TA}_2$  phonons are all well defined, the optic modes are much less clear in our measurements. In particular, the structure factor of the  $\text{TO}_2$  mode near  $(110)$  is extremely weak and can barely be observed.

The data in Fig. 1 reveal no significant changes in the overall features of the dynamic response in  $\text{BiFeO}_3$  between 300 and 700 K. To obtain more detailed information, we fit these data using Lorentzian functions of  $q$  convoluted with the Gaussian instrumental resolution function to extract the acoustic and optic phonon intensities vs energy transfer  $\hbar\omega$  at various wave vectors  $q$ . The phonon energy, energy width ( $2\Gamma$ ), and intensity were also obtained from these fits.

The phonon dispersions obtained from the fits are shown in Fig. 2. We note here that all uncertainties and error bars in this and subsequent figures represent standard deviations. The energies of all acoustic modes show little to no temperature variation, especially in the long-wavelength (small- $q$ ) limit. Near the zone boundary, a slight softening on warming is observed for the  $\text{TA}_1$  mode near  $(2,0.5,0)$  and for the  $\text{TA}_2$  mode near  $(1.5,0.5,0)$ . However the size of this softening is  $\lesssim 0.3$  meV, which is comparable to our experimental uncertainty. The optic phonon intensities are considerably

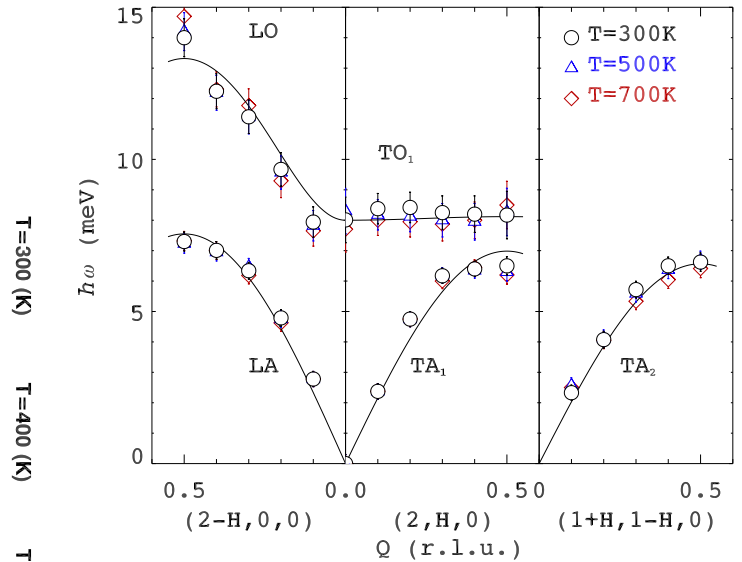


FIG. 2. (Color online) Phonon dispersions measured along various symmetry directions. The phonon energies are obtained from the fits described in the text. Lines are guides to the eye.

weaker than those of the acoustic phonons, and consequently the optic phonon energies have larger error bars. The  $\text{TO}_2$  phonon intensity near the  $(110)$  zone center is particularly weak (Fig. 1, middle column), and for this reason we were not able to determine the  $\text{TO}_2$  phonon dispersion along  $[1\bar{1}0]$ . In the other two zones, the  $\text{TO}_1$  mode propagating along  $[100]$  is almost flat, while the LO mode measured along  $[100]$  is quite steep. Similar to the negligible softening observed for the zone-boundary acoustic modes, the zone-center optic modes also show a slight decrease in energy on warming. But the zone-boundary optic-mode energies exhibit a slight increase instead.

Our results are generally consistent with the neutron inelastic scattering measurements of Delaire *et al.* on powder samples of  $\text{BiFeO}_3$  [18]. They found that the lowest-energy optic phonon branch bottoms out around 8 meV and that the top of the TA branch is close to 6.5 meV. From Fig. 2, one can see that the relevant energies are roughly 8.0 meV (lowest TO phonon energy) and 6.5 meV (top of the TA phonon branch). The value of 8.0 meV is also close to the  $57\text{ cm}^{-1}$  line observed via Raman scattering [11] and the  $66\text{ cm}^{-1}$  line seen in infrared measurements [14], both of which probe zone-center ( $q = 0$ ) optic modes. Other Raman [10] and x-ray inelastic scattering studies [19] suggest that the lowest-energy TO mode is around 9.2 meV. However our results show that a zone-center optic mode is present at 8 meV, clearly below 9 meV, as is illustrated in Figs. 1 and 2.

