

**1 A dosimetric uncertainty analysis for photon-emitting brachytherapy**  
**2 sources: Report of AAPM Task Group No. 138 and GEC-ESTRO**

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**23** This report addresses uncertainties pertaining to brachytherapy single-source dosimetry preceding  
**24** clinical use. The International Organization for Standardization (ISO) Guide to the Expression of  
**25** Uncertainty in Measurement (GUM) and the National Institute of Standards and Technology  
**26** (NIST) Technical Note 1297 are taken as reference standards for uncertainty formalism. Uncertain-  
**27** ties in using detectors to measure or utilizing Monte Carlo methods to estimate brachytherapy dose  
**28** distributions are provided with discussion of the components intrinsic to the overall dosimetric  
**29** assessment. Uncertainties provided are based on published observations and cited when available.  
**30** The uncertainty propagation from the primary calibration standard through transfer to the clinic for  
**31** air-kerma strength is covered first. Uncertainties in each of the brachytherapy dosimetry parameters  
**32** of the TG-43 formalism are then explored, ending with transfer to the clinic and recommended  
**33** approaches. Dosimetric uncertainties during treatment delivery are considered briefly but are not  
**34** included in the detailed analysis. For low- and high-energy brachytherapy sources of low dose rate  
**35** and high dose rate, a combined dosimetric uncertainty  $<5\%$  ( $k=1$ ) is estimated, which is consistent  
**36** with prior literature estimates. Recommendations are provided for clinical medical physicists, do-  
**37** simetry investigators, and source and treatment planning system manufacturers. These recommen-  
**38** dations include the use of the GUM and NIST reports, a requirement of constancy of manufacturer  
**39** source design, dosimetry investigator guidelines, provision of the lowest uncertainty for patient  
**40** treatment dosimetry, and the establishment of an action level based on dosimetric uncertainty. These  
**41** recommendations reflect the guidance of the American Association of Physicists in Medicine  
**42** (AAPM) and the Groupe Européen de Curiethérapie–European Society for Therapeutic Radiology  
**43** and Oncology (GEC-ESTRO) for their members and may also be used as guidance to manufactur-  
**44** ers and regulatory agencies in developing good manufacturing practices for sources used in routine  
**45** clinical treatments. © 2011 American Association of Physicists in Medicine.  
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**47** Key words: brachytherapy, dosimetry, uncertainty, standards

<b>48</b>	<b>TABLE OF CONTENTS</b>			
<b>49</b>			ESTIMATION. . . . .	<b>3 52</b>
<b>50</b>	I. INTRODUCTION. . . . .	2	III. MEASUREMENT UNCERTAINTY IN BRACHYTHERAPY DOSIMETRY. . . . .	<b>53</b> <b>4 54</b>
<b>51</b>	II. METHODOLOGY OF UNCERTAINTY		III.A. Intrinsic measurement uncertainties. . . . .	<b>4 55</b>
			III.A.1. Source activity distribution. . . . .	<b>4 56</b>

57 III.A.2. Source: Detector positioning. . . . . 4  
 58 III.B. Dose measurement. . . . . 5  
 59 III.B.1. Thermoluminescent dosimeters. . . . . 5  
 60 III.B.2. Radiochromic film. . . . . 6  
 61 III.B.3. Diamonds, diodes, and MOSFETs. . . . . 6  
 62 IV. MONTE CARLO UNCERTAINTY IN  
 63 BRACHYTHERAPY DOSIMETRY. . . . . 6  
 64 IV.A. Source construction. . . . . 6  
 65 IV.B. Movable components. . . . . 7  
 66 IV.C. Source emissions. . . . . 7  
 67 IV.D. Phantom geometry. . . . . 8  
 68 IV.E. Phantom composition. . . . . 8  
 69 IV.F. Radiation transport code. . . . . 8  
 70 IV.G. Interaction and scoring cross sections. . . . . 9  
 71 IV.H. Scoring algorithms and uncertainties. . . . . 9  
 72 V. UNCERTAINTY IN THE TG-43 DOSIMETRY  
 73 FORMALISM PARAMETERS. . . . . 9  
 74 V.A. Air-kerma strength. . . . . 9  
 75 V.A.1. Uncertainty in NIST primary standard for  
 76 LDR low-energy photon-emitting sources. . . . . 9  
 77 V.A.2. Uncertainty in NIST primary standard for  
 78 LDR high-energy photon-emitting  
 79 sources. . . . . 10  
 80 V.A.3.  $S_K$  uncertainty for HDR high-energy  
 81 sources. . . . . 10  
 82 V.A.4. Transfer of NIST standard to the ADCLs. . . . . 11  
 83 V.A.5. Transfer of NIST standard from ADCLs  
 84 to the clinic. . . . . 11  
 85 V.B. Dose-rate constant. . . . . 13  
 86 V.C. Geometry function. . . . . 14  
 87 V.D. Radial dose function. . . . . 14  
 88 V.E. 2D anisotropy function. . . . . 14  
 89 V.F. 1D anisotropy function. . . . . 14  
 90 V.G. TPS uncertainties summary. . . . . 14  
 91 VI. RECOMMENDATIONS. . . . . 15  
 92 VI.A. General uncertainty. . . . . 15  
 93 VI.B. Clinical medical physicists. . . . . 15  
 94 VI.B.1.  $S_K$  and TPS data entry. . . . . 15  
 95 VI.B.2. Treatment planning system developments. . . . . 16  
 96 VI.B.3. Clinical dosimetric uncertainties. . . . . 16  
 97 VI.C. Dosimetry investigators. . . . . 16  
 98 VI.D. Source and TPS manufacturers. . . . . 17  
 99 VII. SUMMARY AND COMPARISON TO  
 100 EXISTING WRITTEN STANDARDS. . . . . 17

101 I. INTRODUCTION

102 This report addresses uncertainties pertaining to photon-  
 103 emitting brachytherapy source calibrations and source do-  
 104 simetry. In the American Association of Physicists in Medi-  
 105 cine (AAPM) TG-40 report,<sup>1</sup> the desired level of accuracy  
 106 and precision is provided for treatment delivery. It is gener-  
 107 ally assumed that brachytherapy uncertainties are larger than  
 108 those in external beam applications. One objective of the  
 109 current report is to quantify the uncertainties involved in  
 110 brachytherapy so a greater understanding can be achieved.  
 111 The uncertainty values of brachytherapy apply to both the

Monte Carlo (MC)-estimated and the experimentally mea-  
 112 sured values. The 2004 AAPM TG-43U1 report considered  
 113 these uncertainties in a cursory manner.<sup>2</sup> Before publication  
 114 of the TG-43U1 report, estimates of dosimetry uncertainties  
 115 for brachytherapy were limited. Most investigators using MC  
 116 techniques presented only statistical uncertainties; only re-  
 117 cently have other MC uncertainties been examined. 118  
 119 In the current report, the uncertainty propagation from the  
 120 primary calibration standard through transfer to the clinic for  
 121 air-kerma strength  $S_K$  is detailed (Fig. 1). Uncertainties in  
 122 each of the brachytherapy dosimetry parameters are then ex-  
 123 plored, and the related uncertainty in applying these param-  
 124 eters to a TPS for dose calculation is discussed. Finally, rec-  
 125 ommended approaches are given. Section II contains detailed  
 126 explanations of type A and type B uncertainties. The brachy-  
 127 therapy dosimetry formalism outlined in the AAPM TG-43  
 128 report series [1995,<sup>3</sup> 2004,<sup>2</sup> and 2007 (Ref. 4)] is based on  
 129 limited explanation of the uncertainties involved in the mea-  
 130 surements or calculations. The 2004 AAPM TG-43U1 report  
 131 presented a generic uncertainty analysis specific to calcula-  
 132 tions of brachytherapy dose distributions. This analysis in-  
 133 cluded dose calculations based on simulations using MC  
 134 methods and experimental measurements using thermolumi-  
 135 nescent dosimeters (TLDs). These simulation and measure-  
 136 ment uncertainty analyses included components toward devel-  
 137 oping an uncertainty budget. While a coverage factor of 2  
 138 ( $k=2$ ) is recommended for testing and calibration laborato-  
 139 ries per the International Organization for Standardization  
 140 (ISO) 17025 report<sup>5</sup> and in general for medicine,<sup>6</sup> we also  
 141 recommend this coverage factor for the scope of uncertain-  
 142 ties included in the current report. Thus, a coverage factor of  
 143 2 is used in the current report unless explicitly described  
 144 otherwise.  
 145 The current report is restricted to the determination of  
 146 dose to water in water without consideration of material het-  
 147 erogeneities, interseed attenuation, patient scatter conditions,  
 148 or other clinically relevant advancements upon the AAPM  
 149 TG-43 dose calculation formalism.<sup>7</sup> Specific commercial  
 150 equipment, instruments, and materials are described in the  
 151 current report to more fully illustrate the necessary experi-  
 152 mental procedures. Such identification does not imply rec-  
 153 ommendation or endorsement by either the AAPM, ESTRO,  
 154 or the U.S. National Institute of Standards and Technology  
 155 (NIST), nor does it imply that the material or equipment  
 156 identified is necessarily the best available for these purposes.  
 157 These recommendations reflect the guidance of the AAPM  
 158 and GEC-ESTRO for their members and may also be used as  
 159 guidance to manufacturers and regulatory agencies in devel-  
 160 oping good manufacturing practices for sources used in rou-  
 161 tine clinical treatments. As these recommendations are made  
 162 jointly by the AAPM and ESTRO standing brachytherapy  
 163 committee, the GEC-ESTRO, some of the specifically men-  
 164 tioned U.S. agencies, organizations, and standard laborato-  
 165 ries should be interpreted in the context of the arrangements  
 166 in other countries where applicable. In particular, other pri-  
 167 mary laboratories, such as the Physikalisch-Technische  
 168 Bundesanstalt (PTB) in Braunschweig, Germany, the Na-

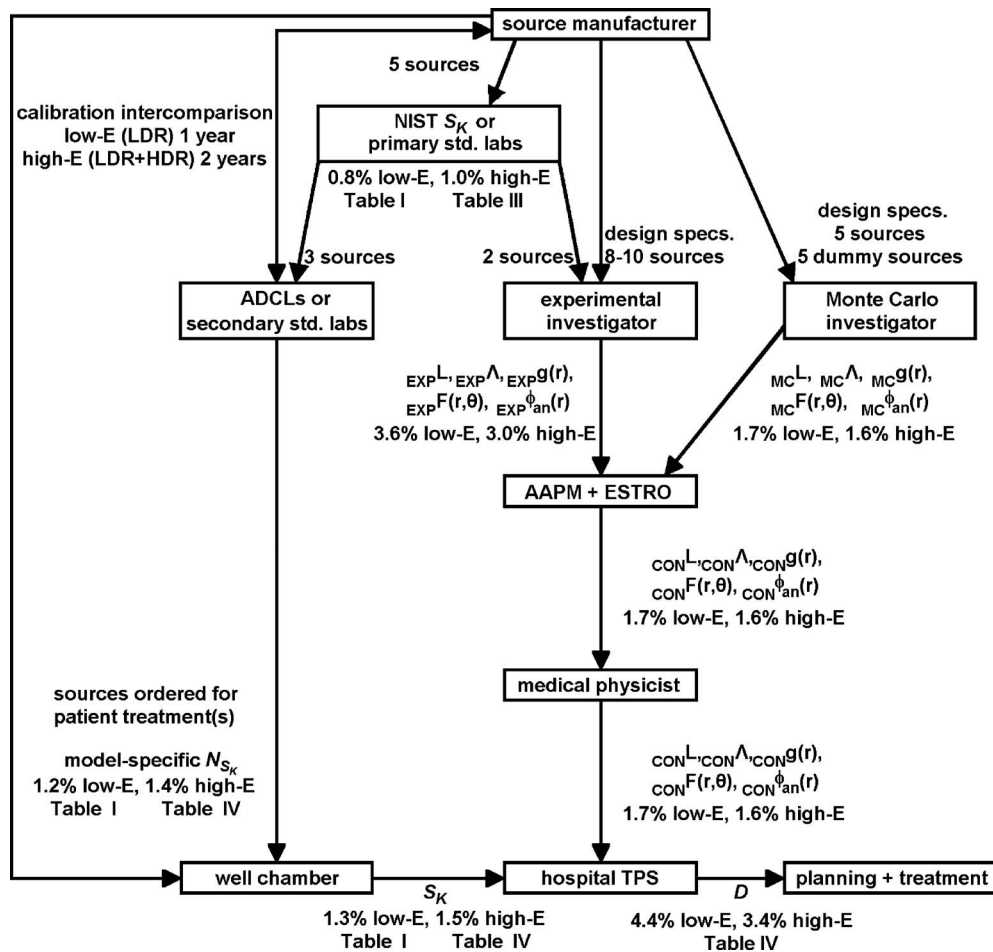


FIG. 1. Brachytherapy source dosimetry data chain, highlighting the uncertainty values ( $k=2$ ) and how they combine to increase the overall dosimetric uncertainty for the U.S. The low- $E$  and high- $E$  refer to low- and high-energy photon-emitting sources, respectively, and are representative of both LDR and HDR brachytherapy sources. The symbols and notation in this figure are in accordance with the 2004 AAPM TG-43U1 report. Symbols such as  $EXP^L$ ,  $MC^L$ , and  $CON^L$  represent the active lengths used by the experimental investigators, Monte Carlo simulator investigators, and the consensus value, respectively. Following the flow chart, manufacturers first create sources and follow the AAPM 2004 CLA subcommittee recommendations for initial source calibrations by sending the flow sources to a primary standards laboratory (e.g., NIST) then to the secondary standards laboratories (e.g., ADCLs) and experimental dosimetry investigator(s). The AAPM and GEC-ESTRO then prepare candidate and consensus dosimetry parameters to serve as reference datasets for widespread and uniform clinical implementation. Clinical medical physicists should use these data whenever available and assure proper entry and QA for commissioning in their TPS. At the upper-right, calibration intercomparisons are performed to ensure the secondary standards laboratories and manufacturers are in agreement. When the clinical medical physicist orders sources for treating a patient, sources are calibrated on site using equipment calibrated at a secondary standards laboratory or ADCL with direct traceability to a primary standards laboratory (e.g., NIST) according to AAPM 2008 LEBS recommendations. The patient-specific source strength  $S_K$  is entered into the TPS, and clinical treatment planning and treatment delivery are performed as illustrated in the bottom portion of this figure.

