## Merging 3-D Symbolic Deacriptions Obtained from Multiple Views of a Scene

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#### Abstract

An algorithm is presented for merging threedimensional symbolic descriptions of static polyhedral scenes obtsined from multiple viewpoints. The 3-D descriptions are assumed to be partial because of occlusions. The merging algorithm treats the topology of the descriptions (i.e., connections between vertices, edges, and faces) separately from the geometry (i.e., physical dimensions and relative locations). This paper describes one part of a larger project whose goal is to obtain an integrated symbolic description of a scene from range data obtained from multiple viewpoints.


## 1. Introduction

An important problem for robotics vision is that of generating a 3-D description of an unknown scene from range mape obtained from multiple views. This paper describes part of a project whose goal is to obtain a full symbolic description of a polyhedral scene from range data obtained from multiple viewpoints. Each view is processed in sequence, and the 3-D information extracted from each view is used to incrementally construct a model of the scene. Three main steps are followed in this project. First, a scene description, in terms of faces, edges, and vertices, is generated from each view. This step is described in [5]. Next, descriptions from separate views are matched to obtain corresponding elements and to obtain the six parameters of the global coordinate transformation. This process is described in [6]. Finally, the separate descriptions are merged, resulting in a more complete overall description of the scene. This step is the topic of the current paper.

The approach of the overall project is useful for two applicstions: (1) a mobile robot or sensor incrementally learning its environment as it moves through it $[3,7,8,9,10,11]$, and (2) incrementally learning the 3-D shape of an object presented via multiple views to a sensor $\{2,12,13 \mid$.

## 2. Approach

Each new view of the scene undergoes analysis which results in a symbolic scene description. This description is then merged with the current model. The description extracted from the first view forms the initial state of the scene model. This model is incrementally updated with information from esch new view.

Both the symbolic descriptions extracted from each viewpoint, as well as the scene model, are represented in the form of a graph. Since this graph represents 3-D structure in the scene, we call it a structure graph [7]. The nodes and links represent topological and geometric constraints. The structure
graph representation models surfaces in the scene as polyhedra. The components of a polyhedral surface are the face, edge, and vertex. We distinguish the topology of the polyhedral components from their geometry [1, 4]. The geometry involves the physical !imensions and location in $3-$ space of each component, while the topology involves conneclions between the components.

Each node in the structure graph represents a face, edge, or vertex. Associated with each face node is its plane equation, with each edge node its line equation, and with each vertex node its coordinate values. The links in the structure graph capture the topology between nodes. A vertex node has a link to each edge and face node on which it lies, an edge node has links to its vertex nodes and to the face nodes on which it lics, and a face node has links to its vertex and edge nodes.

A vertex must lie on at least two edges. If it lies on only one edge, then it is not really a vertex, and is tagged as a non-vertex end point of the edge. This comes about when a portion of the edge has been occluded, and the edge is therefore tagged as incomplete (see Fig. 1). Any face that contains incomplete edges, or that is not closed by a ring of edges, is also tagged as incomplete.

## 3. Merging

Given a structure graph description extracted from a new view, it is incorporated into the current model structure graph as follows. First, the two descriptions are matched as described in [6]. The output of this matching process is a set of corresponding pairs of elements, i.e., vertices, edges, and faces. Those elements in one description that have no match in the other description because of occlusion are matched with NIL. Non-vertex end points are not ineluded in the corresponding pairs of elements, since the matching process does not match such points.

In order to merge the two descriptions, we require not only the corresponding elements, but also the global coordinate transformation that maps one description into the other. To obtain the coordinate transformation, we use an algorithm that obtains the best rigid transformation (rotation and translation) between two sets of corresponding points in 3-space. Suppose a point $\vec{v}_{1}$ in description 1 is transformed into the point $\vec{v}_{2}$ in description 2 by the equation:

$$
\vec{v}_{2_{i}}=R \vec{v}_{1_{1}}+T,
$$

where $R$ is a rotation matrix and $T$ a translation vector. Then $R$ and $T$ may be estimated by minimizing the sum of the square norms:


Fig. 1

$$
\left|\left|R \vec{v}_{i_{1}}+T-\vec{v}_{2_{1}}\right|\right|^{2} .
$$

The vertex malches returned by the matching module are used to obtain this transformation.

At this point, both descriptions are expressed in the same coordinate system. To merge the two descriptions, pairs of corresponding elements are first merged, then elements for which no correspondences were found are included.

Basically, the merging process consists of two main steps. First, the topology of the two descriptions are merged, then the geometry is merged. Topological merging involves generating new elements (vertices, edges, and faces) for pairs of corresponding ones, and then generating appropriate links among these new clements and between these elements and those that have no correspondences. Geometric merging involves determining the appropriate geometry (i.e., coordinates of vertices, line equations of edges, and plane equations of faces) of all elements modified by the topological merging.