Based on the measured acoustic phonon branches, a number of useful bulk parameters such as the elastic constants can be obtained [22]. Here we make use of the expression

$$v_i = \sqrt{\frac{C_{\text{eff}}}{\rho}}, \quad (1)$$

where  $v_i$  is the phonon velocity for the  $\text{TA}_1$ ,  $\text{TA}_2$ , or LA modes,  $\rho = 8.408\text{ g/cm}^3$  is the density of  $\text{BiFeO}_3$ , and  $C_{\text{eff}}$  is the effective elastic constant, where  $C_{\text{eff}} = C_{11}$  for the LA

TABLE I. Description of the acoustic phonons.

Mode	Propagation vector	Polarization vector	Velocity (m/s)
LA	[100]	[100]	$2.6(5) \times 10^3$
TA <sub>1</sub>	[100]	[010]	$2.2(4) \times 10^3$
TA <sub>2</sub>	[1 $\bar{1}$ 0]	[110]	$1.6(3) \times 10^3$

mode along [100],  $C_{44}$  for the TA<sub>1</sub> mode along [100], and  $(C_{11} - C_{12})/2$  for the TA<sub>2</sub> mode along [1 $\bar{1}$ 0].

The acoustic phonon velocities were obtained from the limiting slopes of the 300 K dispersion curves shown in Fig. 2 and are listed in Table I. From these, we obtain  $C_{11} = 58(6)$  GPa,  $C_{44} = 42(4)$  GPa,  $C_{12} = 17(2)$  GPa, and the bulk modulus  $B = \frac{1}{3}(C_{11} + 2C_{12}) = 31(3)$  GPa. We note that the room-temperature values of the longitudinal elastic constant  $C_{11}$  derived from previous experimental [19,23,24] and theoretical [25,26] work on BiFeO<sub>3</sub> are highly inconsistent. The value of  $C_{11}$  ranges from  $\approx 60$  GPa (our neutron measurements) to  $\approx 125$  GPa (ultrasonic measurements) to  $\approx 207$  GPa (x-ray inelastic measurements). We believe that the difference between our results and those from the ultrasonic measurements is an artifact of comparing  $C_{11}$  for a single-crystal sample to  $C_L$  for a ceramic sample.  $C_{11}$  is determined by the longitudinal acoustic phonon velocity along [100]. When the LA phonon velocities along other crystallographic directions are higher, a powder/ceramic average will lead to a larger value of  $C_L$ . With respect to the x-ray scattering measurements in Ref. [19], we note that a different coordinate system with trigonal symmetry was used along with a different definition of  $C_{11} = \rho v_{LA[110]}^2$ . For the purpose of obtaining bulk properties in the pseudocubic coordinate system, our results provide a direct reference for the acoustic phonon velocities and elastic constants.

In addition to the acoustic modes and low-energy optic modes discussed above, we have also observed a few spurious signals in our measurements. For example, one can see a faint streak of intensity originating from the (200) Bragg peak in the top-left panel of Fig. 1 that increases to about 4 meV at (1.5,0,0), thus resembling a phonon branch below the LA branch. The intensity of this spurion has no temperature dependence, which is why when  $\chi''$  is plotted in Fig. 1 (and the Bose factor is divided out) it appears to weaken at higher temperatures. When we checked the energy gain side of our scattering data, we found no trace of this spurion, which does not happen with real phonons. We believe it is most likely caused by spurious intensities coming from detectors located close to the strong (200) Bragg peak. We also looked for, but did not detect, any extra modes that resemble the “electromagnon” excitations observed by Raman measurements [6–9].