169 tional Physical Laboratory (NPL) in the United Kingdom,  
 170 and the Laboratoire National Henri Becquerel (LNHB) in  
 171 France perform brachytherapy source calibrations, each mea-  
 172 surement system having an associated uncertainty budget. It  
 173 should be noted that many of these uncertainties affect  
 174 source parameters before use in the clinic and the clinical  
 175 medical physicist has no control over them.

## 176 II. METHODOLOGY OF UNCERTAINTY ESTIMATION

177 Uncertainty is a useful and important concept for quanti-  
 178 tatively determining the accuracy of measurements and cal-  
 179 culations. Uncertainty analysis is different from the outdated  
 180 method of random and systematic errors. The terms *accuracy*  
 181 and *precision* are still maintained but with slightly different  
 182 definitions. Accuracy is defined as the proximity of the result

to the conventional true value (albeit unknown) and is an  
 indication of the correctness of the result. Precision is de-  
 fined as a measure of the reproducibility of the result. A  
 stable instrument capable of making high-precision measure-  
 ments is desired since it can be calibrated to provide an ac-  
 curate result. Uncertainty determination takes into account  
 measurement or calculation variations, including all of the  
 precisions of the measurements or calculations and their ef-  
 fects on the results. Thus, uncertainty is a part of every mea-  
 surement or calculation. The hardest part of uncertainty de-  
 termination is to account for all possible influences. The  
 uncertainty can be thought of as a defining interval, which is  
 believed to contain the true value of a quantity with a certain  
 level of confidence. For a coverage factor of 2 (see above),  
 the true value of the quantity is believed to lie within the

198 uncertainty interval with a 95% level of confidence.

199 The present-day approach to evaluating uncertainty in  
200 measurements is based on that recommended by the Comité  
201 International des Poids et Mesures (CIPM) in 1981.<sup>8</sup> The  
202 CIPM recommendations included grouping uncertainties into  
203 two categories (type A and type B, to be explained below), as  
204 well as the methods used to combine uncertainty compo-  
205 nents. This brief CIPM document was expanded by an ISO  
206 working group into the *Guide to the Expression of Uncer-*  
207 *tainty in Measurement* (GUM), first published in 1993 and  
208 subsequently updated in 2010.<sup>9</sup> This formal method of as-  
209 sessing, evaluating, and reporting uncertainties in measure-  
210 ments was presented in a succinct fashion in NIST Technical  
211 Note 1297, *Guidelines for Evaluating and Expressing the*  
212 *Uncertainty of NIST Measurement Results* (1994).<sup>10</sup> The  
213 main points of this Technical Note relevant to the current  
214 report are summarized below.

215 Components of measurement uncertainty may be classi-  
216 fied into two types, namely, those evaluated by statistical  
217 methods (type A) and those evaluated by other means (type  
218 B). In the past, type A and type B uncertainties were com-  
219 monly referred to as *random* and *systematic* errors (more  
220 properly uncertainties), respectively. The use of the term *er-*  
221 *ror* is discouraged in uncertainty analyses since it implies a  
222 mistake or refers to the difference between the measured  
223 value of a quantity and the true value, which is unknown. For  
224 example, what might be considered as an error by one do-  
225 simetry investigator could be considered an uncertainty by  
226 another investigator. Specifically, investigator 1 might assign  
227 a large uncertainty to the dimensions of internal source com-  
228 ponents without having first-hand knowledge of source con-  
229 struction or the ability to open the capsule. Investigator 2  
230 might question the values used by investigator 1, considering  
231 them erroneous, having opened the capsule and measured the  
232 dimensions of the internal components. If the true value was  
233 known, there would be no need to perform the measurement  
234 or simulation.

235 Representing each component of uncertainty by an esti-  
236 mated standard deviation yields the *standard uncertainty*,  $u$ .  
237 For the  $i$ th type A component,  $u_i = s_i$ , the statistically esti-  
238 mated standard deviation is evaluated as the standard devia-  
239 tion of the mean of a series of measurements. For the  $j$ th  
240 type B component,  $u_j$  is an estimate of the corresponding  
241 standard deviation of an assumed probability distribution  
242 (e.g., normal, rectangular, or triangular) based on scientific  
243 judgment, experience with instrument behavior, and/or the  
244 instrument manufacturer's specifications. Historical data in  
245 the form of control charts from a given measurement process  
246 may be used to evaluate type B components of uncertainty.  
247 The *combined standard uncertainty*  $u_c$  represents the esti-  
248 mated standard deviation of a measurement result and is cal-  
249 culated by taking the square root of the sum-of-the-squares  
250 of the type A and type B components. This technique of  
251 combining components of uncertainty, including relevant  
252 equations such as the Law of Propagation of Uncertainty, is  
253 illustrated in Sec. IV C of the TG-43U1 report.<sup>2</sup> In the cur-  
254 rent report, uncertainty propagation is accomplished by add-  
255 ing in quadrature the relative (%) uncertainties at each step

of a measurement traceability chain. This is only the case  
since the measurement equation is a simple product of mea-  
sured or calculated quantities. If the probability distribution  
characterized by the measurement result  $y$  is approximately  
normal, then  $y \pm u_c$  gives an interval within which the true  
value is believed to lie with a 68% level of confidence.

Normally, the symbol  $U$  is used to express the *expanded*  
*uncertainty*; however, to avoid confusion with the unit  $U$  for  
air-kerma strength, this AAPM/GEC-ESTRO report uses the  
symbol  $V$  for this quantity. An expanded uncertainty  $V = ku_c$ ,  
where  $k$  is the coverage factor, is typically reported and is  
applied only to the combined uncertainty, not at each stage of  
an evaluation. Assuming an approximately normal distribu-  
tion,  $V = 2u_c$  ( $k = 2$ ) defines an interval with a 95% level of  
confidence, and  $V = 3u_c$  ( $k = 3$ ) defines an interval with a level  
of confidence  $>99\%$ . When there is limited data and thus  $u_c$   
has few degrees of freedom,  $k = t$  factor is determined from  
the  $t$  distribution.<sup>9,10</sup>

### III. MEASUREMENT UNCERTAINTY IN BRACHYTHERAPY DOSIMETRY

There are a number of uncertainties involved in brachy-  
therapy dosimetry measurements. These measurements are  
usually performed at research facilities outside the clinic.  
Dosimetry investigators should propose methods to quantify  
all these uncertainties and specify them in their publications.

#### III.A. Intrinsic measurement uncertainties

Inherent characteristics of the source and devices used for  
dosimetric measurements include knowledge of the source  
activity distribution and source-to-detector positioning.  
These characteristics contribute to dosimetric uncertainties,  
often specific to the model of source and detector.

##### III.A.1. Source activity distribution

An uncertainty in source activity distribution on the inter-  
nal substrate components becomes a systematic uncertainty,  
propagating to all measurements. Most brachytherapy  
sources are assumed to be uniform about the circumference  
of the long axis due to their cylindrical symmetry. However,  
in reality the vast majority of sources demonstrate variations  
of 2%–20% in the intensity of emissions about the long axis  
for high- and low-energy photon emitters. Such variations  
are reflected in the statistical uncertainty of measurements if  
measurements are made at numerous circumferential posi-  
tions around the source, and the results are averaged.<sup>11,12</sup>  
Variations around the source have been demonstrated in the  
calibrations performed at NIST.<sup>13</sup>

##### III.A.2. Source: Detector positioning

Several types of uncertainty arise from the relative posi-  
tions of the source and detector and depend on the phantom  
material and the detector. If TLD is used, the shape of the  
detector (TLD rods, chips, or capsules of powder) may lead  
to different uncertainties in the location of the detector rela-  
tive to the source. Film, generally radiochromic film, has

308 become a common detector for brachytherapy measure-  
 309 ments. The positional uncertainty for film has two compo-  
 310 nents: The positioning of the film and the positional uncer-  
 311 tainty for relating the reading of the optical density to the  
 312 position in the phantom. Measurements in a water phantom  
 313 rarely use diode or diamond detectors. For measurements of  
 314 some parameters, such as dose-rate constant  $\Lambda$  and radial  
 315 dose function  $g(r)$ , the source is positioned normal to the  
 316 detector plane. A type A dosimetric uncertainty in detector  
 317 distance from the source relative to the mean detector dis-  
 318 tance appears as an uncertainty in detector reading. However,  
 319 a type B uncertainty in the mean distance of a group of  
 320 detectors must be considered in the analysis of  $\Lambda$  and  $g(r)$ .  
 321 For measurements of the 2D anisotropy function  $F(r, \theta)$ , the  
 322 uncertainty in the distance of each detector from the source  
 323 must be determined. In addition, the uncertainty in the angle  
 324 from the source long axis must be considered. Taylor *et al.*<sup>14</sup>  
 325 determined the uncertainty ( $k=1$ ) in the mean distance to the  
 326 detectors in a water phantom to be 0.09 mm. However, Taylor  
 327 *et al.*<sup>15</sup> claimed a seed-to-TLD positioning uncertainty of  
 328 0.05 mm ( $k=3$ ) for a 0.3% type B component dosimetric  
 329 uncertainty at  $r=1$  cm. More typical values obtained by a  
 330 routine investigator would fall around 0.5 mm ( $k=1$ ).

331 The uncertainty in the detector point of measurement var-  
 332 ies somewhat with the phantom material and related tech-  
 333 nique. If a water tank scanner is used, there is an uncertainty  
 334 associated with the movement and positioning. A scanning  
 335 system might display a source-to-detector positioning preci-  
 336 sion of 0.1 mm. However, typical positioning accuracy of a  
 337 water tank scanner is about 0.4 mm, expressed as  $k=2$ .<sup>16</sup> The  
 338 accuracy is more difficult to specify, in part, because of the  
 339 uncertainty in the source-positioning device and also because  
 340 of the uncertainty in the effective point of measurement for  
 341 the detector. Considering only the effects of geometry (i.e.,  
 342 the inverse-square relationship) and ignoring signal variation  
 343 across the detector (i.e., a pointlike detector), the dosimetric  
 344 effects of a 0.04 cm positional uncertainty at distances of 1  
 345 cm and 5 cm are 8% and 1.6%, respectively.

346 For dose rate measurements of the same duration at these  
 347 positions, the reading at 5 cm is 25 times lower than the 1 cm  
 348 reading due to the inverse-square effect alone, not account-  
 349 ing for medium attenuation. For measurements involving  
 350 low-energy photon emitters, the relative signal at the greater  
 351 distance is considerably lower due to medium attenuation  
 352 that is not compensated by increased scatter. Most often, the  
 353 detectors used for brachytherapy dosimetry measurements  
 354 are not limited by counting statistics, but rather intrinsic  
 355 properties such as signal-to-noise ratio and detector repro-  
 356 ducibility. This often produces an uncertainty at 5 cm about  
 357 ten times larger than that at 1 cm. When compared to source-  
 358 :detector positioning uncertainty, there is partial compensa-  
 359 tion between these two effects. The decreased signal with  
 360 distance can sometimes be overcome when using integrating  
 361 dosimeters simply by leaving the dosimeters in place for a  
 362 longer time. Radionuclides with short half-lives limit the im-  
 363 provement that can be achieved by increasing the exposure  
 364 duration. For <sup>103</sup>Pd, with a 17-day half-life, the dose rate at 5

cm is only 0.4% of that at 1 cm in water. To obtain 1 Gy at  
 1 cm from a 1 U source requires about 6.9 days. At 5 cm  
 from this same source, the maximum dose possible after  
 complete decay of the source is less than 1.5 cGy. Thus,  
 extending the exposure time for the more distant points can-  
 not be considered equivalent.