## 4. Merging Edges and Faces Within a Deacription

Before topological and geometric merging between elements in the two descriptions can occur, we want to merge multiple elements in each description that correspond to a single element in the other description. For example, in Fig. 2, the face $f_{1}$ will match both faces $f_{2}$ and $/ 2$, while the edge $e_{1}$ will match both edges $\varepsilon_{2}$ and $e_{3}$. The final goal of the merging process is to merge $f_{1}$ with $f_{2}$ and $f_{3}$, and $e_{1}$ with $e_{2}$ and $e_{3}$. By first merging elements within each description, e.g., $f_{2}$ with $\int_{3}$, and $e_{2}$ with $e_{3}$, the later process of merging elements across the two descriptions can be more uniform, since it will only have to merge pairs of, rather than mulliple, corersponding elements.

Notice that our approach for merging elements within a description is different from the typical approach. Typically, edges $e_{2}$ and $c_{2}$ in Fig. 2 would be merged using heuristics such as that they are colinear and have opposing $T$ junctions (i.e., junctions $A$ and B). Such heuristics often will lead to errors, since we can only guess at what happens in occluded regions. A more reliable way to determine what is occurring in occluded regions is to move to another viewpoint where the occluded region becomes visible. This is in effect what is

occurring here. After the totally visible edge $e$, has been determined to match with the partially complete edges $e_{2}$ and $e_{2}$, we know that $e_{2}$ and $e_{2}$ are portions of the same edge.

Merging of edges and faces within a description occurs as follows. If an edge in one description matches multiple edges in the other (which will be multiple incomplete edges), the multiple edges are merged into a single edge by connecting the
two verlex end poinis (e.g., C and D in Fig. 2) of these edges. This new edge, which is complete, then replaces the multiple ones. Topological pointers are then modified, so that the new edge is given pointers to all the vertices and faces of the old edges (except for the non-vertex end points, e.g., $A$ and $B$ in Fig. 2, which are deleted), and all the vertices and faces that had pointers to the old edges are given pointers to the new edge instead.

The merging of faces within a description occurs after the edges have been merged. If a face in one description matches multiple faces in the other (which will be multiple incomplete faces), the multiple faces are merged into a single face. This new face then replaces the multiple ones. It is tagged as incomplete if it has at least one incomplete edge. Topological pointers are then modified, so that the new face is given pointers to all the vertices and edges of the old faces, and all the vertices and edges that had pointers to the old faces are given pointers to the new face instead.

## 5. Dealing with Non-Vertex End Points

At this point, we want to find vertices in one description that "correspond" to non-vertex end points in the other description (e.g., $J$ and $L$ in Fig. 3), and "corresponding" nonvertex end points in the two descriptions (e.g., B and D in Fig. 4). Such points do not really correspond becsuse the point on the edge which divides the visible from the oceluded portions is in general diffcrent for different viewpoints. However, it is convenient to treat the points as corresponding pairs, since they must somehow be combined to produce a single point in the merged description.


Description 2


Description 1
Fig. 3


Description 1


Description 2

Fig. 4


Description 1


Description 2
Fig. 5

Notice that in both these cases, the edges on, which these points lie have been found to match by the matching aigarithm. Also, in both cases, the matching edges have one pair of matching vertices. Therefore, to find corresponding pairs of points involving non-vertex end points, each matching pair of edges is examined. If at least one of the edges is incomplete, then one pair of end points will not appear in the list of vertex matches obtained by the matching algorithm. This pair is then included in the list. The non-vertex end points are tagged as such so that when merging occurs later, these points will be merged differently from those returned by the matching algorithm.

The current algorithm for finding correspondences for non-vertex end points does not handle the situation depicted in Fig. 5, where it appears that A corresponds to C and B to D. This situation is not handled because it is not known at this point in the processing that the edges $c_{1}$ and $e_{2}$ should match. Our matching algorithm matches verlices first, and
then finds edge and face matches based on the vertex matches [6]. Since $e_{1}$, and $e_{2}$ have no matching vertices, they themselves are not found to match. (In fact each of them will be matched with NIL.)

Notice that it is possible for a vertex point in one description to match with multiple non-vertex end points in the other description. In Fig. 3, for example, the vertex point $L$ in description 2 corresponds to the non-vertex end points $\mathrm{J}, \mathrm{M}$, and N in description 1.

As described earlier for cases involving multiple edges or faces in one description that match single edges or faces in the other, we want to merge multiple end points in one description that match a single vertex in the other. By doing this first, the later process of merging elements across two descriptions can be simpler and more uniform.

The procedure we use to merge multiple non-vertex end points is to intersect all the edges on which these points lie. In Fig. 3, for example, the edges $e_{d} e_{6}$ and $e$, are intersccted (in 3-space) in pairs, resulting in three intersection points. The average position of the intersection points is used to form a new vertex, which is given topoiogical pointers to all the edges and faces of the old end points. All edges and faces with pointers to the old end points are then given pointers to the new vertcx. All edges on which the old end points were lying are then tagged as complete, and all faces that contained these end points are checked for completeness. Any of these faces containing only complete edges is tagged as complete.

