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Solid State Communications 142 (2007) 154-158

solid state communications

www.elsevier.com/locate/ssc

Signatures of many-particle correlations in two-dimensional Fourier-transform spectra of semiconductor nanostructures

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Received 20 November 2006; accepted 3 February 2007 by R. Merlin Available online 15 February 2007

Abstract

On the basis of a microscopic theory, the signatures of many-particle correlations in Two-Dimensional Fourier-Transform Spectra (2D-FTS) of semiconductor nanostructures are identified and compared to experimental data. Spectra in the photon energy range of the heavy-hole and light-hole excitonic resonances show characteristic features due to correlations, which depend on the relative polarization directions of the excitation pulses.

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PACS: 78,47.+p; 42.50.Md; 42.65.Re; 78.67.-n

Keywords: A. Semiconductor nanostructures; D. Many-body correlations; E. Two-dimensional Fourier-transform spectroscopy; E. Four-wave-mixing

1. Introduction

Recent reports illustrate the potential of a novel method, known as "Two-Dimensional Fourier-Transform Spectroscopy" (2D-FTS), to investigate many-particle induced correlations in semiconductor structures [1-3]. 2D-FTS is based on a four-wave-mixing experiment where three excitation pulses are separated in time, and is heterodyne detected to fully characterize its phase. The signal is transformed into the frequency domains ω_t (emission frequency) and ω_{τ} (excitation frequency), both with respect to the real time t and time separation τ of the first two pulses, respectively. The third pulse is delayed with respect to the second one by T. 2D-FTS is widely used to study vibrational [4-6] and electronic excitations [7-9] in molecules. Applying 2D-FTS in the optical regime, we investigate the complex interplay between exciton, biexciton, and continuum excitations in semiconductor nanostructures.

In previous publications demonstrating the 2D-FTS of semiconductors [1–3], the experimental results were compared to a phenomenological theory based on extending the Optical Bloch Equations to include terms that describe excitation induced dephasing (EID) [10,11] and excitation induced shift (EIS) [12]. Here, we use a microscopic theory to calculate the 2D-FTS. Furthermore, the model predicts that the 2D-FTS qualitatively depends on the polarization directions of the excitation pulses. Our results demonstrate that for 2D-FTS, the influence of many-particle correlations on the spectra can clearly be identified and are in agreement with the experimental findings.

For the qualitative modelling of 2D-FTS in such systems and in order to keep the numerical requirement within reasonable limits, we use a microscopic many-body theory and apply it to a one-dimensional tight-binding model. Therefore, a quantitative agreement between theory and experiment cannot be expected. It has, however, been shown that many important signatures of nonlinear optical experiments performed on quantum wells can qualitatively be well reproduced by this model [13–19].

The optical nonlinearities are treated up to third order in the coherent $\chi^{(3)}$ -limit beyond the Hartree–Fock level. In order

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to separate the correlation effects from those due to the first-order Coulomb interaction (i.e., Hartree–Fock), we use a set of equations for the interband coherence P and two-exciton amplitude \bar{B} , which in symbolic form reads [14,15,20,21]

$$-i\hbar \frac{\partial P}{\partial t} = \hbar(\omega_X - i\gamma)P + V_C P^* PP - V_C P^* \bar{B} + \mu^* E$$
$$-\mu^* E P^* P, \tag{1}$$

$$-i\hbar \frac{\partial \bar{B}}{\partial t} = \hbar(\omega_{BX} + i\beta)\bar{B} + PPV_C.$$
 (2)

In fact, all the terms in the microscopic version of the equations depend on the spatial indices of the tight-binding model as well as the band indices, referring to electron, heavy-hole (h), and light-hole (1) bands, respectively. Details of the model and the set of microscopic equations that are used in our numerical evaluations are presented and discussed in Ref. [15]. In Eqs. (1) and (2) V_C is the Coulomb matrix that is responsible for the existence of exciton and biexciton resonances and interactions between them. In Eq. (1) for the polarization P, the Hartree-Fock terms are given by the kinetic term $\hbar\omega_X$, the renormalization term $V_C P^* PP$, and the coupling to the light field containing the Pauli-blocking μ^*E P^* P and the linear term μ^*E . The correlation term beyond Hartree-Fock is given by $V_C P^* \bar{B}$. As given in Eq. (2), the biexciton correlation \bar{B} is driven by PPV_C . The biexciton energy is $\hbar\omega_{BX}$. Coherent $\chi^{(3)}$ -equations with h- and l-transitions have been previously analysed, see e.g., [16,18,22].