### III.B. Dose measurement

There are unique challenges to measuring radiation dose  
 in the presence of either a high dose gradient or a very low  
 dose rate (LDR), particularly for low-energy photon-emitting  
 sources. The major consideration is the need for a detector  
 with a wide dynamic range, flat energy response, small geo-  
 metric dimensions, and adequate sensitivity. Radiation mea-  
 surement devices in general use for brachytherapy source  
 dosimetry are LiF TLDs, radiochromic films, diamond, di-  
 ode, and metal-oxide-field effect transistor (MOSFET) detec-  
 tors. These detector types are considered below and may be  
 chosen for their dynamic dose range, high-spatial resolution,  
 feasibility for *in vivo* dosimetry, and approximation to human  
 soft tissue, or relative ease of use. However, the accuracy of  
 the results from these detectors is subject to the uncertainties  
 due to volume averaging, self-attenuation, and absorbed-  
 dose sensitivity. At the small source:detector distances of  
 brachytherapy, detector size can influence self-attenuation  
 and volume averaging.

#### III.B.1. Thermoluminescent dosimeters

TLDs have been the main dosimeter used for measure-  
 ment of brachytherapy source dose. Typically, these mea-  
 surements have been made in solid-water phantoms com-  
 prised of plastics having radiological characteristics similar  
 to water. Kron *et al.*<sup>17</sup> provided characteristics that should be  
 reported each time a TLD measurement is made. A calibra-  
 tion of the TLDs to a known energy and dose is necessary to  
 perform dosimetry. Two major sources of uncertainty are the  
 annealing regime used by different investigators and the in-  
 trinsic energy dependence  $k_{Bq}(Q)$ , which is per unit of activ-  
 ity (i.e., Becquerel). Depending on the temperatures and  
 cooling for the materials, the uncertainty can increase dras-  
 tically, from 1% to 5%. The uncertainty is reduced when  
 meticulous care is used in the handling, reading, and irradiation  
 conditions. The other large source of uncertainty is the  
 variation in the TLD absorbed-dose sensitivity between the  
 energy used for calibration and that of the brachytherapy  
 source. This is the uncertainty in the relation of the energy  
 dependence of the absorbed-dose sensitivity relative to that  
 in the beam quality used for calibration. Each reading regime  
 should be the same to reduce the variation. The characteris-  
 tics that affect thermoluminescence are elaborated upon in  
 Chap. 24 of the 2009 AAPM Summer School text.<sup>18</sup> If care  
 is taken in each of the regimes, an overall estimate of the  
 expanded uncertainty to measure absorbed dose would be  
 5.58% ( $k=2$ ).

### 417 **III.B.2. Radiochromic film**

418 Radiochromic film has become a common detector for  
 419 brachytherapy measurements. Various advantages of EBT  
 420 film compared to silver halide film include the following:  
 421 Relative energy insensitivity, insensitivity to visible light,  
 422 self-developing characteristics, greater tissue equivalency,  
 423 and dose-rate independence.<sup>20-23</sup> Different investigators have  
 424 noted up to 15% variation in the film response throughout a  
 425 film that was exposed to a uniform dose of radiation. Sources  
 426 for these uncertainties have been pointed out by Bouchard *et*  
 427 *al.*<sup>24</sup> Looking at two orthogonal directions, the film response  
 428 is more uniform in one direction. Applications of various  
 429 models of radiochromic film in radiation dosimetry have  
 430 been discussed in detail in AAPM TG-55 (Ref. 25) and more  
 431 recently by Soares *et al.*<sup>26</sup> Radiochromic film response is  
 432 independent of dose rates in the clinical range of 0.1–4 Gy/  
 433 min. Dini *et al.*<sup>23</sup> showed that the responses of both XR type  
 434 T and type R films were independent of the dose rate. The  
 435 results of their investigations showed a 5% variation for dose  
 436 rates ranging from 0.16 to 7.55 Gy/min. These results were  
 437 in good agreement with the finding of Giles and  
 438 Murphy,<sup>27</sup> who had shown that XR type films are dose-rate-  
 439 independent within 5%. In an independent investigation,  
 440 Saylor *et al.*<sup>21</sup> showed 5% variation in optical densities of  
 441 HD-810 film for dose rates ranging from 0.02 to 200 Gy/  
 442 min. However, many of the reports in literature pertain to  
 443 older films that are not useful for current brachytherapy mea-  
 444 surements. The manufacturer discontinued production of  
 445 EBT film and now only provides the EBT2 model. The do-  
 446 simetric uncertainties of brachytherapy source measurements  
 447 made with EBT2 are increasingly being investigated.<sup>28-30</sup>  
 448 Before use, the dosimetry investigator should be aware of the  
 449 characteristics of the individual type of film.

450 In general, the handling of the film can be important so  
 451 that exposure to ultraviolet light and other conditions are  
 452 minimized; again the uncertainty can be reduced if this care  
 453 is taken. An estimate of the expanded uncertainty to measure  
 454 absorbed dose is 10%.<sup>30,31</sup> Due to the increasing number of  
 455 different radiochromic films and their dependence on scan-  
 456 ning techniques, caution is recommended. In addition, it is  
 457 important to realize that the scanner can have a significant  
 458 effect on the results of the film.<sup>32</sup> While investigations have  
 459 been made for various scanners such as by Hupe and  
 460 Brunzendorf<sup>31</sup> and by Alva *et al.*,<sup>33</sup> there have been conflict-  
 461 ing results requiring further research.

### 462 **III.B.3. Diamonds, diodes, and MOSFETs**

463 Occasionally, measurements in a water phantom use diode  
 464 or diamond detectors, but their dosimetric uncertainties can  
 465 exceed 15% ( $k=1$ ) for low-energy photon-emitting brachy-  
 466 therapy sources.<sup>34</sup> These uncertainties result from the large  
 467 energy dependence of its absorbed-dose sensitivity, nonlin-  
 468 earity, directional dependence, temperature dependence, and  
 469 bias dependence, especially when used for low-energy  
 470 brachytherapy sources. Diode characteristics are given in the  
 471 AAPM TG-62 report by Yorke *et al.*<sup>35</sup> MOSFET dose re-  
 472 sponse is also energy and dose-rate dependent.<sup>36,37</sup> While

MOSFETs have been used for brachytherapy *in vivo*<sup>473</sup>  
 dosimetry,<sup>38,39</sup> they have not been used to date for direct<sup>474</sup>  
 dosimetric parametrization of brachytherapy sources.<sup>475</sup>

## IV. MONTE CARLO UNCERTAINTY IN BRACHYTHERAPY DOSIMETRY

476 While MC methods may be used to characterize brachy-  
 477 therapy source dosimetry accurately, there are both obvious  
 478 and hidden uncertainties associated with the process that  
 479 must be accounted for. For large numbers of histories where  
 480 Poisson statistics applies, the uncertainty in the estimated  
 481 results decreases by the square root of the number of particle  
 482 histories. This uncertainty is referred to as the type A uncer-  
 483 tainty for MC methods and should be kept to <0.1% when  
 484 feasible so as to be negligible in comparison to other com-  
 485 putational uncertainties. In many cases, it is unfeasible to  
 486 simulate additional histories due to processing power and  
 487 time constraints. While variance reduction techniques are  
 488 sometimes used to diminish type A uncertainties, careful  
 489 benchmarking is required for radiation transport codes and  
 490 their individual features and subroutines. The MC dosimetric  
 491 uncertainty analysis presented in Table XII of the TG-43U1  
 492 report listed four separate components<sup>2</sup> and has been sub-  
 493 stantially expanded here into eight separate components (all  
 494 but one being type B). These roughly correspond chronologi-  
 495 cally (for nonadjoint particle transport) with the MC simula-  
 496 tion process and must be estimated by each dosimetry inves-  
 497 tigator for the specific source and circumstance being  
 498 studied. Consequently, example tables are not provided since  
 499 the results are dependent on the energy of the source emis-  
 500 sions, capsule design, simulation goals, and MC code. This  
 501 subsection reviews the simulation process and current state-  
 502 of-the-art for uncertainty analyses. It is important to clarify  
 503 the methods used to arrive at values for the dosimetric com-  
 504 ponent uncertainties and always aspire to minimize these un-  
 505 certainties. It is also important to understand that manufac-  
 506 tured sources may differ from the design parameters, and  
 507 MC simulations should be performed with representations of  
 508 the final clinically delivered product. What follows are de-  
 509 scriptions of uncertainties that arise throughout the process  
 510 of using MC methods to simulate dose-rate distributions in  
 511 the vicinity of brachytherapy sources. Dosimetry investiga-  
 512 tors are urged to consider these analyses and introduce de-  
 513 tailed estimates, with quadrature sum uncertainties on each  
 514 type of result, in future brachytherapy dosimetry publica-  
 515 tions.<sup>516</sup>

### IV.A. Source construction

517 Characterization of brachytherapy dose-rate distributions  
 518 for clinical purposes for all source parameters starts with a  
 519 full understanding of the source construction. In general,  
 520 brachytherapy sources contain radionuclides that are sealed  
 521 in a single capsule. High dose-rate (HDR) sources usually  
 522 have the capsule attached to a delivery cable used to position  
 523 the individual source at multiple locations within the patient.  
 524 Pulsed dose-rate sources are similar to HDR, but the treat-  
 525 ment is applied in a protracted manner. LDR sources may be  
 526

described as individual entities and do not utilize a delivery cable. However, they may be contained within metal or plastic cylinders or a surgical suture material as is the case for stranded seeds. With the current TG-43 dosimetry formalism based on superposition of individual sources within a 30 cm diameter water phantom to provide full-scatter conditions for  $r \leq 10$  cm for low-energy sources, characterization of the active radionuclide and the source capsule is all that is required.<sup>2</sup>

The dosimetry investigator should independently assess all available manufacturer data on source construction, estimate the uncertainties associated with each dimension, and estimate the distribution of results within the available range of results. A theoretical example is provided for how to characterize the source geometry uncertainties for a hypothetical brachytherapy source.

(a) The capsule is a right cylinder made of pure (100%) titanium ( $\rho = 4.51 \pm 0.05$  g/cm<sup>3</sup>), with inner and outer diameters of 0.70 and 0.80 mm (rectangular distribution over a tolerance of  $\pm 0.02$  mm), respectively, overall length of 4.52 mm (rectangular distribution over a tolerance of  $\pm 0.05$  mm), and end-weld thicknesses of 0.15 mm (rectangular distribution over a tolerance of  $\pm 0.03$  mm).

(b) The capsule is filled with room temperature Ar gas ( $\rho = 1.78 \pm 0.04$  mg/cm<sup>3</sup>) and an Ir pellet.

(c) The Ir source pellet ( $\rho = 22.5 \pm 0.3$  g/cm<sup>3</sup>) is a right cylinder with a 0.66 mm diameter (rectangular distribution over a tolerance of  $\pm 0.01$  mm) and 4.10 mm active length  $L$  (rectangular distribution over a tolerance of  $\pm 0.02$  mm) with a <sup>192</sup>Ir loading of  $(3.2 \pm 0.2) \times 10^{11}$  atoms uniformly distributed throughout the pellet.

This description presents uncertainties  $k=1$  associated only with capsule dimensions, internal components, and location of radiation emission. A more sophisticated MC dosimetric analysis would simulate the influence of varying each of these components and estimate the resultant effect of these uncertainties on the calculated dose distribution. Karaikos *et al.*<sup>40</sup> investigated the effect of varying the silver halide coating thickness (i.e., 1–10  $\mu$ m) for an <sup>125</sup>I source;  $\Lambda$  and  $g(r)$  were unchanged within 1%. Koona<sup>41</sup> assessed variable <sup>125</sup>I source capsule wall thickness (i.e., 30–100  $\mu$ m) and found an influence on  $\Lambda$  ranging from +16% to –1%. For similar endweld thicknesses, differences in  $\Lambda$  ranged from –0.2% to 0.9%. However, the variation in the endweld thickness led to a significant impact on  $F(r, \theta)$  for small polar angles.

#### IV.B. Movable components

As shown by Rivard, the internal components within the capsule may change position.<sup>42</sup> The dimensions from source to source may vary also. At distances of a few millimeters from some sources, the dose rate can change more than a factor of 2 upon varying the capsule orientation.<sup>42</sup> Since most low-energy sources do not have their internal components rigidly attached to the encapsulation, it is possible that

the internal components may move about based on the source orientation. Especially for a low-energy photon-emitting source containing radio-opaque markers for localization, such dynamic aspects may be of clinical relevance under certain circumstances. While this effect can be observed experimentally when the source orientation is rotated 180°, this behavior is readily assessable using MC methods, but more challenging with experimental techniques where localization of the internal components may be unknown. To ascribe MC dosimetric uncertainties to this component, the full range of motion should be considered, along with possibilities for configuring internal components if multiple items are free to move and subtend different geometries upon settling within the capsule. An example is provided.

- For the example given in the source geometry uncertainty description, the Ir pellet could move  $\pm 0.25$  mm along the capsule long axis and  $\pm 0.035$  mm in the lateral direction within the capsule due to a combination of dimensional tolerances.
- In addition to the aforementioned shifts, the pellet could possibly rotate within the capsule.

Clearly, the single internal component (Ir pellet) is well constrained, and dosimetric uncertainties due to a dynamic internal component would be small compared to other dosimetric uncertainty components. However, this would not be the case if the internal component containing a low-energy photon-emitting radionuclide were much smaller and nestled behind a radio-opaque marker where the radiation emissions would be substantially attenuated in comparison to an optimized geometry for the internal components.