## B. Merging the Topology of the Two Deacriptions

At this point, all mergers within each description have been done, so that each element in one description will match at most one element in the other description. To merge elements across the two descriptions, it is simpler to merge the lopology separately from the geometry.

The first step is to create a new empty vertex, edge, or face node for each matching pair of vertices, edges, and faces, respectively. The new nodes will represent the merging of each original pair.

The next step is to merge the topology of the two initial descriptions. This is accomplished by substituting, in the two structure graphs, each new node for its matching pair. For example, each new vertex node is given a topological pointer to each of the edges and faces pointed to by its matching pair, and all edges and faces with pointers to either of the pair are given a pointer to the new vertex instead. New edge and face nodes are handied in a similar manner.

## 7. Merging the Geometry of the Two Deacriptions

The next step is to merge the geometry of matching pairs of elements. For each new vertex node previously generated, the original matching pair of vertices is examined. If both are not non-vertex end points (i.e., both correspond to real vertices in their descriptions), then the position of the new vertex is the average position of the original pair. Notice that this algorithm gives equal weight to the positions of the original vertices.

Next, for each new edge node previously generated, the original matching pair of edges is examined. Three different merging techniques are used depending on whether both original edges are complete, both are incomplete, or one is complete and one is complete. If both original edges are complete (Fig. 6 a), the 3 -space line of the new edge mereiy connects the two new vertices previously obtained. If one of the original edges is complete and the other is incomplete (Fig. 6b), we must obtsin the line equation of the new edge and the position of the new vertex on the edge. (Because the new vertex is formed by merging a vertex and a non-vertex end point, its coordinates have not yet been determined.) To see how this is done, consider Fig. 6e. Let newv; be the new vertex formed by merging $v_{1}$ and $v_{2}$ in Fig. 6 b . Let $p$ be the average position of the other two end points of the edges, i.e.,

$$
\bar{p}=\left(\boldsymbol{H}_{2}+\bar{p}_{1}\right) / 2 .
$$

The line of the new edge is a line containing neww, and $p$. The position of the other new vertex, nevv, lies on this line at a distance from newv, equal to the length of the original complete edge, and in the same direction from newv, as nevv ${ }_{2}$, i.e.,

$$
n e \bar{\omega} v_{2}=n e \bar{v} v_{1}+\left|e_{1}\right|\left|t p-n e \bar{e} v_{1}\right| /\left|\bar{p}-n e \bar{e} v_{1}\right| \mid .
$$

To see intuitively why the resulting new edge should pass through the midpoint of $p_{1}$ and $v_{2}$ in Fig. $6 c$, consider the two extreme cases for the relative lengtis of $e$, and $e q$. If the length of $e_{2}$ equals the length of $e_{1}$, then we want the resulting edge to lic along the angle bisector of $e_{1}$ and $c_{2}$, which it will under our formula. On the other hand, if the length of $e_{2}$ approaches 0 , then we want the resulting new edge to lie along the edge $e_{1}$, which it will under our formula.

If both original edges are incomplete (Fig. 6d), the line of the new edge and position of the new vertex is obtained exactly as for the case of one complete edge and one incomplete edge, except that the length of the new edge is the same as that of the longest of the original edges $e_{1}$ and $e_{9}$. Also, the new vertex is tagged as a non-vertex end point and the new edge is lagged as incomplete.


Fig. 6

## 8. Adding Elements with No Matches

Both description 1 and description 2 will often have elements that have no matches. Merging these elements inco the final structure graph involves two steps: (1) modifying their topological pointers so that they obtain links to the newly created nodes formed by merging pairs of matching elements, and (2) modifying their geometry so that they are represented in the same coordinate system as the final description. But these two steps have already been performed. All topological pointers were modified immediately after the new elements were created, and the geometry of all elements were modified when the coordinate transformation between the two original descriptions was calculated.

For each new face node previously generated, its plane equation is calculated by a least squares fit to all the new vertices of the face. If any new edge of the face is incomplete, the face node is tagged as incomplete. Otherwise, it is complete.

## - Experimental Reaults

This section presents results of the merging algorithm on some examples. The first example involves 3-D descriptions automatically generated from range data [5]. Fig. 7 shows the descriptions generated from two views of an object. This might be an example of the application mentioned earlier of learning the shape of an object presented via multiple views. Fig. 8 shows two views of the resulting description after matching and merging the descriptions in Fig. 7.

Our next example involves a complicated office scene containing chairs and a table. This might be an example of the application mentioned earlier of a mobile robot learning its environment by moving through it. The 3-D descriptions in Fig. 9 were manually generated from synthesized depth maps. Fig. 10 shows the resulting description after matching and merging the descriptions in Fig. 9. Fgi. 11 shows an additional view of the office scene. Fig. 12 shows the resulting description after matching and merging the descriptions in Figs. 10 and 11. Note how the scene model is incrementally updated with 3-D information from each new view.

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\text { Fig. } 12
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