The quantum well samples used in this study show heavy hole and light hole excitonic resonances. Their spectral positions are determined by the kinetic parts of Eqs. (1) and (2), which also contain the phenomenological dephasing rates, $\gamma = 1/T_2^{(h,l)}$ for excitons and $\beta = 1/T_2^{(h,l,l,hl,lh)}$ for biexcitons. By such rates, we can distinguish biexcitons formed by h-excitons (hh), by l-excitons (ll), and mixed h- and l-excitons (hl, lh). The optical transitions are given by dipole matrix elements μ chosen to model the relevant selection rules for dipole transitions in III–V semiconductor structures [15,17]. This model agrees with the selection rules for the nonlinear polarization presented by Lindberg et al. for the three beam situation [23].

Based on this model, we present microscopic calculations for 2D-FTS for semiconductor structures. We choose realistic material parameters, ratio between h- and l-effective masses, and dipole matrix elements, energetic h- and l-offset, and Coulomb strength. The experimental conditions such as pulse duration, detuning, dephasing times, polarization directions, and the sequence of the pulses are incorporated into the model. The dephasing times of the various excitons and biexcitons are taken as phenomenological parameters.

In this paper, we concentrate on the situation where the first pulse enters the nonlinear polarization conjugated, the so called rephasing case [3]. The figures show the amplitude $|E(\omega_t, \omega_\tau, T)|$, where the electric field $E(\omega_t, \omega_\tau, T)$ is proportional to the third-order polarization multiplied by the imaginary unit, i.e., $iP(\omega_t, \omega_\tau, T)$. The emission frequency ω_t , is given on the horizontal-axis. The emission frequency is used to define the sign of the frequency, thus the conjugation of the

first pulse means that the excitation frequency, ω_{τ} , is negative. It is given on the vertical axis. The h- and l-exciton peaks then show up on the diagonal in the left-upper (low energy) and right-lower (high energy) corners, respectively, while the off-diagonal peaks are due to coupling between h- and l-exciton resonances.

2. Experiment

For the particular system considered in this paper, i.e., a GaAs quantum well, the nonlinear optical properties have been explored quite extensively in the past using the four-wave-mixing and pump-probe experiments. This system therefore presents a good testing ground for the exploration of the features of the 2D-FTS. In particular, the sample used in the experiment is a 10 period multiple quantum well structure with 10 nm GaAs wells and 10 nm AlGaAs barriers. It is held at 8 K. Experimental spectra are obtained using the apparatus described by Zhang et al. [1], with the addition of polarizing optics.

3. Results and discussions

In the following section, we concentrate on the amplitude features of the 2D-FTS. The distribution of the heights of the peaks strongly depends on the interplay of the material and experimental parameters, including the tuning of the excitation pulses, shape and temporal full width at half maximum (FWHM) of the pulses, ratio μ^h/μ^l of h- vs. l-dipole matrix elements (which due to band-mixing in the quantum well structure depart from their bulk values), and dephasing times. We found that $|\mu^h/\mu^l|^2 = 2.1$ is a good choice for modelling the experiment. The simplest approach to model the h-lexciton system is a three level system (V-system) without any interactions, but with coupling of two excited levels (modelling the h- and l-excitonic resonances) to a common ground state. In this model, it is not possible to obtain a peak height distribution in the 2D-FTS features that is asymmetrical with respect to the diagonal, if the excitation pulses are extremely short and $\mu^{\rm h} = \mu^{\rm l}$. The asymmetry of such spectra in our experiments on quantum well systems appears because of the interplay of several effects: different dipole matrix elements, dephasing times of excitons and biexcitons, degree of overlap with the spectrum of the excitation pulses and, many-particle couplings within the system as supported by the theoretical spectra. In our model, the electric field of the excitation pulses is proportional to $\exp(-t^2/\delta^2)$, where δ is the Gaussian width of around 115 fs, corresponding to intensity FWHM of 135 fs and a spectral FWHM of 13.5 meV.