It appears that the dynamic internal components of sources can have the largest influence on dose rate variations and thus should be considered for the source models, positions of interest, and source orientation relevant to the clinical application. In general, the dosimetric uncertainty related to internal component movement increases as photon energy decreases. While not an important aspect for all sources, the dosimetry investigator should assess the impact of this effect for the type of source being examined since some sources are fairly susceptible to this effect (previously mentioned factor of 2) where other sources exhibit less than a 0.1% dosimetric effect at the reference position.<sup>43</sup> Time-averaged internal component positions should be used for reference data, and the dosimetric uncertainties for all possible internal component positions should be considered.

#### IV.C. Source emissions

Brachytherapy sources generally contain radioactive materials and have capsules to prevent direct contact of the radioactive materials with patients. Exceptions include electronic brachytherapy sources, which generate radiation without radionuclides,<sup>44,45</sup> and the <sup>103</sup>Pd RadioCoil source.<sup>46</sup> Since nuclear disintegration processes are well understood, there is little uncertainty associated with knowledge of the radiation spectrum from the radioactive materials. A general uncertainty in dose rate per unit source strength at  $P(r_0, \theta_0)$

638 of 0.1% for low-energy sources<sup>43</sup> and 0.5% for high-energy  
639 sources<sup>47</sup> may be assumed. However, physical fabrication of  
640 brachytherapy sources often involves radiochemistry and  
641 other processes to purify the isotopic and elemental compo-  
642 sition of the radioactive product. With radiocontaminants  
643 having different half-lives than the desired radionuclide,  
644 there may be substantial uncertainty concerning the radionu-  
645 clides contained in the source. When simulated using MC  
646 methods, the dosimetry investigator is advised not to assume  
647 a pure radioactive product and to include the contaminant  
648 radionuclides and daughter products in the carrier material if  
649 the presence of such contaminants has been verified (mass-  
650 spectroscopy measurements and/or photon spectrometry  
651 measurements). Further, electron dose contributions from  
652 sources generally considered as photon emitters should be  
653 considered.<sup>48–50</sup>

654 The National Nuclear Data Center (NNDC) at  
655 Brookhaven National Laboratory is an internationally re-  
656 garded reference for radionuclide radiation spectra.<sup>51</sup> This  
657 database includes all of the commonly used radionuclides in  
658 brachytherapy, often listing the precision of photon and elec-  
659 tron energies to four significant digits and the emission in-  
660 tensities to three significant digits and probabilities to parts  
661 per million. As a result of uncertainties in the source photon  
662 energies and the exaggerated precision of emission probabili-  
663 ties, the dosimetry investigator should consider the influence  
664 of an inaccurate spectral characterization on the resultant  
665 dose distribution. This latter feature would be most meaning-  
666 ful for considering relatively new radionuclides, for sources  
667 with novel means of generating radiation, and for sources  
668 that contain radionuclides which emit both photons and elec-  
669 trons.

#### 670 IV.D. Phantom geometry

671 Phantom size has a significant effect on brachytherapy  
672 dose distributions.<sup>52–54</sup> Although variations in radiation scat-  
673 ter and attenuation are readily accounted for with modern  
674 external-beam TPS, brachytherapy TPS generate dosimetry  
675 data based on brachytherapy dosimetry parameters and may  
676 not account for full-scatter conditions or appropriate scatter  
677 conditions for the task at hand. Thus, the dosimetry investi-  
678 gator should describe the phantom size used in the simula-  
679 tions and should estimate the influence of scatter conditions  
680 over the positions in which dose was calculated. The current  
681 brachytherapy dosimetry formalism,<sup>2</sup> based on the AAPM  
682 TG-43 report,<sup>3</sup> stipulates that MC calculations be performed  
683 in a 15 cm radius liquid water phantom to provide at least 5.0  
684 cm of radiation backscatter for low-energy photon-emitting  
685 sources such as <sup>125</sup>I and <sup>103</sup>Pd at the farthest position from  
686 the source. By the current AAPM definition, low-energy  
687 photon-emitting sources are those which emit photons of en-  
688 ergy less than or equal to 50 keV.<sup>2</sup> Under these circum-  
689 stances for a 50 keV photon-emitting source, approximately  
690 5.0 and 7.5 cm of backscattering material are needed to  
691 simulate infinite scatter conditions within 3% and 1%,  
692 respectively.<sup>53</sup> Thus, the initially recommended 5.0 cm of

backscatter to simulate infinite scatter conditions within 1%  
693 applies only for photon-emitting sources with  $E < 40$  keV.  
694

#### IV.E. Phantom composition

695  
696 Presently, the TG-43 dosimetry formalism does not ac-  
697 count for material heterogeneities and recommends liquid  
698 water as the reference media for specification of *in vivo* dose-  
699 rate distributions. Being a simple and readily available ma-  
700 terial, it is not challenging to simulate the composition  
701 ( $H_2O$ ) and mass density ( $\rho = 0.998$  g/cm<sup>3</sup> at 22 °C) of liq-  
702 uid water. However, care must be taken when the dosimetry  
703 investigator aims to simulate the geometry of a physical ex-  
704 periment. Here, the setup will often include a plastic medium  
705 in place of liquid water. Due to the variable nature in fabri-  
706 cating these plastic media, the dosimetry investigator is ad-  
707 vised to determine the composition and mass density inde-  
708 pendently and assign uncertainties to this assessment.  
709 Furthermore, these uncertainties directly impact the resultant  
710 dosimetric uncertainties, which should be assigned to the  
711 phantom composition. In contrast to phantom size, the MC  
712 dosimetric uncertainties due to phantom composition gener-  
713 ally increase with decreasing photon energy and increase  
714 with increasing radial distance.

715 Specification of a solid phantom material is important for  
716 dosimetric evaluation of brachytherapy sources, particularly  
717 for low-energy photon-emitting sources.<sup>16,55</sup> Meigooni *et al.*  
718 *et al.*<sup>55</sup> showed that a 0.4% difference in the calcium content of  
719 the Solid Water™ phantom material may lead to 5% and 9%  
720 differences in  $\Lambda$  for <sup>125</sup>I and <sup>103</sup>Pd sources, respectively.  
721 These results are in good agreement with the published data  
722 by Patel *et al.*,<sup>56</sup> who performed a robust material analysis of  
723 the phantom composition. In addition, Meigooni *et al.*  
724 showed the impact of the phantom composition on  $g(r)$  for  
725 both <sup>125</sup>I and <sup>103</sup>Pd sources.<sup>55</sup> Small differences in phantom  
726 composition lead to large differences in  $g(r)$  for low-energy  
727 photon emitters. Differences were more significant at larger  
728 depths from the source, and they concluded that one must  
729 use updated correction factors based on correct chemical  
730 composition and cross-section data when extracting a con-  
731 sensus of dosimetric parameters for a brachytherapy source  
732 by means of the TG-43U1 protocol.<sup>2</sup> Dosimetric uncertain-  
733 ties arising from uncertainties in phantom composition are  
734 typically classified as type B.

#### IV.F. Radiation transport code

735  
736 All MC codes use approximations and assumptions when  
737 simulating radiological interactions. For example, generation  
738 of multiple-photon emissions following characteristic x-ray  
739 production may be simplified to the most probable photons,  
740 some MC codes ignore electron binding effects, and electron  
741 transport is often reduced to a multigroup algorithm or ig-  
742 nored entirely. Although molecular form factors can be used  
743 in some codes, there is no significant dosimetric effect when  
744 using an independent-atom approximation for coherent scat-  
745 tering form factors.<sup>54</sup> Specific to the use of radiation trans-  
746 port codes for determining brachytherapy dose-rate distribu-  
747 tions, there is a practical energy limit for simplification to a



748 photon-only transport technique at the exclusion of coupled  
749 photon-electron transport, and high-energy photon-emitting  
750 radionuclides such as  $^{192}\text{Ir}$  and  $^{137}\text{Cs}$  may not be simulated  
751 accurately when close to the source. Electron contributions  
752 to the dosimetric uncertainty could be negligible given accu-  
753 rate transport equations, empirically derived atomic form  
754 factors, and proper implementation of the code by the dosim-  
755 etry investigator. However, dosimetric differences within 1  
756 mm of a  $^{192}\text{Ir}$  source capsule between photon-only and  
757 coupled photon-electron transport may exceed 15%.<sup>49,50,57</sup>  
758 Estimates of  $k=1$  dosimetric uncertainties due to the physics  
759 implementation within MC radiation transport algorithms at  
760  $r=1$  cm are 0.3% and 0.2% for low- and high-energy  
761 sources, respectively, and 0.7% and 0.3% at  $r=5$  cm.<sup>43,47</sup>

#### 762 IV.G. Interaction and scoring cross sections

763 With the computational geometry established, progression  
764 of radiation transport is governed by atomic and nuclear  
765 cross sections that dictate the type and frequency of radio-  
766 logical interactions. These cross sections are organized into  
767 libraries that are maintained by international agencies such  
768 as the NNDC. Uncertainties in the cross sections within the  
769 source affect radiation emitted in the phantom. These cross  
770 sections are typically calculated and compared to experimen-  
771 tal cross sections, determined at discrete energies. Given the  
772 physics model used to characterize the element and radio-  
773 logical interaction, a fitting function (such as a log-log fit) is  
774 used by the radiation transport code to interpolate between  
775 reported cross-section values. Since the interpolation fit may  
776 not be robust for all element and energy possibilities, it is  
777 recommended to use the recently derived cross-section li-  
778 braries with high resolution in energy. Sensitivity of dosim-  
779 etric results on cross-section libraries was illustrated by De-  
780 Marco *et al.*<sup>58</sup>

781 MC-based radiation transport codes utilize  $\mu_{\text{en}}/\rho$  toward  
782 calculating dose rates and are separated from  $\mu/\rho$  as, for  
783 example, one could determine dose to muscle in water in-  
784 stead of dose to water in water. Here, the  $\mu/\rho$  and  $\mu_{\text{en}}/\rho$   
785 values for water and muscle would be used, respectively.  
786 Thus, the uncertainties ( $k=1$ ) in both  $\mu/\rho$  and  $\mu_{\text{en}}/\rho$  are of  
787 concern and are about 1.2% and 1.0% for low- and high-  
788 energy sources, respectively.<sup>59,60</sup> The influence of the cross-  
789 section uncertainties on the absorbed dose is a function of  
790 distance from the source with larger distances subject to  
791 larger dosimetric uncertainties. For low-energy sources, the  
792 dosimetric uncertainties at 0.5 and 5 cm are about 0.08% and  
793 0.76%, respectively; with high-energy sources, dosimetric  
794 uncertainties are 0.01% and 0.12% for these same  
795 distances.<sup>43,47</sup> Further research on a modern assessment of  
796 cross-section uncertainties is needed.

#### 797 IV.H. Scoring algorithms and uncertainties

798 All the prior steps set the simulation framework in which  
799 the calculations are performed. The dosimetry investigator  
800 must select the scoring algorithm used to determine the dose-  
801 rate distributions. While some estimators are more appropri-  
802 ate than others,<sup>61</sup> none will truly represent the desired output

803 resultant from the dosimetry calculations. Typically, some  
804 form of volume averaging or energy-weighted modification  
805 will be used to determine the dose rate at a given location  
806 within the calculation phantom. These uncertainties should  
807 be  $<0.1\%$  for all classes (HDR/LDR and low/high energy)  
808 of brachytherapy sources. For path-length estimators used to  
809 determine collisional kerma, decreases in voxel thickness  
810 along the radial direction will diminish volume averaging  
811 within the voxel without significant influence on the type A  
812 uncertainties.<sup>62</sup> However, MC estimators based on energy  
813 deposition within the voxel will have type A uncertainties  
814 inversely proportional to the square root of the voxel volume  
815 and are thus influenced by voxel thickness along the radial  
816 direction. Derivation of brachytherapy dosimetry parameters  
817 such as  $\Lambda$ ,  $g(r)$ ,  $F(r, \theta)$ , and  $\phi_{\text{an}}(r)$  using MC methods in-  
818 volves the summation of results over various tallied voxels,  
819 weighting results based on solid angle, or taking ratios of  
820 simulated dose rates. Since all brachytherapy dosimetry pa-  
821 rameters are ratios of dose rates, except for  $\Lambda$ , it is often  
822 straightforward to simply take ratios of the raw simulated  
823 results. Systematic uncertainties in postsimulation processing  
824 may arise when energy thresholds  $\delta$ ,<sup>2</sup> intentional volume av-  
825 eraging, or tally energy modifiers are employed. Further re-  
826 search on these uncertainties is needed.

#### 827 V. UNCERTAINTY IN THE TG-43 DOSIMETRY 828 FORMALISM PARAMETERS

829 What follows is a quantitative assessment of dosimetric  
830 uncertainties in the brachytherapy dosimetry parameters used  
831 in the TG-43 dose calculation formalism. The reader is di-  
832 rected to the 2004 AAPM TG-43 report for definitions of the  
833 brachytherapy dosimetry parameters.<sup>2</sup> The tables in the cur-  
834 rent report present best practice values for propagated uncer-  
835 tainties and are not meant to be used for uncertainty budgets.