Figure 3 shows energy scans for the TA<sub>2</sub> mode ( $q \parallel [1\bar{1}0]$ ) at two different wave vectors. The intensities correspond to the dynamic response function  $\chi''(Q, \omega)$  (measured scattering intensity divided by the Bose factor). For small values of  $q$ , such as that shown in the top panel, there is virtually no change of  $\chi''(Q, \omega)$  between 300 and 700 K. But at the zone boundary ( $q = 0.5$ ), as shown in the bottom panel, we observe a clear broadening of the phonon linewidth that is accompanied by a slight softening as the temperature increases

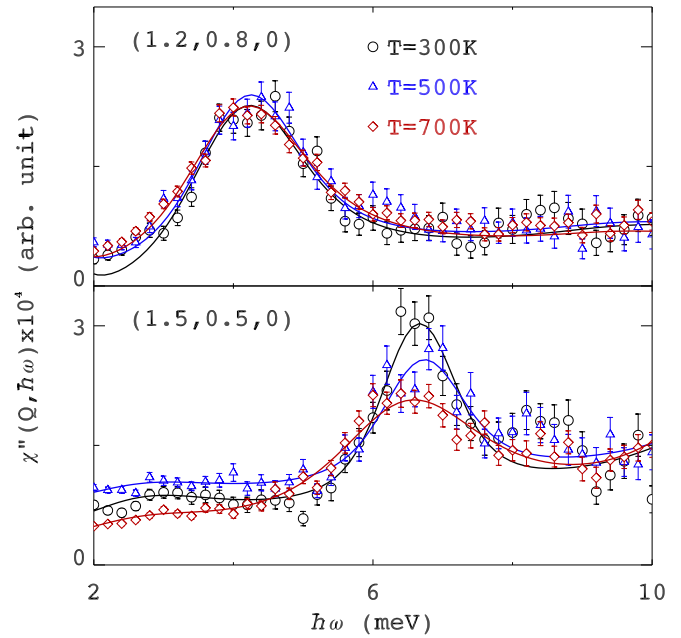


FIG. 3. (Color online) Energy cuts at  $Q = (1.2, 0.8, 0)$  (top frame) and  $Q = (1.5, 0.5, 0)$  (bottom frame). Plotted intensities correspond to  $\chi''(Q, \hbar\omega)$  measured at 300 K (black circles), 500 K (blue triangles), and 700 K (red diamonds).

towards  $T_N \approx 640$  K. We see some evidence of an optic phonon located near 8.5 meV in the bottom panel of Fig. 3; however, it is so weak that we are unable to fit it in a meaningful way. Fortunately, it does not affect our measurement of the TA<sub>2</sub> phonon linewidth. We also observe a broadening of the zone-boundary TA<sub>1</sub> mode, but none is seen for the zone-boundary LA mode. A plot of the phonon-energy widths  $2\Gamma$  between 300 and 700 K for different  $Q$  is shown in Fig. 4. Here we see that only in Figs. 4(b) and 4(d), which are the zone-boundary positions for the TA<sub>1</sub> and TA<sub>2</sub> modes, do the phonon-energy widths increase on heating close to  $T_N$ . For all other wave vectors, there is very little temperature dependence to the phonon-energy widths.

This anomaly in the TA phonon-energy width is unlikely to be the result of pure thermal broadening because it correlates well with  $T_N$  and is not seen at other wave vectors. Previous neutron scattering measurements of the phonon density of states (DOS) in powdered BiFeO<sub>3</sub> [18] reveal a strong anharmonicity, as evidenced by phonon softening and broadening on warming. These DOS measurements are mostly focused on the optic modes; by contrast, our measurements show that the acoustic phonons in BiFeO<sub>3</sub> are well defined and display no significant energy broadening or softening from 300 to 700 K for small  $q$ . Signs of anharmonicity only occur for TA phonons at the zone boundaries.