In Fig. 1, we compare experimental (first column) and theoretical results for the amplitudes from the full calculation (second column), and the Hartree–Fock part (third column) for $\sigma^+\sigma^+\sigma^+$, co-linear *XXX*, and cross-linear *YXX* polarizations. In all the figures, the central excitation energy is 1 meV above the l-exciton in order to compensate for the small dipole matrix element of the l-exciton.

The numerical results for the full calculation (second column) show agreement with experiments, not only for

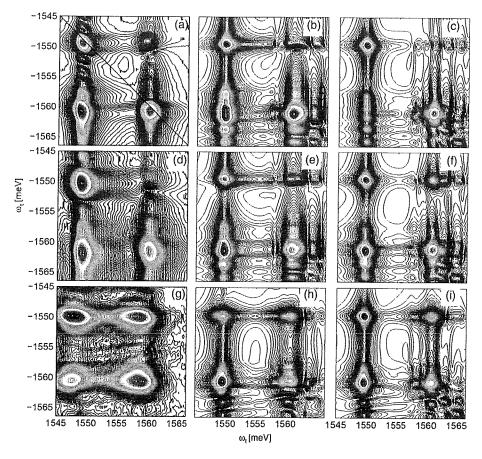


Fig. 1. 2D-FTS spectra amplitudes (normalized). Left column: experimental. Middle column: full $\chi^{(3)}$ -calculation. Right column: Hartree–Fock calculation. Upper row: $\sigma^+\sigma^+\sigma^+$ polarization, T=100 fs. Middle row: XXX co-linear polarization, T=100 fs. Lower row: YXX cross-linear polarization, T=350 fs. Dephasing times are: $T_2^h=1.3$ ps, $T_2^l=0.8$ ps for excitons and $T_2^{hh}=1.3$ ps, $T_2^{ll}=0.8$ ps, $T_2^{hl}=T_2^{lh}=0.5$ ps for biexcitons. Theoretical spectra are weakly inhomogeneously broadened by Gaussian width of 0.3 meV.

the h-, l-exciton and mixed peaks, but also for the hcontinuum at higher ω_{τ} (the vertical continuum contributions in the experimental data are more apparent in a previous publication [2]). Note that in the theoretical figures, the h-continuum, appearing close to the l-excitonic peaks as dominantly vertical structures is decomposed into discrete peaks, because only N = 40 sites have been taken in the tightbinding approach for numerical reasons. It should be noted that the continuum appears dominantly as a vertical feature close to the mixed peaks in the lower-left corner. This demonstrates that the lower energetic part of the continuum cannot be seen as a pure inhomogeneous spectrum in the model containing the many-particle interaction [15,24]. In an interaction-free model, the continuum would in fact be purely inhomogeneous, i.e. it would consist of independent two-level systems belonging to a spectrum of k-vectors. If this were true, one would expect a feature of continua along the main diagonal close to the 1-excitonic peak in the right-lower corner. In the frame of the Hartree-Fock approximation, where the correlations are ignored, the features due to the h-continuum clearly show up at the higher energies for all the polarization cases (Fig. 1 third column).