#### 836 V.A. Air-kerma strength

##### 837 V.A.1. Uncertainty in NIST primary standard for 838 LDR low-energy photon-emitting sources

839 The U.S. national primary standard of air-kerma strength  
840 ( $S_{K,\text{NIST}}$ ) for low-energy ( $\leq 50$  keV) photon-emitting  
841 brachytherapy sources, containing the radionuclide  $^{103}\text{Pd}$ ,  
842  $^{125}\text{I}$ , or  $^{131}\text{Cs}$ , is realized using the NIST wide-angle free-air  
843 chamber (WAFAC).<sup>63</sup> The WAFAC is an automated, free-air  
844 ionization chamber with a variable volume. As of October  
845 2010, over 1000 sources of 41 different designs from 19  
846 manufacturers have been calibrated using the WAFAC since  
847 1999. The expanded uncertainty ( $k=2$ ) in  $S_{K,\text{NIST}}$  is given as

$$848 V_{\text{WAFAC}} = 2\sqrt{(s_i^2 + u_j^2)}, \quad (1)$$

849 where  $s_i$  is equal to the standard deviation of the mean of  
850 replicate measurements (type A) and the quadrature sum of  
851 all type B components of uncertainty is represented by  $u_j$   
852 (less than 0.8%).<sup>64</sup>

853 Following the  $S_{K,\text{NIST}}$  measurement, the responses of sev-  
854 eral well-type ionization chambers of different designs are  
855 measured at NIST. To understand the relationship between

856 well-chamber response  $I$  and WAFAC-measured  $S_{K,NIST}$  for  
 857 low-energy photon brachytherapy sources, emergent photon  
 858 spectra are measured with a high-purity germanium spec-  
 859 trometer. Knowledge of source spectrum allows separation  
 860 of well-chamber response effects due to spectrum differences  
 861 from those caused by variations in the spatial anisotropy of  
 862 emissions due to self-absorption by internal source compo-  
 863 nents. The relative response of calibration instruments has  
 864 been observed to depend on both emergent spectrum and  
 865 anisotropy.<sup>64</sup>

866 To verify that sources of a given design calibrated at  
 867 NIST are representative of the majority of those calibrated in  
 868 the past, several additional tests have been implemented. The  
 869 distribution of radioactive material within a source is  
 870 mapped using radiochromic film contact exposures. The in-  
 871 air anisotropy of sources is studied by taking WAFAC and  
 872 x-ray spectrometry measurements at discrete rotation angles  
 873 about the long axis and the axis perpendicular to the mid-  
 874 point of the source long axis, respectively. The “air-  
 875 anisotropy ratio,” calculated from the results of angular x-ray  
 876 measurements, has proven to be a useful parameter for ex-  
 877 plaining differences in well-chamber response observed for  
 878 different source models having the same emergent spectrum  
 879 on their transverse plane.<sup>65</sup> The first primary standard device  
 880 in Europe for calibration of low-energy photon sources was  
 881 the large-volume extrapolation chamber built at the PTB  
 882 where the procedures are, in principle, the same as at NIST.<sup>66</sup>  
 883 For each seed type (not necessarily for each individual seed  
 884 of same type), the spectral photon distribution to obtain the  
 885 spectrum dependent correction factors for air attenuation,  
 886 scattering, etc., is determined. Details are given in Ref. 66.  
 AQ: 887 Using a sensitive scintillation detector free-in-air at 1 m,  
 #1 888 both polar and azimuthal anisotropies are measured for each  
 889 individual seed to be calibrated. The results of the anisotropy  
 890 measurements are part of the calibration certificate. The NPL  
 891 also provides air-kerma rate calibrations of  $^{125}\text{I}$  sources using  
 892 their secondary standard radionuclide calibrator, a well-type  
 893 ionization chamber for which the calibration coefficient is  
 894 traceable to the NIST primary air-kerma standard.<sup>64</sup>

### 895 V.A.2. Uncertainty in NIST primary standard for LDR 896 high-energy photon-emitting sources

897 The U.S. national primary standard of  $S_{K,NIST}$  for LDR  
 898 high-energy gamma-ray-emitting brachytherapy sources con-  
 899 taining the radionuclide  $^{192}\text{Ir}$  is realized using a spherical  
 900 graphite-wall cavity chamber that is open to the  
 901 atmosphere.<sup>67</sup> Since arrays of approximately 50 sources were  
 902 required to perform the cavity chamber measurement due to  
 903 low detector-sensitivity, the  $S_{K,NIST}$  of individual sources is  
 904 determined by using a spherical-Al re-entrant chamber work-  
 905 ing standard with a  $^{226}\text{Ra}$  source to verify the stability of the  
 906 re-entrant chamber over time. The expanded uncertainty ( $k$   
 907 =2) in  $S_{K,NIST}$  for LDR  $^{192}\text{Ir}$  sources is 2%. Well-chamber  
 908 response is not as sensitive to small changes in source con-  
 909 struction due to manufacturing variability for high-energy  
 910 photon emitters in comparison to low-energy sources.<sup>68</sup> Nev-  
 911 ertheless, additional characterization measurements are per-

912 formed on the sources following calibration, including well-  
 913 chamber response, photon spectrometry, and radiochromic  
 914 film contact exposure measurements. The results of these  
 915 measurements are used to verify that no significant modifi-  
 916 cations to the LDR low-energy source design have been  
 917 implemented by the manufacturer.

918 Similar to  $^{192}\text{Ir}$ , the U.S. national primary standard of  
 919  $S_{K,NIST}$  for LDR high-energy photon-emitting brachytherapy  
 920 sources containing  $^{137}\text{Cs}$  is also realized using a spherical  
 921 graphite-wall cavity chamber that is open to the  
 922 atmosphere.<sup>69</sup> For routine calibrations, a spherical-Al cavity  
 923 chamber with several  $^{137}\text{Cs}$  working standard sources is  
 924 used. The expanded uncertainty ( $k=2$ ) in  $S_{K,NIST}$  for LDR  
 925  $^{137}\text{Cs}$  sources is 2%. As is the case with LDR  $^{192}\text{Ir}$  sources,  
 926 well-chamber response is relatively insensitive to small  
 927 changes in source construction. Additional characterization  
 928 measurements performed on the sources following calibra-  
 929 tion include well-chamber response and radiochromic film  
 930 contact exposure measurements.<sup>70</sup>

931 At NPL, air-kerma rate calibrations are performed for  
 932  $^{192}\text{Ir}$  wires and pins using the secondary standard radionu-  
 933 clide calibrator, which is traceable to the NPL air-kerma pri-  
 934 mary standard. The expanded uncertainty ( $k=2$ ) for an  $^{192}\text{Ir}$   
 935 air-kerma rate measurement is stated to be 1.5%.<sup>66</sup>

### 936 V.A.3. $S_K$ uncertainty for HDR high-energy sources

937 NIST traceability for the measurement of air-kerma  
 938 strength for HDR  $^{192}\text{Ir}$  sources is based on the interpolation  
 939 of air-kerma calibration coefficients of a secondary standard  
 940 ionization chamber.<sup>71</sup> The weighted average-energy of these  
 941 sources is 397 keV and thus an interpolated value between  
 942 the calibration points of  $^{137}\text{Cs}$  and 250 kVp x rays is used.  
 943 However, more rigorous methodologies for the ionization  
 944 chamber  $^{192}\text{Ir}$  air-kerma calibration coefficient have been  
 945 suggested,<sup>72,73</sup> with Eq. (2) from Eq. (1) of Ref. 72,

$$946 \frac{1}{N_{S_K}^{\text{Ir-192}}} = \frac{1}{2} \left( \frac{1}{N_K^{\text{Cs-137}}} + \frac{1}{N_K^{\text{x ray}}} \right), \quad (2)$$

947 which results in agreement within 0.5%, falling within the  
 948 2.15 % uncertainty ( $k=2$ ).  $N_{S_K}^{\text{Ir-192}}$  is the ionization chamber  
 949 air-kerma calibration coefficient for  $^{192}\text{Ir}$  (or as designated  
 950  $^{137}\text{Cs}$  or x ray).

951 There are two techniques to measure  $S_K$  using an ioniza-  
 952 tion chamber calibrated as above, the shadow shield method  
 953 and the seven-distance technique. The seven-distance tech-  
 954 nique has been refined and the results for  $S_K$  from all HDR  
 955  $^{192}\text{Ir}$  source manufacturers have been found to agree to  
 956 within 0.5%.<sup>74</sup> Air-kerma strength is thus given as

$$957 S_K = \frac{N_{S_K}^{\text{Ir-192}}(M_d - M_s)(d + c)^2}{\Delta t}, \quad (3)$$

958 where  $N_{S_K}^{\text{Ir-192}}$  is the air-kerma calibration coefficient for  $^{192}\text{Ir}$ ,  
 959  $M_d$  is the direct measurement including the primary beam  
 960 scatter  $M_s$ , distance to the source center  $d$ , setup distance  
 961 error  $c$ , and irradiation time  $\Delta t$ . The value of  $S_K$  is then  
 962 transferred to a well-type ionization chamber.

963 HDR  $^{192}\text{Ir}$  air-kerma standards are established at LNHB,  
 964 PTB, and NPL.<sup>75</sup> An intercomparison of the University of  
 965 Wisconsin Accredited Dosimetry Calibration Laboratory  
 966 (ADCL) calibration standard with the LNHB calibration  
 967 standard showed agreement for a specific HDR  $^{192}\text{Ir}$  source  
 968 within 0.3%.<sup>76</sup> Intercomparisons done between NPL and  
 969 LNHB demonstrated agreement to within 0.3% to 0.5%.<sup>77</sup>  
 970 When uncertainty analysis is performed for all other HDR  
 971  $^{192}\text{Ir}$  source models and intercomparisons, the overall ex-  
 972 panded uncertainty ( $k=2$ ) for  $S_K$  is 2.15%.<sup>73,74</sup> LNHB  
 973 achieves a HDR  $^{192}\text{Ir}$  calibration uncertainty ( $k=2$ ) of 1.3%  
 974 for well-type ionization chambers.<sup>76</sup> Given the assortment of  
 975 HDR high-energy sources and a variety of calibration meth-  
 976 ods used at the various primary standards laboratories, the  
 977 aforementioned calibration uncertainties are not necessarily  
 978 indicative for other sources or other laboratories.

#### 979 **V.A.4. Transfer of NIST standard to the ADCLs**

980 The AAPM ADCLs are responsible for transferring a  
 981 traceable calibration coefficient to the clinics. Therefore, the  
 982 ADCLs maintain secondary air-kerma strength standards us-  
 983 ing well-type ionization chambers, which are directly trace-  
 984 able to NIST to a great precision and add about 0.1% to the  
 985 uncertainty budget. The AAPM Calibration Laboratory Ac-  
 986 creditation subcommittee monitors this traceability. ADCLs  
 987 establish their on-site secondary standard by measuring the  
 988 response of a well chamber to a NIST-calibrated source. The  
 989 ratio of air-kerma strength  $S_K$  to  $I$  yields a calibration coef-  
 990 ficient for a given source type. The ADCLs use their cali-  
 991 brated well chamber and manufacturer-supplied sources to  
 992 calibrate well chambers for clinics. Calibrations of electrom-  
 993 eters and instruments monitoring atmospheric conditions are  
 994 also necessary to complete the system. Intercomparisons  
 995 among ADCLs and proficiency tests with NIST ensure that  
 996 each ADCL is accurate in its dissemination, and that the  
 997 calibrations from different ADCLs are equivalent. Europe  
 998 does not yet have the same scale of infrastructure for low-  
 999 energy source calibrations as does the U.S.

1000 For LDR low-energy photon-emitting brachytherapy  
 1001 sources, the NIST air-kerma strength standard for each new  
 1002 source model is initially transferred to all ADCLs that are  
 1003 accredited by the AAPM to perform brachytherapy source  
 1004 calibrations by sending a batch of three WAFAC-calibrated  
 1005 sources, in turn, to each ADCL. To ensure that the NIST-  
 1006 traceable standard at each ADCL remains consistent over  
 1007 time with the initial baseline values, subsequent batches of  
 1008 three sources of each model are calibrated by NIST and cir-  
 1009 culated among all ADCLs at least annually.<sup>78</sup> Supplementary  
 1010 measurements performed at NIST, including  $I$ , photon spec-  
 1011 trometry, and anisotropy characterization, provide quality as-  
 1012 surance (QA) checks for WAFAC measurements as well as  
 1013 the ability to monitor possible modifications in LDR low-  
 1014 energy seed construction. Data from NIST, the ADCLs, and  
 1015 the source manufacturer for each seed model are plotted as a  
 1016 function of time such that the integrity of the measurement  
 1017 traceability chain is verified. This process provides assurance  
 1018 that any ADCL secondary standard has not changed since the

initial transfer within the uncertainty level, serving as a  
 monitor for consistency. Based on the data collected by NIST  
 and the ADCLs over many years, it appears that the accuracy  
 achievable in a secondary standard is not the same for all  
 source models. Variations in emergent spectrum and spatial  
 anisotropy of emissions influence well chamber to WAFAC  
 response ratios, and how well such variations are minimized  
 during source fabrication affects the magnitude of variability  
 in well-chamber measurements for sources of supposedly  
 identical construction.