The fact that the TA phonon broadening at the zone boundary becomes pronounced when the Néel temperature  $T_N$  is approached and the magnetic order starts to melt implies a possible connection between the TA phonons and the magnetic phase transition. Previous Raman measurements [12,13] have suggested that certain optic phonon modes also behave anomalously near  $T_N$ , which is indicative of a spin-phonon coupling in this multiferroic material and possibly other

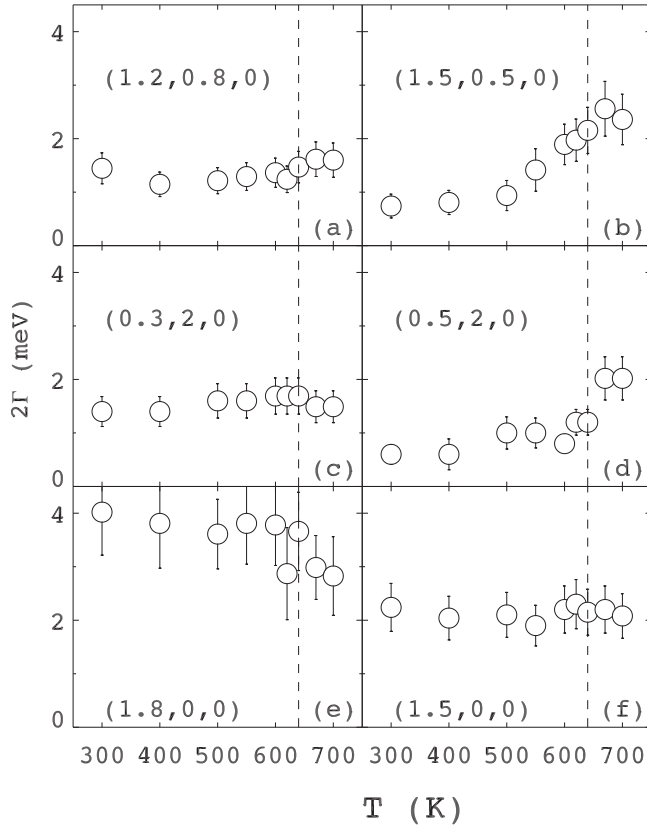


FIG. 4. Energy widths ( $2\Gamma$ ) of acoustic phonons measured at different  $Q$ . The dashed line in the figure denotes the Néel temperature  $T_N$ .

multiferroic perovskites [27]. Our results show that the effects of spin-phonon coupling also extend to the TA phonons. It is possible that this anomalous zone-boundary TA phonon broadening is a combination of spin-polar phonon (TO mode) coupling and TA-TO phonon coupling. While the lowest-lying TO phonon can be affected by the magnetic order near  $T_N$  based on results from the optic measurements, the coupling between the TA and TO modes can lead to the anomalies in the TA branches as well. The coupling is strongest at zone boundaries because the energy difference between the two modes decreases at large  $q$ . This can also explain the lack of

energy broadening in the LA mode, as the LO phonon energy is much higher at zone boundary and the LO-LA coupling there should be significantly weaker. Although the underlying mechanism of this coupling in BiFeO<sub>3</sub> is not entirely clear, it is evident that the melting of the magnetic order at  $T_N$  correlates with a decrease in the zone-boundary TA phonon lifetime, which suggests the development of a lattice instability. Note that the coupling shown here is between the lattice dynamics, or phonons, to the static magnetic order, but not to the spin dynamics (the spin wave). For the latter, one would need to go near the antiferromagnetic zone center [ $Q_{AF} = (0.5, 0.5, 0.5)$ ] where the spin-wave energies are compatible with those of low-energy phonons. Further studies are being planned for the possibilities of dynamic coupling in BiFeO<sub>3</sub>.

#### IV. SUMMARY

Using neutron time-of-flight spectroscopy, we have measured the dispersions of the LA, TA<sub>1</sub>, and TA<sub>2</sub> phonon modes for a single crystal of BiFeO<sub>3</sub> and determined the elastic constants  $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ . The lowest-energy TO and LO phonon dispersions were also measured, and these are consistent with previous Raman and infrared studies. Our results suggest that the zone-center optic-mode energy softens slightly on warming. Most importantly, the transverse acoustic phonons measured at the zone boundary clearly broaden in energy when  $T_N$  is approached from below. This indicates that the acoustic phonon modes and magnetic order are coupled in this multiferroic material.

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