The co-linear situation (Fig. 1 middle row) looks similar to the co-circular case (Fig. 1 upper row), as is to be expected

from the selection rules. It is remarkable that the upper right non-diagonal mixed peak for co-circular case (Fig. 1(b)) is very small. As a comparison with a Hartree-Fock result (Fig. 1(c)) shows, this is not due to correlations, but results from an interplay of detuning, dipole matrix elements, and dephasing times. The mixed signature in the left-lower corner for the Hartree-Fock calculation (Fig. 1(c)) shows discrete weak features due to the h-l-excitons and the h-continuum. The many-body correlations lead to the increase of this mixed signature at higher excitation energies and vertical features of the continuum as well. Unlike in the co-circular case, the influence of correlations on the mixed signature at higher excitation energy is less pronounced for the co-linear case. The Hartree–Fock approximation (Fig. 1(f)) and the full calculation (Fig. 1(e)) do not differ that much for the co-linear case. This can be understood by consideration of a simple V-system, where for the excitation $\sigma^+\sigma^+\sigma^+$ the h- and l-transitions resemble two independent two-level systems. The linear case contains both σ^+ and σ^- transitions, thereby such excitation couples the h- and l-exciton transitions resulting in two Vsystems. This coupling generates the mixed signatures and appears for both the linear polarized cases in the Hartree-Fock calculations (Fig. 1(f): XXX, (i): YXX).

The cross-linear polarized excitation case (YXX) shows additional signatures from two-exciton resonances (bound and unbound biexcitons), as predicted by the selection rules and supported by the theoretical results (Fig. 1(h)). This is due to a suppression of the excitonic features with respect to the biexcitonic ones [18]. Bound biexcitons show up on the low emission-energy side and unbound ones on the high emission-energy side of the exciton [13,14,18]. The biexciton contribution results in a horizontal elongation of the peaks compared to the XXX-case. The Hartree-Fock calculation (Fig. 1(i)) clearly shows that the horizontal elongation of the YXX spectra (Fig. 1(h)) is due to correlations, i.e. bound and unbound two-exciton states. In the Hartree-Fock limit, the horizontal elongation is absent (Fig. 1(i)). Interestingly, the continuum contribution and respectively the elongation of the signatures at higher excitation energies is less developed as compared to the co-linear case, which is supported by the experiment (Fig. 1(d), (g)). For the cross-linear situation one can show [15,24] that indeed the continuum becomes suppressed due to cancellation effects that result from Coulomb-correlations in this situation. Indeed, the Hartree-Fock calculation shows a more pronounced continuum contribution (and concomitantly of the superimposed l-exciton peak) in the right-lower corner of the spectrum, as compared to the full $\chi^{(3)}$ -calculation.

It is surprising that the lower left non-diagonal peak is the strongest one in the theoretical spectra for the YXX-case (Fig. 1(h)), in contrast to the experimental data (Fig. 1(g)), where the h-peak is the strongest one. At present, the reason for this discrepancy is not clear. The peak in question is a mixture of three contributions, the h- and l-excitonic resonances and the h-continuum. Therefore, it is reasonable to assume an effective dephasing of this peak, which is not included in our present treatment.

A comparison between the results of the full and the Hartree–Fock calculations shows that the left-lower non-diagonal peak is less prominent in the latter spectra. This difference suggests that correlations enhance this signature in the full treatment. These couplings could well be more sensitive to relaxation processes than the trivial ones which already appear in the V-system or within a model, which only considers the phase-space (Pauli-blocking) nonlinearities.

We have not studied the dependence of the peak heights on the spectral shape of the incident laser pulses, which we have always taken as Gaussian here. Our calculations have shown that the temporal duration, and thus the spectral width, of the laser beams strongly influences the 2D-FTS. Therefore, deviations of the pulse envelopes from a Gaussian shape will clearly significantly alter the peak heights.