A NIST-traceable air-kerma strength standard for both  
 high-energy gamma-ray-emitting brachytherapy sources (i.e.,  
 $^{192}\text{Ir}$  and  $^{137}\text{Cs}$ ) has been available from all ADCLs for many  
 years. The continued accuracy of the secondary standards is  
 verified through the performance of periodic measurement  
 quality assurance tests. Recommendations have been pub-  
 lished, specifying that a check of the accuracy of manufac-  
 turer source or equipment calibrations be verified by either  
 NIST or an AAPM-accredited ADCL on an annual basis.<sup>78</sup>

#### **V.A.5. Transfer of NIST standard from ADCLs to the clinic**

The use of an ADCL-calibrated well-ionization chamber  
 is the usual manner for clinics to measure the strength of  
 their brachytherapy sources. Therefore, the uncertainty in the  
 well-chamber calibration coefficient for the specific type of  
 source used is the key component that creates the final un-  
 certainty in the air-kerma strength measured at the clinic.

Following the primary standard measurement of air-  
 kerma strength ( $S_{K,NIST}$ ), the response (usually a measured  
 current  $I$ ) of a well-ionization chamber is determined. The  
 $S_K/I$  ratio yields a calibration coefficient for the well-  
 ionization chamber for a given source type. Such calibration  
 coefficients enable well-ionization chambers to be employed  
 at therapy clinics for calibration of source air-kerma strength.  
 To model the traceability of measurements performed on  
 brachytherapy sources from the primary standard measure-  
 ment of air-kerma strength at NIST to the transfer of this  
 standard to the ADCLs and source manufacturers to a final  
 verification of source strength at a therapy clinic prior to  
 their use in treatment, uncertainties have been assigned  
 (based on NIST measurement histories) to  $S_{K,NIST}$  and  $I$  as  
 $\%u_{c,WAFAC}=0.8\%$  ( $k=1$ ) and  $\%u_{c,I}=0.5\%$  ( $k=1$ ). These val-  
 ues are propagated through the measurement traceability  
 chain in two paths, the first of which is shown in Table I.  
 Although this model is applied to measurements of a single  
 low-energy photon-emitting source, the same analysis may  
 be applied to high-energy photon-emitting sources by using  
 the appropriate  $u_c$  values.

In row 1 of Table I, the air-kerma strength  $S_{K,NIST}$  of a  
 source is measured, which is then sent to an ADCL. The  
 response of an ADCL standard well-ionization chamber is  
 measured, yielding a current  $I_{ADCL}$ . A calibration coefficient  
 for the chamber  $S_{K,NIST}/I_{ADCL}$  is then calculated (row 2). The  
 ADCL receives a source from the manufacturer (row 3), and  
 the air-kerma strength  $S_{K,ADCL}$  is calculated based on the  
 standard well-chamber current measurement and the calibra-

TABLE I. Propagation of best practice uncertainties ( $k=1$  unless stated otherwise) associated with the transfer of air-kerma strength from NIST through the ADCL to the clinic for LDR low-energy brachytherapy sources.

Row	Measurement description	Quantity (units)	Relative propagated uncertainty (%)
1	NIST WAFAC calibration	$S_{K,NIST}$ (U)	0.8
2	ADCL well ion chamber calibration	$S_{K,NIST}/I_{ADCL}$ (U/A)	0.9
3	ADCL calibration of source from manufacturer	$S_{K,ADCL}$ (U)	1.1
4	ADCL calibration of clinic well ion chamber	$S_{K,ADCL}/I_{CLINIC}$ (U/A)	1.2
5	Clinic measures source air-kerma strength	$S_{K,CLINIC}$ (U)	1.3
	Expanded uncertainty ( $k=2$ )	$S_{K,CLINIC}$ (U)	2.6

1075 tion coefficient for the chamber. To transfer the source cali-  
 1076 bration to the clinic, a well chamber from the clinic is sent to  
 1077 an ADCL, where the calibration coefficient  $S_{K,ADCL}/I_{CLINIC}$   
 1078 is determined (row 4). Finally, in row 5, the well-chamber  
 1079 ionization current is measured and multiplied by the calibra-  
 1080 tion coefficient, yielding an air-kerma strength  $S_{K,CLINIC}$  for  
 1081 the clinical source. According to this model, the propagation  
 1082 of uncertainties from the various well-chamber measure-  
 1083 ments involved in the transfer of the source-strength standard  
 1084 to the clinic results in a minimum expanded uncertainty ( $k$   
 1085  $=2$ ) in  $S_{K,CLINIC}$  of 2.56%. This level of uncertainty assumes  
 1086 that the clinic is measuring a single seed with a high-quality  
 1087 electrometer and other reference-quality measurement equip-  
 1088 ment. An alternate method of calibration, instead of the well-  
 1089 chamber calibration, is for the clinic to purchase a source and  
 1090 send it to the ADCL for calibration. When this calibrated  
 1091 source is sent to the clinic, it is used to calibrate the clinic's  
 1092 well chamber. This procedure results in an additional uncer-  
 1093 tainty of 0.6%, resulting in a total uncertainty of 2.83% at  
 1094  $k=2$ .

1095 The second path of the measurement traceability chain is  
 1096 illustrated in Table II. Following measurement of air-kerma  
 1097 strength  $S_{K,NIST}$  at NIST, a source is returned to the manu-  
 1098 facturer. The response of a manufacturer's well-ionization  
 1099 chamber is measured, yielding a current  $I_M$ . A calibration  
 1100 coefficient for the chamber  $S_{K,NIST}/I_M$  is then calculated (row  
 1101 2). For QA purposes, the air-kerma strength  $S_{K,M}$  of a refer-  
 1102 ence source is calculated based on well-chamber current  
 1103 measurements and the chamber calibration coefficient (row  
 1104 3). This reference source is used to determine the calibration  
 1105 coefficient  $S_{K,M}/I_M$  for a well-ionization chamber located on

the source production line (row 4). To verify source strength  
 as part of the production process, the well-chamber ioniza-  
 tion current is measured and multiplied by the calibration  
 coefficient, yielding an air-kerma strength  $S_{K,M}$  for the source  
 (row 5). Finally, in row 6, the source is placed in a 2% wide  
 bin with other sources of air-kerma strength  $S_{K,M \text{ bin}} \pm 1\%$ .  
 Some manufacturers have larger bin sizes, up to 7% wide.  
 Therefore, a range is included in row 6 of Table II to account  
 for the range in bin sizes. The source is then sent to a clinic  
 for patient treatment. According to this model, the propaga-  
 tion of uncertainties from the various well-chamber measure-  
 ments involved in the transfer of the source-strength standard  
 to the manufacturer, including binning, results in a minimum  
 expanded uncertainty ( $k=2$ ) in  $S_{K,M \text{ bin}}$  of 2.83%. To evalu-  
 ate the uncertainty due to binning, the binning process is  
 treated as an additive perturbation such that

$$S_{K,M \text{ bin}} = S_{K,M} + B, \quad (4)$$

where  $B$  is the bias associated with placing a seed of air-  
 kerma strength  $S_{K,M}$  in a bin of center value  $S_{K,M \text{ bin}}$ . The bin  
 width is modeled by a rectangular distribution, yielding a  
 component of uncertainty due to binning of 0.6% for a 2%  
 wide bin and 2.0% for a 7% wide bin. The minimum uncer-  
 tainty in  $S_{K,M \text{ bin}}$  ( $k=2$ ) is therefore 2.81%, increasing to  
 4.78% for the widest bin in this model (row 6 in Table II).

Now the question may be asked, "How well should the  
 clinical determination of source air-kerma strength  
 ( $S_{K,CLINIC}$ ) based on an ionization current measurement in a  
 calibrated well chamber agree with the value ( $S_{K,M \text{ bin}}$ ) pro-  
 vided by the manufacturer?" To answer this question, one  
 must first establish a source acceptance criterion. One possi-

TABLE II. Propagation of best practice uncertainties ( $k=1$  unless stated otherwise) associated with the transfer of the air-kerma strength standard from NIST to the manufacturer for LDR low-energy brachytherapy sources.

Row	Measurement description	Quantity (units)	Relative propagated uncertainty (%)
1	NIST WAFAC calibration	$S_{K,NIST}$ (U)	0.8
2	Manufacturer well ion chamber calibration	$S_{K,NIST}/I_M$ (U/A)	0.9
3	Manufacturer calibration of QA source	$S_{K,M}$ (U)	1.1
4	Manufacturer instrument calibration for assay	$S_{K,M}/I_M$ (U/A)	1.2
5	Manufacturer assays production sources	$S_{K,M}$ (U)	1.3
6	Manufacturer places sources in 2% or 7% bins	$S_{K,M \text{ bin}}$ (U)	1.4 or 2.4
	Expanded uncertainty ( $k=2$ )	$S_{K,M \text{ bin}}$ (U)	2.8 or 4.8

TABLE III. Propagation of best practice uncertainties ( $k=1$  unless stated otherwise) associated with the transfer of air-kerma strength from NIST through the ADCL to the clinic for LDR high-energy brachytherapy sources. Well-chamber measurement uncertainty is estimated to be 0.5 %.

Row	Measurement description	Quantity (units)	Relative propagated uncertainty (%)
1	NIST calibration	$S_{K,NIST}$ (U)	1.0
2	ADCL well ion chamber calibration	$S_{K,NIST}/I_{ADCL}$ (U/A)	1.1
3	ADCL calibration of source from manufacturer	$S_{K,ADCL}$ (U)	1.2
4	ADCL calibration of clinic well ion chamber	$S_{K,ADCL}/I_{CLINIC}$ (U/A)	1.3
5	Clinic measures source air-kerma strength	$S_{K,CLINIC}$ (U)	1.4
	Expanded uncertainty ( $k=2$ )	$S_{K,CLINIC}$ (U)	2.8

1136 bility is to require that the absolute value of the difference  
1137 between the air-kerma strength stated by the manufacturer  
1138  $S_{K,M \text{ bin}}$  and that determined by the clinic  $S_{K,CLINIC}$  be less  
1139 than the propagated uncertainty of that difference with an  
1140 appropriate coverage factor according to

$$|S_{K,CLINIC} - S_{K,M \text{ bin}}| < \sqrt{V_{S_{K,CLINIC}}^2 + V_{S_{K,M \text{ bin}}}^2 - V_{S_{K,WAFAC}}^2}. \quad (5)$$

1141

1142 Since  $V_{S_{K,WAFAC}}$  is common to both paths of the measure-  
1143 ment traceability chain, it is removed (in quadrature) so as  
1144 not to be added twice. Using the uncertainties determined  
1145 from the model at the ends of the two paths of the measure-  
1146 ment traceability chain,  $S_{K,CLINIC}$  must agree with  $S_{K,M \text{ bin}}$  to  
1147 within 3.4% (assuming 2% bins) in order for the source to be  
1148 acceptable for use by the clinic. This result is for a set of  
1149 measurements made on a single source and does not include  
1150 uncertainties due to source-to-source variability. Thus, 3.4%  
1151 is the lower limit for the source acceptance criterion. Crite-  
1152 rion for acceptance of calibration is discussed in Ref. 79,  
1153 where the lower-third of its Table II for 100% source assay is  
1154 directly comparable to Table II of the current report.

1155 In the case of high-energy sources, the procedure is simi-  
1156 lar to that given above with some minor differences. For  
1157 LDR high-energy sources, there are long-lived sources, such  
1158 as  $^{137}\text{Cs}$ , and shorter-lived sources, such as  $^{192}\text{Ir}$  sources.  
1159 Table III is presented for the clinic measurement uncertainty  
1160 with an ADCL-calibrated well-ionization chamber and is cer-  
1161 tainly appropriate for a short-lived source. Following the

same model of uncertainty propagation as above (assuming 1162  
1163  $\%u_{c,i}=0.5\%$  for each well-chamber measurement), the mini- 1164  
1165 mum expanded uncertainty ( $k=2$ ) of clinical air-kerma 1166  
1167 strength measurements for LDR high-energy sources is 2.8% 1168  
1169 (Table III). In the case of a long-lived source, the original 1170  
1171 NIST-calibrated source may be used, in which case, rows 2 1172  
1173 and 3 are not present. In this case, the uncertainty in the 1174  
1175 ADCL calibration of the clinic well chamber is 1.12% and 1176  
1177 the uncertainty in the clinical measurement is 1.22%, with 1178  
1179 the expanded uncertainty of 2.45% ( $k=2$ ). The HDR high- 1180  
1181 energy sources have a NIST-traceable calibration through an 1182  
1183 interpolated calibration coefficient from two photon beams 1184  
1185 as given in Ref. 71. Following the same model of uncertainty 1186  
1187 propagation as above (assuming 0.5% uncertainty on each 1188  
1189 well-chamber measurement), the minimum expanded uncer- 1190  
1191 tainty ( $k=2$ ) of clinical  $S_K$  measurements for HDR high- 1192  
1193 energy sources is 2.94% from Table IV. 1194

## V.B. Dose-rate constant 1179

As  $\Lambda$  is defined as the ratio of dose rate at the reference 1180  
1181 position to the air-kerma strength,  $\Lambda \equiv \dot{D}(r_0, \theta_0)/S_K$ , the  $\Lambda$  1182  
1183 uncertainty is simply 1184

$$\%u_{\Lambda} = \sqrt{\%u_{\dot{D}(r_0, \theta_0)}^2 + \%u_{S_K}^2}. \quad (6) \quad 1183$$

While Sec. V A 5 discussed  $u_{S_{K,CLINIC}}$ , clinical users do not 1184  
1185 measure the reference dose rate and thus do not directly ob- 1186  
1187 tain  $\%u_{\Lambda}$ . Instead,  $\%u_{\Lambda}$  values are taken from the literature 1188

TABLE IV. Propagation of best practice uncertainties ( $k=1$  unless stated otherwise) associated with the transfer of air-kerma strength from a traceable NIST coefficient from the ADCL to the clinic for HDR high-energy brachytherapy sources.