The amplitude of the non-diagonal signatures relative to the diagonal ones generally depends on T. Already, for a V-system one finds that the two non-diagonal peaks show beating with respect to T, where the period is $2\pi\hbar/\Delta E_{\rm h,l}$, with $\Delta E_{\rm h,l}$ the energetic h- and l-exciton separation. In the experimental data shown here, T=350 fs has been taken. With $\Delta E_{\rm h,l}=11.5$ meV, corresponding to a beating period of 360 fs, this is close to the situation of maximum non-diagonal

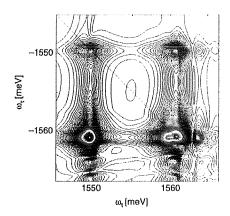


Fig. 2. Amplitude of 2D-FTS for YXX case. Dephasing times are: $T_2^1 = T_2^h = 1.3$ ps for excitons and $T_2^{II} = T_2^{hh} = 1.3$ ps, $T_2^{hI} = T_2^{Ih} = 0.65$ ps for biexcitons. Theoretical spectra are slightly inhomogeneously broadened by a Gaussian width of 0.3 meV.

peaks. However, as mentioned above, the left-lower signature is definitely too strong when compared to the experiments. In our calculations for the YXX-case, we have used T = 350 fs.

It should be noted that biexcitonic features can be observed in different kinds of nonlinear optical experiments for certain polarization cases. The 2D-FTS always shows the presence of biexcitonic features in the plots for amplitude or real part (not shown here), albeit to a different extent, depending on polarization.

Since 2D-FTS is based on a photon-echo experiment, it is not surprising that it can be used to measure the dephasing time T_2 , even in the presence of inhomogeneous broadening. Specifically, inhomogeneous broadening will elongate peaks along the diagonal, while the width perpendicular to the diagonal is inversely proportional to T_2 . However, 2D-FTS is clearly superior to a traditional one-dimensional photon echo measurement when multiple resonances are involved, as is the case here. The photon-echo signal mixes the contributions of the resonances, possibly leading to ambiguity in assigning the dephasing times. This ambiguity does not occur in 2D-FTS, as the peaks corresponding to distinct resonances are well separated.

A traditional one-dimensional transient four-wave-mixing (or photon echo) measurement also has trouble yielding T_2 when there are strong many-body correlations, which may result in a rapid decay of the signal unrelated to T_2 [25]. 2D-FTS is much better at revealing the T_2 of individual resonances. As an example, we consider theoretical 2D FTS-amplitude plots for cross-linearly polarized pulses, which show the correlation-induced features most prominently. However, now the 1-transitions have been given the same dephasing time as the h-ones, i.e., $T_2^1 = T_2^{\rm h} = 1.3$ ps, while the theoretical results shown in Fig. 1 correspond to $T_2^{\rm h} = 1.3$ ps and $T_2^1 = 0.8$ ps. Fig. 2 shows, that the distribution of the peak heights changes due to the longer dephasing time of 1-exciton. The comparison with Fig. 1(h) demonstrates the large sensitivity of the 2D-spectra on T_2 -times.

4. Conclusions

In summary, we have investigated the correlation effects in quantum well systems by applying the Two-Dimensional Fourier-Transform Spectroscopy (2D-FTS). This method provides a wide spectrum of information about many-body correlations simultaneously, such as: the strength of the couplings between excitons, biexcitons and continua, the character of continuum excitations, dephasing times, and the dependences of these features on the polarization directions.

A first comparison between experiment and theory has been performed on the basis of a microscopic model. Depending on the polarization directions of the excitation pulses, characteristic signatures of many-particle correlations can be identified in the amplitude spectra. Differences between experiment and theory point towards the action of relaxation processes on many-particle correlations, which are not included in the present purely coherent treatment. An additional important bit of information is contained in the real- and imaginary parts of the spectra. Work is in progress to analyse these parts of the signal and to exploit these spectra for semiconductor structures in the energetic range of both excitonic and continuum transitions.

Acknowledgements

This work has been supported by the Optodynamics Center of the Philipps-University Marburg, and by the Deutsche Forschungsgemeinschaft (DFG), and by the Research Centre Jülich (NIC). T.M. thanks the DFG for support via a Heisenberg fellowship (ME 1916/1). The work at JILA was supported DOE/BES grant DE-FG02-02ER15346.