Row	Measurement description	Quantity (units)	Relative propagated uncertainty (%)
1	ADCL calibration	$S_{K,NIST}$ (U)	1.1
2	ADCL well ion chamber calibration	$S_{K,NIST}/I_{ADCL}$ (U/A)	1.2
3	ADCL calibration of source from manufacturer	$S_{K,ADCL}$ (U)	1.3
4	ADCL calibration of clinic well ion chamber	$S_{K,ADCL}/I_{CLINIC}$ (U/A)	1.4
5	Clinic measures source air-kerma strength	$S_{K,CLINIC}$ (U)	1.5
	Expanded uncertainty ( $k=2$ )	$S_{K,CLINIC}$ (U)	2.9

of dosimetry investigators upon deriving  $\Lambda$ . For instances, when the AAPM issues consensus datasets,  $\Lambda$  and  $\%u_{\Lambda}$  consensus values may be provided with  $\%u_{\Lambda}$  values generally smaller than the individual investigator  $\%u_{\Lambda}$  value due to increased sampling of candidate datasets. For low- and high-energy photon-emitting brachytherapy sources, the measured values of  $\%u_{\Lambda}$  ( $k=1$ ) are approximately 2.9%; MC-simulated values of  $\%u_{\Lambda}$  ( $k=1$ ) are approximately 2.1%.

### V.C. Geometry function

The geometry function is dependent on  $L$  (or effective length),  $r$ , and  $\theta$ . Since  $L$  is primarily used to minimize interpolation errors during treatment planning, it can take on almost any value.<sup>62,80,81</sup> However, realistic dose distributions are usually best-approximated through using realistic  $L$  values. In practice, the geometry function is used by dosimetry investigators to determine other parameters such as  $g(r)$  and  $F(r, \theta)$ . In both cases, the geometry function is used to remove the effects of solid angle when evaluating measurements or calculations of dose rate around a source. Consequently, the geometry function appears in both the numerator and the denominator of the expressions used to determine these parameters. A proper uncertainty analysis will recognize the artificial decoupling of the TG-43 brachytherapy dosimetry parameters, and that the geometry function cancels out once dose-rate values are obtained in the TPS as long as it is used consistently in the other parameters such as  $g(r)$  and  $F(r, \theta)$ . Variability in dose measurements resulting from the associated variability in source positioning contributes to dosimetric uncertainties, not geometry function uncertainties. Thus, the practical implementation of the geometry function means there is no associated uncertainty. That is,  $\%u_{G(r, \theta)} = 0$ . While sources of a given model have  $L$  variations, these variations manifest themselves with physical dose rates and other parameters because a single consistent  $L$  is used for a given source model.<sup>81</sup>

### V.D. Radial dose function

The radial dose function uncertainty is the square root of the sum of the squares of the relative dose-rate uncertainties at the reference position and point of interest on the transverse plane. In Sec. V C, it was shown that the geometry function uncertainty was zero. Thus,

$$\%u_{g(r)} = \sqrt{\%u_{\dot{D}(r_0, \theta_0)}^2 + \%u_{\dot{D}(r, \theta_0)}^2}. \quad (7)$$

In general, the uncertainty increases for large  $r$  (more for low-energy sources where attenuation is greater) and for small  $r$  (based on dosimetric uncertainties close to the source). Estimates of this type B uncertainty are based on the experience gained through the derivation of a large number of AAPM consensus datasets from candidate datasets.<sup>2</sup> For  $0.5 \text{ cm} \leq r \leq 5 \text{ cm}$ , low- and high-energy photon-emitting brachytherapy source measured values of  $\%u_{g(r)}$  ( $k=1$ ) are approximately 2% and 1%, respectively; MC-simulated values of  $\%u_{g(r)}$  ( $k=1$ ) are approximately 1% and 0.5%, respectively. These dose uncertainties increase for  $r < 0.5 \text{ cm}$  due

to the influence of dynamic internal components and for  $r > 5 \text{ cm}$  due to cross-section uncertainties in the phantom material.

### V.E. 2D anisotropy function

The 2D anisotropy function uncertainty is the square root of the sum of the squares of the relative dose-rate and geometry function uncertainties. It was shown that the geometry function uncertainty was zero in Sec. V C. Thus,

$$\%u_{F(r, \theta)} = \sqrt{\%u_{\dot{D}(r, \theta)}^2 + \%u_{\dot{D}(r, \theta_0)}^2}. \quad (8)$$

In general, the uncertainty increases with increasing  $r$  and when  $\theta$  approaches the long axis of the source due to diminished dose rates. As  $\theta$  approaches  $90^\circ$ ,  $\%u_{F(r, \theta)}$  approaches zero. The numerator and denominator of  $F(r, \theta)$  share the same  $r$ , and uncertainties due to cross section or medium corrections are minimized. Estimates of this type B uncertainty are based on the experience gained through the derivation of a large number of AAPM consensus datasets from candidate datasets.<sup>2</sup> For low- and high-energy sources, measured  $\%u_{F(r, \theta)}$  ( $k=1$ ) uncertainties are approximately 2.4% and 1.3%, respectively; MC-simulated values of  $\%u_{F(r, \theta)}$  ( $k=1$ ) are approximately 1.1% and 0.6%, respectively. These uncertainties are weighted over all polar angles and are substantially larger near the source long axis where dynamic internal components may cause large dose variations.

### V.F. 1D anisotropy function

Since the 1D anisotropy function is the average of the dose rate around the source at a given  $r$  divided by the dose rate on the transverse plane at the same  $r$ , it is a relative function just like  $g(r)$  and  $F(r, \theta)$ . Because of the volume averaging, it is more complicated to express the dosimetric uncertainty at a given radius since the  $4\pi \text{ sr}$  averaging may require exclusion of the capsule. However, its expression is similar to that for the 2D anisotropy function,

$$\%u_{\phi_{\text{an}}(r)} = \sqrt{\%u_{\int \dot{D}(r, \theta) d\theta}^2 + \%u_{\dot{D}(r, \theta_0)}^2}. \quad (9)$$

In practice,  $\%u_{\phi_{\text{an}}(r)}$  is less than  $\%u_{F(r, \theta)}$  due to diminishment of positioning uncertainties due to volume/angular averaging. As for  $g(r)$  and  $F(r, q)$ , uncertainties increase for large  $r$  (diminishment of dose rate) and for small  $r$  based on dosimetric uncertainties close to the source. Estimates are based on the determination of  $F(r, q)$  uncertainty (Sec. V E). For low- and high-energy sources, measured  $\%u_{\phi_{\text{an}}(r)}$  ( $k=1$ ) uncertainties are approximately 1.5% and 1.1%, respectively; MC-simulated values of  $\%u_{\phi_{\text{an}}(r)}$  ( $k=1$ ) are approximately 0.6% and 0.4%, respectively.

### V.G. TPS uncertainties summary

The uncertainty in TPS-calculated dose will be based on the combination of uncertainties of NIST-traceable  $S_K$  and the dose rates determined by the dosimetry investigator. However, there are additional uncertainties introduced by the TPS.

TABLE V. Propagation of best practice uncertainties ( $k=1$  unless stated otherwise) in dose at 1 cm on the transverse plane associated with source-strength measurements at the clinic, brachytherapy dose measurements or simulation estimates, and treatment planning system dataset interpolation for low-energy (*low-E*) and high-energy (*high-E*) brachytherapy sources as relating to values presented in Fig. 1.

Row	Uncertainty component	Relative propagated uncertainty (%)	
		<i>Low-E</i>	<i>High-E</i>
1	$S_K$ measurements from row 5 of Tables I and IV	1.3	1.5
2	Measured dose	3.6	3.0
3	Monte Carlo dose estimate	1.7	1.6
4	TPS interpolation uncertainties	3.8	2.6
5	Total dose calculation uncertainty	4.4	3.4
	Expanded uncertainty ( $k=2$ )	8.7	6.8

1290 Commissioning of the brachytherapy source for dose cal-  
 1291 culations requires the physicist or other responsible person to  
 1292 install source characterization data into the TPS computer.  
 1293 Since primary calculations for patient treatment are almost  
 1294 never performed today using manual methods, other than for  
 1295 a check, the uncertainty associated with manual calculations  
 1296 will not be discussed. Therefore, the question becomes, what  
 1297 additional uncertainty is associated with the installation of  
 1298 source characterization data, and the use of those data in the  
 1299 TPS, to calculate dose distributions?

1300 When dosimetry parameters are entered, the frequency  
 1301 and spacing of the data are the keys since the TPS performs  
 1302 interpolation on the entered data. Unless spacing varies in  
 1303 inverse proportion to the contribution of a parameter, the  
 1304 uncertainty is likely to be different at different distances.  
 1305 When fits to experimental- or MC-derived dosimetry param-  
 1306 eters are entered, the uncertainty relates to the quality of the  
 1307 fit. The fit approach and model used will affect the uncer-  
 1308 tainty. Further, the TPS dose calculation uncertainty depends  
 1309 on the implementation of the algorithm, the calculation ma-  
 1310 trix spacing, and the veracity of the output mechanisms.  
 1311 Consequently, it is impossible to determine explicitly the un-  
 1312 certainty introduced by model fitting and interpolation.  
 1313 Based on the experience gained through the derivation of a  
 1314 large number of AAPM consensus datasets from candidate  
 1315 datasets,<sup>2</sup>  $\%u_{\text{TPS}}$  values ( $k=1$ , type B) of 3.8% and 2.6% are  
 1316 recommended for low- and high-energy sources, respec-  
 1317 tively, unless specific data indicate otherwise. These values  
 1318 are slightly higher than the 2% ( $k=1$ ) value in the 2004  
 1319 TG-43U1 report which, pertained to individual dosimetry pa-  
 1320 rameters.

1321 Propagating the uncertainties from all components (see  
 1322 Sec. V and Table V) to obtain the dose at 1 cm on the  
 1323 brachytherapy source transverse plane, the  $k=2$  uncertainties  
 1324 for low- and high-energy sources are  $\%V_D=8.7\%$  and  $\%V_D$   
 1325  $=6.8\%$ , respectively. Note that these uncertainty estimates  
 1326 are generalized for the broad variety of available sources in  
 1327 each source photon energy classification and are restricted to  
 1328 single-source dose distributions in a standardized liquid wa-  
 1329 ter spherical phantom.

## 1330 VI. RECOMMENDATIONS 1330

1331 Uncertainty analyses should include all dosimetric prop- 1331  
 1332 erties of clinical brachytherapy sources and follow a com- 1332  
 1333 mon set of guidelines and principles, analogous to TG-43 1333  
 1334 parameters for brachytherapy sources. We recommend fol- 1334  
 1335 lowing the principles described in Secs. I and II of the cur- 1335  
 1336 rent report. This will provide more accurate and meaningful 1336  
 1337 determination of dose in treatment plans and facilitate com- 1337  
 1338 parison between multiple investigators. The goal is to quan- 1338  
 1339 tify overall uncertainty in the delivered dose and maintain it 1339  
 1340 at the lowest possible level. 1340

### 1341 VI.A. General uncertainty 1341

1342 Uncertainty analyses should be performed using a univer- 1342  
 1343 sal methodology. The recommended methodology (i.e., 1343  
 1344 GUM) was described in detail in Sec. II of the current report 1344  
 1345 and is fully documented in NIST Technical Note 1297.<sup>10</sup> 1345  
 1346 AAPM/GEC-ESTRO recommends that when reporting un- 1346  
 1347 certainties of physical quantities relevant to brachytherapy 1347  
 1348 (e.g., air-kerma strength, absorbed dose, and dose rate), the 1348  
 1349 expanded uncertainty should be given along with the mea- 1349  
 1350 sured value of the quantity using a coverage factor of 2 1350  
 1351 ( $k=2$ ). Moreover, the current report has adopted the symbol 1351  
 1352  $V$  to indicate expanded uncertainty to avoid confusion with 1352  
 1353 the symbol  $U$ , which is commonly used by the medical phys- 1353  
 1354 ics community to indicate  $S_K$  units. In addition, all compo- 1354  
 1355 nents of uncertainty, identified as type A or type B, should be 1355  
 1356 tabulated along with the calculated value of the combined 1356  
 1357 standard uncertainty. The statistical methods used to obtain 1357  
 1358 the various components of  $u_c$  should be described in detail, 1358  
 1359 and a *level of confidence* interpretation of the results may be 1359  
 1360 included, if appropriate. 1360

### 1361 VI.B. Clinical medical physicists 1361

#### 1362 VI.B.1. $S_K$ and TPS data entry 1362

1363 To minimize uncertainties, clinical medical physicists 1363  
 1364 should use the consensus brachytherapy dosimetry data. The 1364  
 1365 use of nonconsensus data would lead to a mistake (see Sec. 1365

1366 II) rather than an increase in uncertainties. The primary aspects under control by the clinical medical physicist are measurements of  $S_K$  and TPS data entry. For the first aspect, the clinical medical physicist should follow the 2008 AAPM brachytherapy source calibration recommendations.<sup>79</sup> For TPS data entry, the physicist should carefully consider the recommendations of Sec. V G and avoid inadvertently increasing the uncertainties by, for example, deviating from the numerical or spatial resolution of the AAPM-recommended consensus dataset.<sup>2</sup> Here, the 2% tolerances associated with dataset interpolation may increase with a coarser dataset. Another example of a local uncertainty exceeding the best practice values in the current report would be the use of a novel source with a calibration certificate indicating higher  $S_K$  uncertainties than presented in Sec. V A.

### 1381 VI.B.2. Treatment planning system developments

1382 It is important for the clinical medical physicist to keep an eye toward the future regarding efforts to improve the current TG-43 dose calculation formalism. These improvements might include development of dose calculation algorithms to account for intersource attenuation, phantom scatter, and material heterogeneities.<sup>7</sup> Currently, there is an infrastructure in place for dosimetry investigators, source manufacturers, TPS manufacturers, clinical medical physicists, and professional societies to promote consistent usage of a standardized dataset (i.e., TG-43 dosimetry parameters) for a single-source model. As dose calculation algorithms become more sophisticated, these standardized datasets will no longer be directly used for derivation of patient dose.<sup>82</sup> Consequently, the clinical medical physicist must note the changes in dose calculation uncertainty as TPS manufacturers migrate toward more sophisticated algorithms.

### 1398 VI.B.3. Clinical dosimetric uncertainties

1399 While lower uncertainties are clearly better, what maximum uncertainty should be clinically acceptable? Like the joint ABS/ACMP/ACRO report,<sup>83</sup> the AAPM and GEC-ESTRO also recommend actions be taken to reduce the uncertainty in dose delivery for a particular patient implant such as applicator repositioning, written directive adjustment, or procedure termination. However, the AAPM and GEC-ESTRO recognize that at this time the clinical medical physicist is unlikely to be able to accurately determine the dosimetric uncertainties in multiple sources because no specific recommendations have been published. Clinical practice recommendations on the uncertainty of the dose deviation have not been previously provided. Table V summarizes dosimetric uncertainty contributions that lead to an overall expanded uncertainty of less than 10% ( $k=2$ ) for conventional photon-emitting brachytherapy sources. Yet there may be sources in which these dosimetric uncertainties are larger, such as when using investigational sources that lack a robust source-strength calibration traceable to a primary standards laboratory, or for sources whose calibration carries uncertainties larger than those in row 1 of Table V due to design variations and subsequent energy differences.<sup>84</sup> These cir-

cumstances and other factors may result in increased dosimetric uncertainties as recognized previously by Nag *et al.*<sup>83</sup> When these uncertainties add to those for sources of Table V and exceed 20% ( $k=2$ ), then the AAPM and GEC-ESTRO recommend that brachytherapy implants be performed with caution—preferably under Institutional Review Board (IRB) oversight with prior disclosure to the patient about the uncertain aspects of the procedure.

### VI.C. Dosimetry investigators

When performing physical measurements, investigators are encouraged to identify as many sources of uncertainty as possible. Several potential sources of uncertainty in physical measurements performed on brachytherapy sources exist. Many of these have been presented in Sec. III of the current report. Other sources of uncertainty may exist and, therefore, it is up to the individual investigators to determine other potential uncertainties and evaluate them appropriately. However, the specific areas of uncertainty presented in the current report should be addressed in articles providing dosimetry parameters for brachytherapy sources and should include:

- (i) Positional uncertainty: When evaluating measurement position uncertainty, both source and detector positional uncertainty should be evaluated. In addition to source-to-detector distance uncertainty, angular uncertainty and its effect on the measured quantity should be addressed. Tolerances for specific source positioning jigs and phantom construction should be included in the uncertainty analysis. Moreover, due to the nature of the radiation emitted from brachytherapy sources, the magnitude of the uncertainty often depends on the distance from the source, as described in Sec. III A 2. Efforts should be made to address this behavior.
- (ii) Dose measurement: Brachytherapy source dosimetry investigations usually involve the quantification of dose from the source. When performing such measurements, the investigator must account for specific detector characteristics for the energy being measured and their role in overall uncertainty. The lowest possible uncertainty that is achievable will come from choosing the best instrument for the experimental investigation. Therefore, dosimeters should be chosen with care. The reported uncertainty should reflect the authors' understanding of the various available dosimeters. For example, an investigation using TLDs should specify the annealing regime used as this can result in an increase in the uncertainty from 1% to 5%, depending on the temperature and the cooling rate procedure.<sup>19</sup> In addition, uncertainties arise from the differences in TLD response due to differing photon energy of the calibration source (e.g., 1.25 MeV) and low-energy brachytherapy sources (e.g., 0.03 MeV). This energy dependence may be divided into intrinsic energy dependence  $k_{Bq}(Q)$  (relating detector reading to detector dose) and absorbed-dose energy dependence  $f(Q)$  (relating dose to a detector to dose to medium in the absence of the



1477 detector).<sup>18</sup> When measuring the absorbed dose for  
 1478 low-energy photon-emitting brachytherapy sources  
 1479 when calibrating with a <sup>60</sup>Co beam, the  $k_{Bq}(Q)$  uncer-  
 1480 tainty ( $k=1$ ) can be significantly less than 5%.<sup>2,18</sup>

1481 (iii) Measurement medium: The AAPM TG-43 brachy-  
 1482 therapy dosimetry protocol specifies a methodology to  
 1483 determine the absorbed dose to water for a brachy-  
 1484 therapy source. The difficulties involved with measure-  
 1485 ments in a liquid medium often results in experiments  
 1486 being carried out in a solid medium that is designed to  
 1487 be radiologically equivalent to liquid water. However,  
 1488 many of the materials on the market today have been  
 1489 designed to be water equivalent at a particular energy  
 1490 range, usually megavoltage photon energies. These  
 1491 materials may or may not be equivalent to water at  
 1492 lower photon energies or for other types of radiation.  
 1493 Investigators should address the impact that measure-  
 1494 ment medium will have on the results as it pertains to  
 1495 absorbed dose to water. In addition, measurement  
 1496 phantom size should be specified in the investigators'  
 1497 publications.

1498 As with physical measurements, MC simulations also  
 1499 contain uncertainties in their results. As such, MC investiga-  
 1500 tors should have a thorough understanding of the MC pro-  
 1501 cess and its associated uncertainties. Specific areas to be ad-  
 1502 dressed are as follows:

1503 (i) Type A uncertainties: MC methods are stochastic in  
 1504 nature. By using probability distributions, appropriate  
 1505 starting conditions, and suitable pseudorandom num-  
 1506 bers, a problem may be simulated to produce a result  
 1507 consistent with a physical system. In general, conver-  
 1508 gence of MC-based radiation transport simulations  
 1509 obey Poisson statistics and, as such, have an associated  
 1510 statistical uncertainty that decreases as the square root  
 1511 of the number of samples (in this case the number of  
 1512 particle histories). Thus, the investigator should pro-  
 1513 vide simulations with a sufficient number of histories  
 1514 to provide an acceptable level of statistical uncertainty  
 1515 ( $<0.1\%$ ) so these may be considered negligible in  
 1516 comparison to other less constrainable uncertainties.

1517 (ii) Type B uncertainties: In addition to the type A uncer-  
 1518 tainties that arise naturally from a MC simulation, any  
 1519 model of a physical system will include type B uncer-  
 1520 tainties. This type of uncertainty will consist of uncer-  
 1521 tainties in source dimensions, internal component loca-  
 1522 tion(s), volume averaging, and material composition,  
 1523 for example. A thorough investigation to determine as  
 1524 many of the type B uncertainties as possible and their  
 1525 effects on the dosimetric quantities should be per-  
 1526 formed in the course of completing a MC study of a  
 1527 brachytherapy source. Examples of determining the  
 1528 type B uncertainties for a brachytherapy source have  
 1529 been given throughout Secs. III and IV.

## VI.D. Source and TPS manufacturers

1530

Brachytherapy source manufacturers should implement  
 tight tolerances on their manufacturing processes since the  
 clinical results are dependent on consistent source fabrica-  
 tion. The largest potential dosimetric variation is from dy-  
 namic internal components (Sec. IV B). Thus, the design  
 should constrain motion of these components. The source  
 design/version in regular clinical use should be the same  
 design/version measured and simulated by the dosimetry in-  
 vestigator and measured by the dosimetry laboratories.  
 Moreover, detailed information on the source components  
 including dimensions, tolerances, and material compositions  
 should be openly provided. If the manufacturer decides to  
 change source design/version, the manufacturer must recog-  
 nize that this is equivalent to construction of a new source,  
 which is subject to the processes described by DeWerd *et al.*,<sup>78</sup>  
 which include regular comparisons with dosimetry labora-  
 tories. Furthermore, manufacturers are advised to  
 minimize and keep constant any radiocontaminants per Sec.  
 VI C.

As also mentioned in Sec. VI C, it is recommended that  
 TPS manufacturers continue to strive for clinical utilization  
 of standardized datasets and development of TPS algorithm  
 benchmarking procedures toward minimizing type B dose  
 calculation uncertainties. This can be accomplished through  
 continuing adoption of the consensus dataset approach for  
 single-source dose calculations in standardized geometries  
 and through providing the information required to dosimetri-  
 cally characterize the clinical applicators and patient inter-  
 faces which will be incorporated in these new TPS platforms.

## VII. SUMMARY AND COMPARISON TO EXISTING WRITTEN STANDARDS

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Throughout the current report, the AAPM and GEC-  
 ESTRO have refined clinical expectations of brachytherapy  
 dosimetric uncertainty. Uncertainties are involved in all as-  
 pects of the dosimetry process. Every aspect of the process  
 results in a greater uncertainty in the estimation of patient  
 dose. In part, the AAPM TG-40 and TG-56 reports attempted  
 to provide QA procedures to reduce dosimetric uncer-  
 tainty.<sup>1,70</sup> The end result for consideration is the uncer-  
 tainties involved in patient treatments. The first aspect of  
 these uncertainties involves the transfer of the NIST calibra-  
 tion standard from the ADCL to the clinic's well chamber for  
 the determination of measured source strength. When the  
 clinical medical physicist measures this, a typical uncertainty  
 ( $k=2$ ) is about 3% (Sec. V A 5). If each source is not mea-  
 sured, the corresponding uncertainty is increased through use  
 of the manufacturer value based on batch averaging. If the  
 physicist relies solely on the manufacturer's value, then un-  
 known manufacturer measurement uncertainties are passed  
 along to the clinic (patient), along with possible administra-  
 tive errors by the manufacturer sending sources from the  
 order placed by another institution. Generally, the manufac-  
 turer source-strength uncertainty is larger than if measured  
 by the clinical medical physicist using an instrument with a  
 calibration coefficient traceable to a primary standards

laboratory.<sup>79</sup> The second aspect of dosimetric uncertainty involves treatment planning. Intrinsic to this process is derivation and utilization of TG-43 parameters. If these parameters are based on AAPM consensus data, their uncertainties should have been provided in the AAPM report. If data from multiple dosimetry investigators are entered into the TPS, the resultant dosimetric uncertainty of the calculated dose is greater. Further, uncertainties in the treatment planning process are not as great an effect on the patient treatment as is the initial determination of the reference dose-rate distribution. When all these uncertainties are combined, the  $k=2$  uncertainty of dose rates for low- and high-energy photon-emitting brachytherapy sources used in treatment planning are approximately 8% and 6%, respectively. Uncertainty in dose delivery due to physical implantation will add to these uncertainties and surely be larger upon clinical implementation. Consequently, it is paramount that the clinical medical physicist be cognizant of these uncertainties and endeavor to minimize them for the aspects within their responsibilities. Similarly, brachytherapy source dosimetry investigators should continue to minimize dosimetric uncertainties in their reference data.

The AAPM TG-56 report recommends brachytherapy dose delivery accuracy within 5%–10% with source calibration accuracy within 3%.<sup>70</sup> This latter tolerance was updated by Butler *et al.*<sup>79</sup> to 6% for individual sources. While the scope of the current report is limited to evaluation of pre-treatment brachytherapy dosimetry uncertainties, it appears that the TG-56 10% criterion for accuracy of brachytherapy dose delivery could be adhered to within a 95% confidence level. To our knowledge, there are no other existing societal standards on uncertainty for brachytherapy source calibration and dose delivery, and additional research in this area is needed. However, a joint effort of GEC-ESTRO and AAPM brachytherapy physicists/physicians will explore more details of the clinical aspects of the total uncertainty budget for brachytherapy treatment delivery.

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**AUTHOR QUERIES — 010102MPH**

- #1 Au: Please verify edit in the sentence “Using a sensitive scintillation detector...” to see if meaning was preserved.
- #2 Au: Please provide last page in Ref. 13.
- #3 Au: Please check accuracy of author’s names in Refs 17 and 37.