References

- [1] T. Zhang, C.N. Borca, X. Li, S.T. Cundiff, Opt. Express 13 (2005) 7432.
- [2] C.N. Borca, T. Zhang, X. Li, S.T. Cundiff, Chem. Phys. Lett. 416 (2005)

- [3] X. Li, T. Zhang, C.N. Borca, S.T. Cundiff, Phys. Rev. Lett. 96 (2006) 057406
- [4] R.R. Ernst, G. Bodenhausen, A. Wokaun, Principles of Nuclear Magnetic Resonance in One and Two Dimensions, Oxford Science Publications, New York, 1987.
- [5] O. Golonzka, M. Khalil, N. Demirdöven, A. Tokmakoff, Phys. Rev. Lett. 86 (2001) 2154.
- [6] M.T. Zanni, N.-H. Ge, Y.S. Kim, R.M. Hochstrasser, Proc. Natl. Acad. Sci. 98 (2001) 11265.
- [7] S. Mukamel, Annu. Rev. Phys. Chem. 51 (2000) 691.
- [8] J.D. Hybl, A.A. Ferro, D.M. Jonas, J. Chem. Phys. 115 (2001) 6606.
- [9] T. Brixner, J. Stenger, H.M. Vaswani, M. Cho, R.E. Blankenship, G.R. Fleming, Nature 434 (2005) 625.
- [10] H. Wang, K. Ferrio, D.G. Steel, Y.Z. Hu, R. Binder, S.W. Koch, Phys. Rev. Lett. 71 (1993) 1261.
- [11] Y.Z. Hu, R. Binder, S.W. Koch, S.T. Cundiff, H. Wang, D.G. Steel, Phys. Rev. B 49 (1994) 14382.
- [12] J.M. Shacklette, S.T. Cundiff, Phys. Rev. B 66 (2002) 045309.
- [13] C. Sieh, T. Meier, F. Jahnke, A. Knorr, S.W. Koch, P. Brick, M. Hübner, C. Ell, J. Prineas, G. Khitrova, H.M. Gibbs, Phys. Rev. Lett. 82 (1999) 3112.
- [14] C. Sieh, T. Meier, A. Knorr, F. Jahnke, P. Thomas, S.W. Koch, Eur. Phys. J. B 11 (1999) 407.
- [15] T. Meier, P. Thomas, S.W. Koch, Coherent Semiconductor Optics From Basic Concepts to Nanostructure Applications, Springer, Berlin, 2007.
- [16] T. Meier, S.W. Koch, M. Phillips, H. Wang, Phys. Rev. B 62 (2000) 12605.
- [17] P. Brick, C. Ell, S. Chatterjee, G. Khitrova, H.M. Gibbs, T. Meier, C. Sieh, S.W. Koch, Phys. Rev. B 64 (2001) 075323.
- [18] E. Finger, S.P. Kraft, M. Hofmann, T. Meier, S.W. Koch, W. Stolz, W.W. Rühle, Phys. Status Solidi (b) 234 (2002) 424.
- [19] A. Euteneuer, E. Finger, M. Hofmann, W. Stolz, T. Meier, P. Thomas, S.W. Koch, W.W. Rühle, R. Hey, K. Ploog, Phys. Rev. Lett. 83 (1999) 2073.
- [20] V.M. Axt, A. Stahl, Z. Phys. B 93 (1994) 195; 93 (1994) 205.
- [21] M. Lindberg, Y.Z. Hu, R. Binder, S.W. Koch, Phys. Rev. B 50 (1994) 18060.
- [22] I. Rumyantsev, N.H. Kwong, R. Takayama, R. Binder, Phys. Rev. B 65 (2002) 245325.
- [23] M. Lindberg, R. Binder, Y.Z. Hu, S.W. Koch, Phys. Rev. B 49 (1994) 16942.
- [24] I. Kuznetsova, Diploma Thesis, Marburg, 2003 (unpublished).
- [25] S.T. Cundiff, M. Koch, W.H. Knox, J. Shah, W. Stolz, Phys. Rev. Lett. 77 (1996) 1107.